

Nuclear Theory Group



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Institute of Research and Development

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Content

□ Group members

□ Research Topics

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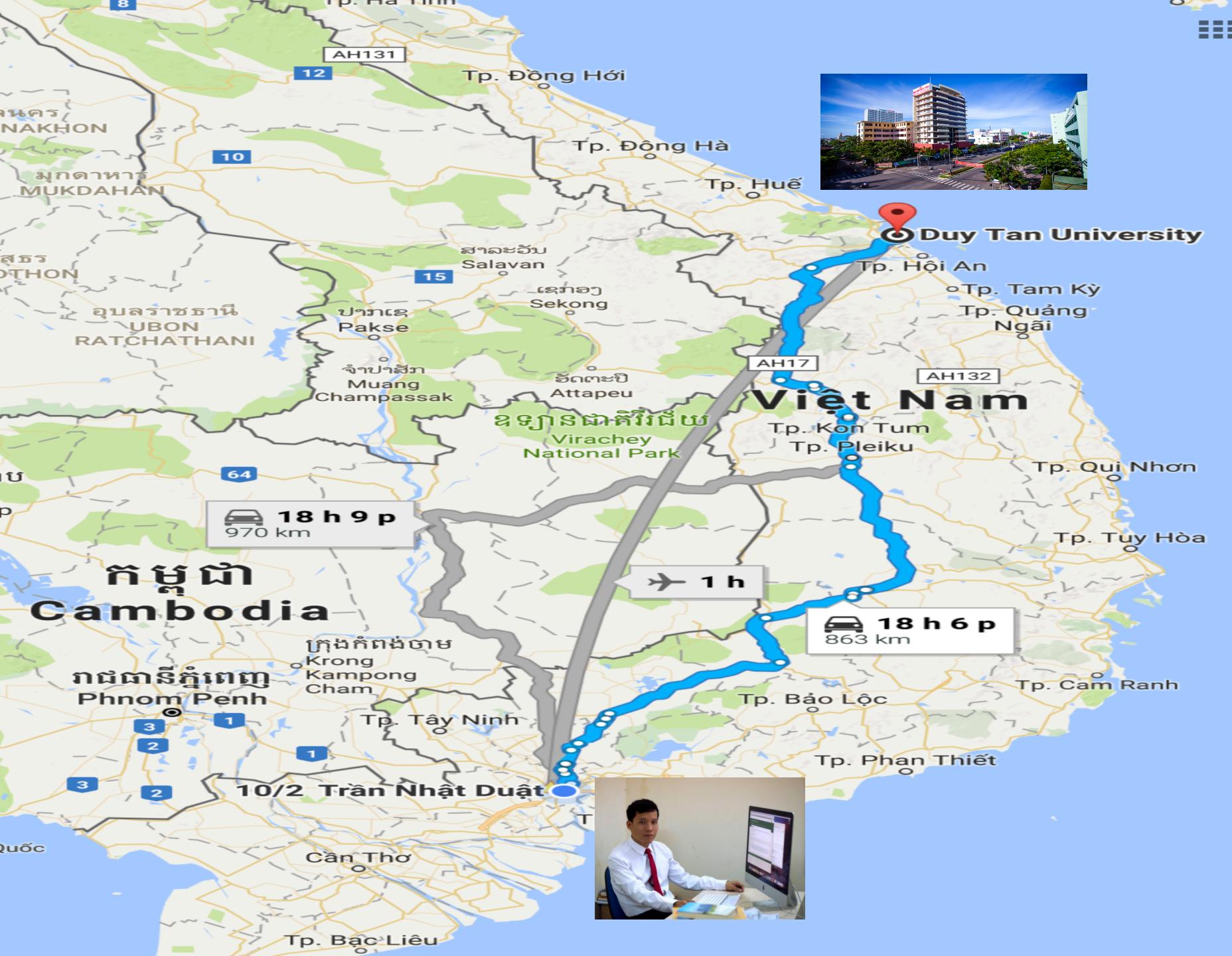
Balaram Dey, Deepak Pandit, Srijit Bhattacharya, K. Banerjee, Debasish Mondal, S. Mukhopadhyay, Surajit Pal, A. De, S. R. Banerjee (VEEC, Kolkata, **India**)

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L. Anh Tuyen, L. Chi Cuong, D. Duy Khiem, P. Trong Phuc, L. Ly Nguyen, N. T. Ngoc Hue, P. Thi Hue, and D. Van Phuc (Center for Nuclear Technique, HCM, **Vietnam**)

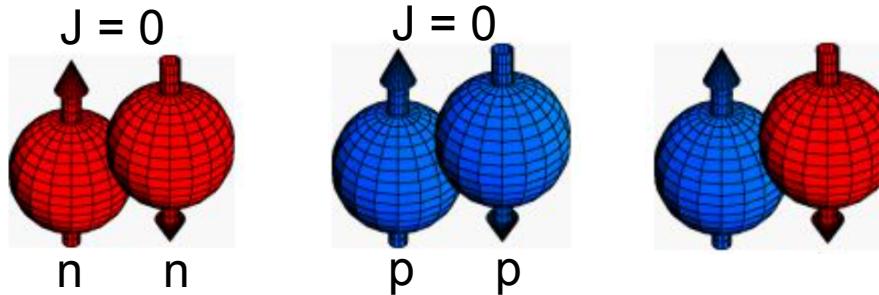
N. Ngoc Anh, N. Xuan Hai, P. Dinh Khang, Ho Huu Thang, V. Huu Tan (Nuclear Research Institute, Dalat, **Vietnam**)



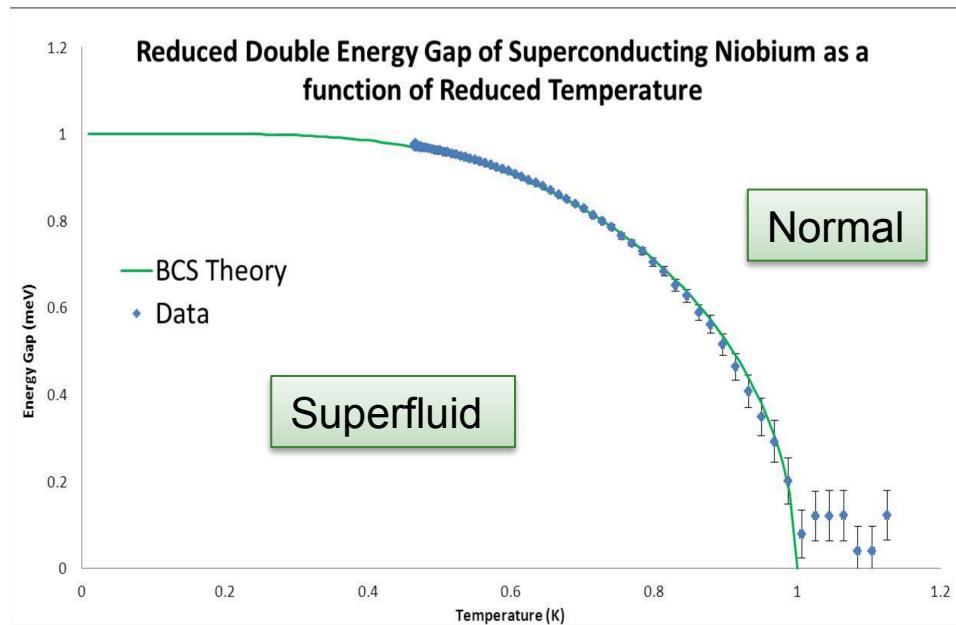
Research Topics

□ Past Research Topics:

✧ *Pairing Properties in Hot Rotating Nuclei*



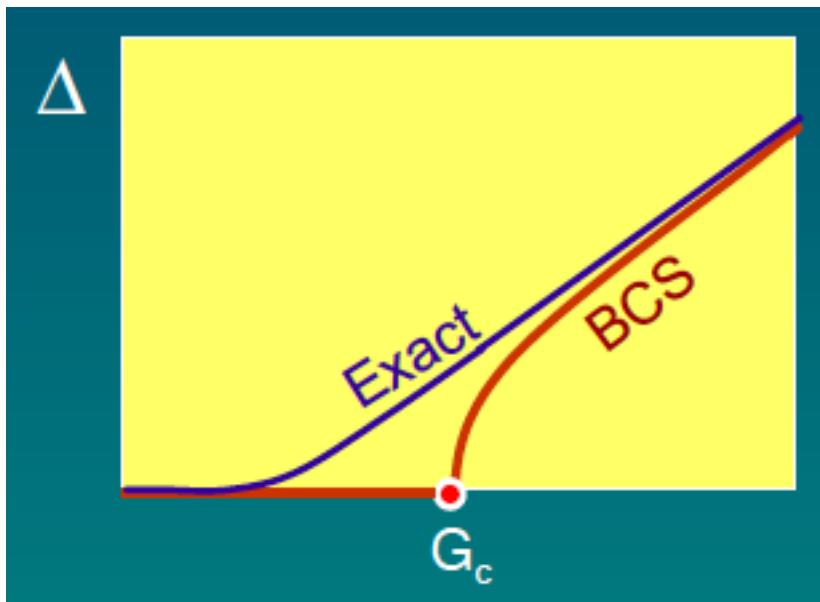
J. Bardeen, L. Cooper,
and J. Schrieffer, Phys.
Rev. 108, 1175 (1957)



Shortcomings of the BCS

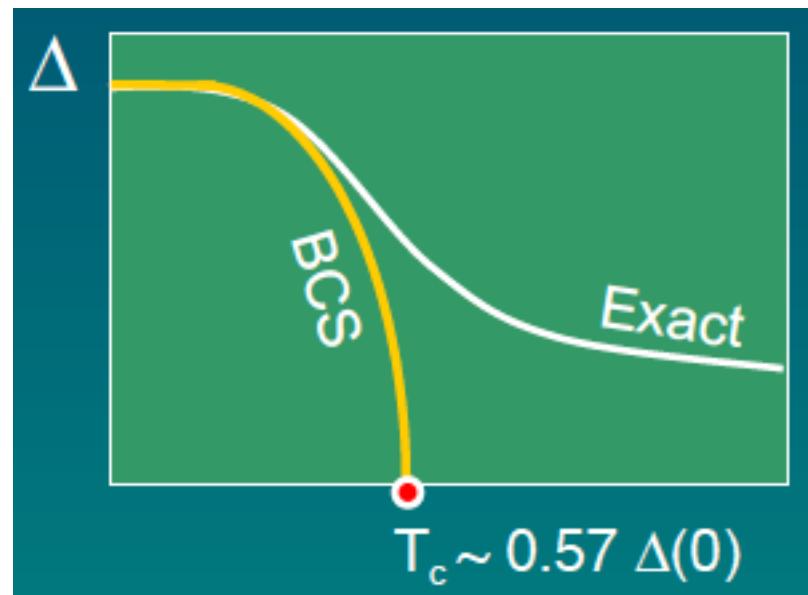
$T = 0$

- *Particle-number violation*
- *Collapse at $G \leq G_c$*



$T \neq 0$

- *No thermal fluctuations*
- *Collapse at $T \geq T_c$*



Past Research Topics

Macroscopic Landau theory

L. G. Moretto, Phys. Lett. B 40, 1 (1972)

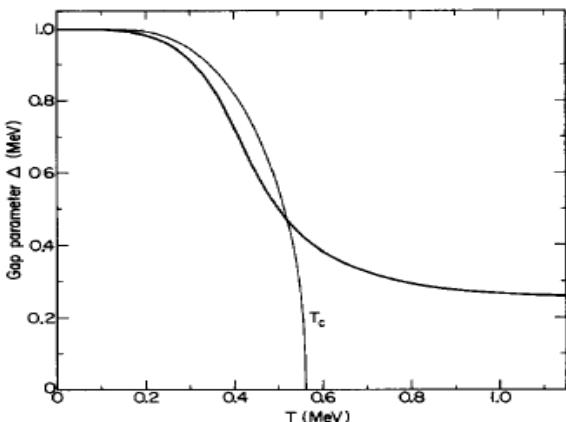


Fig. 2. The average gap parameter (thick line) and the most probable gap parameter is a function of temperature.

HFB at finite temperature

A. Goodman, Phys. Rev. C 29, 1887 (1984)

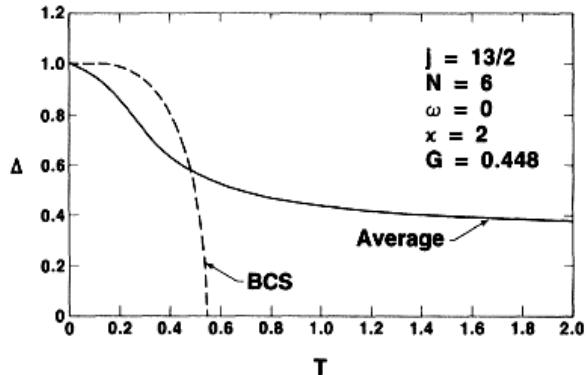
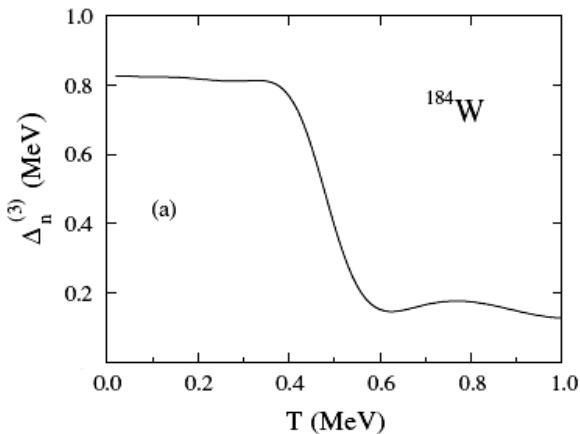


FIG. 15. The pair gap Δ versus the temperature T for $\omega=0$. The dashed curve is the BCS or most probable Δ , and the solid curve is the average Δ .

Pairing in Hot Nuclei

From experimentally extracted gap

K. Kaneko and M. Hasegawa, Phys. Rev. C 72, 024307 (2005)

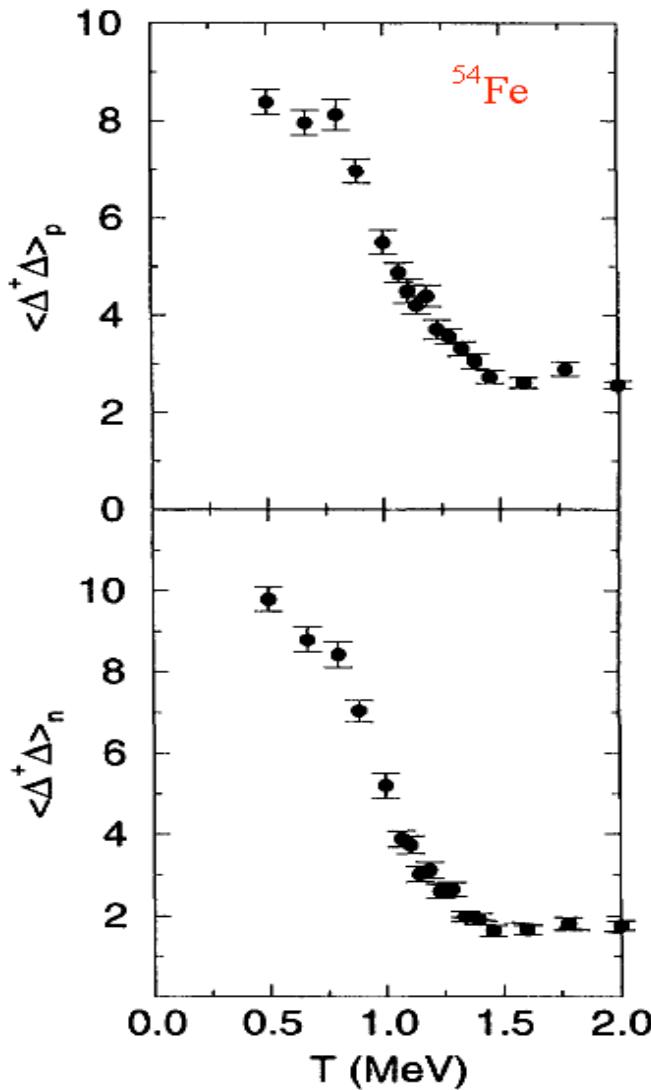


In finite nuclei,
thermal fluctuations
smooth out the sharp
superfluid-normal
(SN) phase transition

Thermal
fluctuations ?

Shell-model Monte-Carlo

Dean et. al, Phys. Rev. Lett. 74, 2909 (1995)



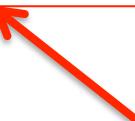
Past Research Topics

Pairing in Hot Nuclei

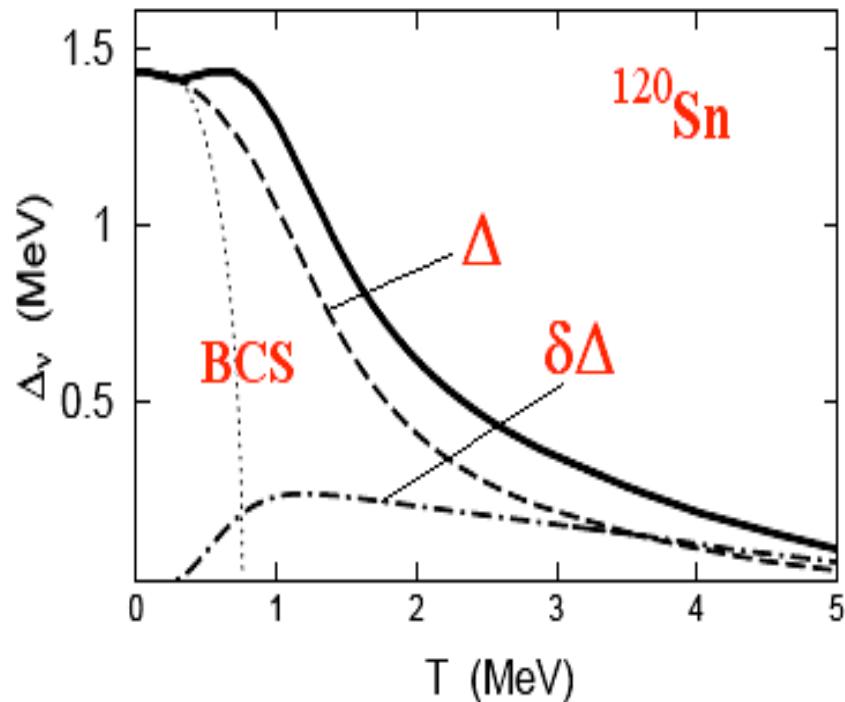
Modified BCS (MBCS):

*N. Dinh Dang and V. Zelevinsky, Phys. Rev. C 64, 064319 (2001);
N. Dinh Dang and A. Arima, Phys. Rev. C 67, 014304 (2003).*

$$\bar{\Delta} = \Delta_{quantal} + \delta \Delta_{thermal} = G \sum_j u_j v_j (1 - 2n_j) + G(1 - 2v_j^2) \delta N_j$$
$$\delta N_j = \sqrt{n_j(1-n_j)}; n_j = [1 + e^{E_j/T}]^{-1}$$



Quasiparticle-number
fluctuations (QNF)



Past Research Topics

Pairing in Hot Rotating Nuclei

Magnetic field H

Superconductor

H

Superfluid

Normal

T

Angular momentum (velocity)

Nucleus

ω

Normal

Superfluid

T

Past Research Topics

Pairing Reentrance

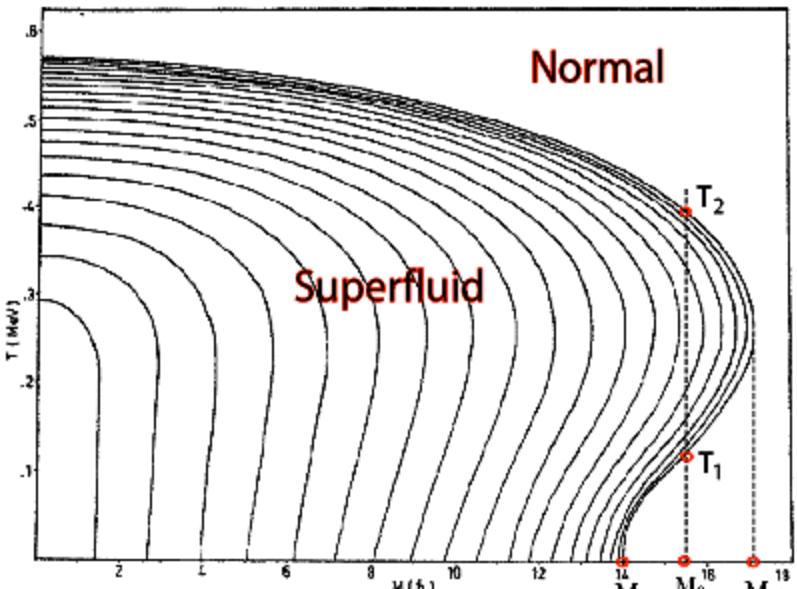
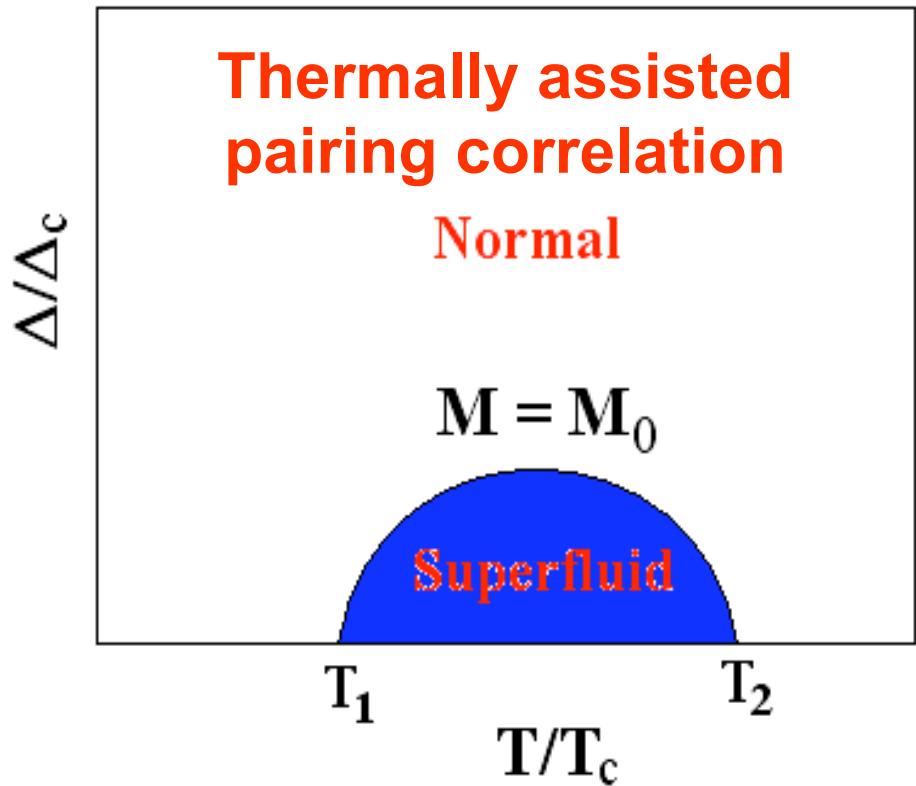
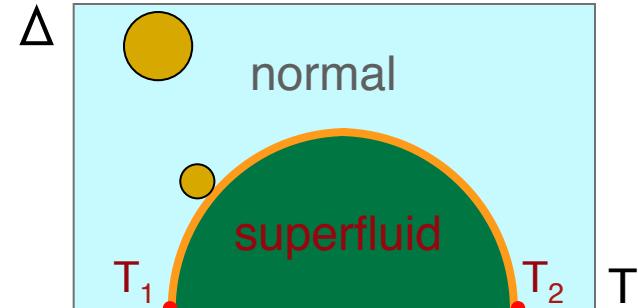
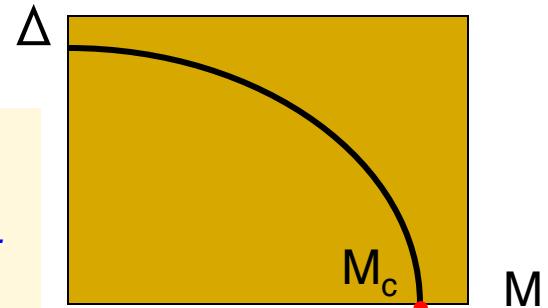
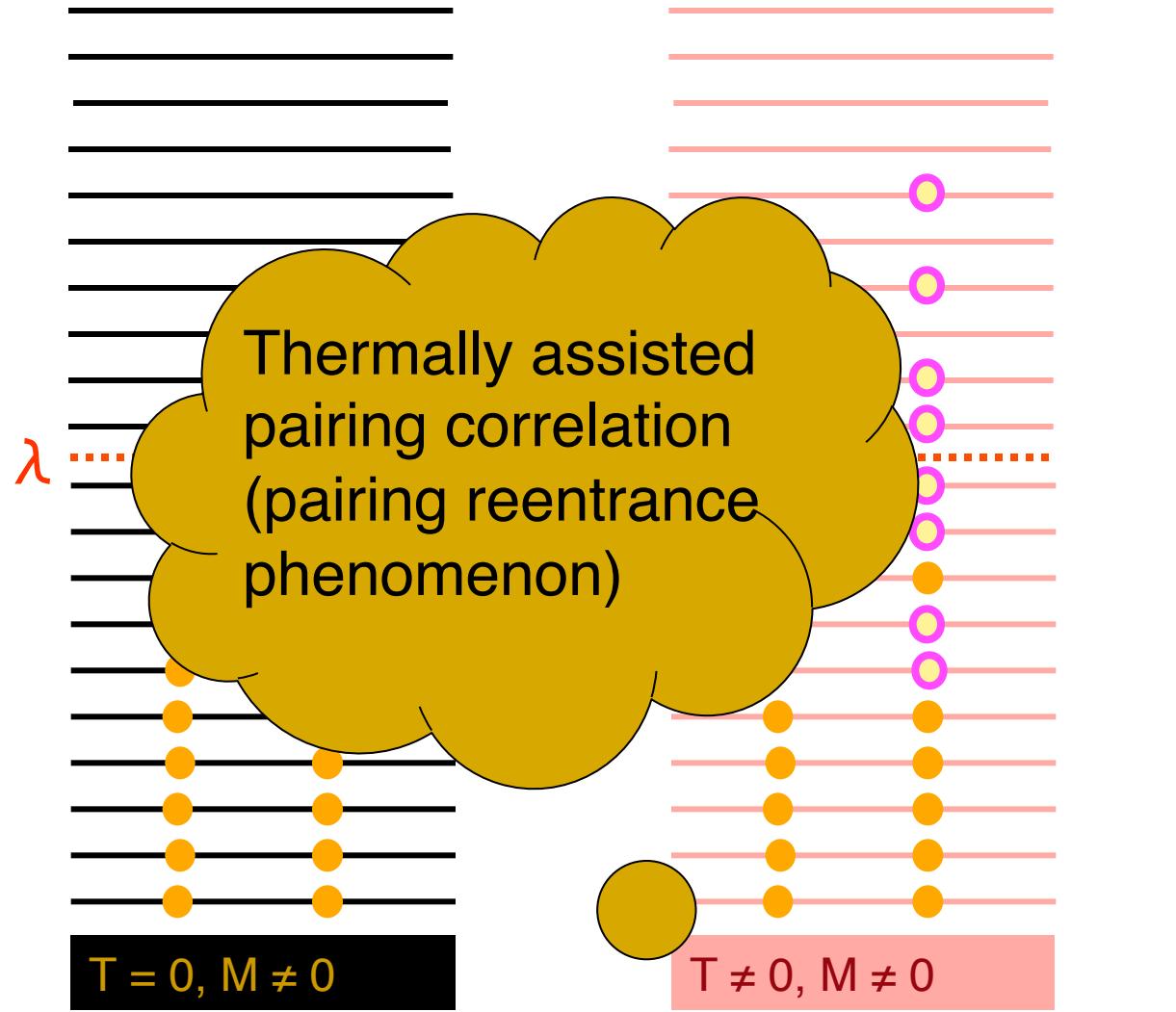
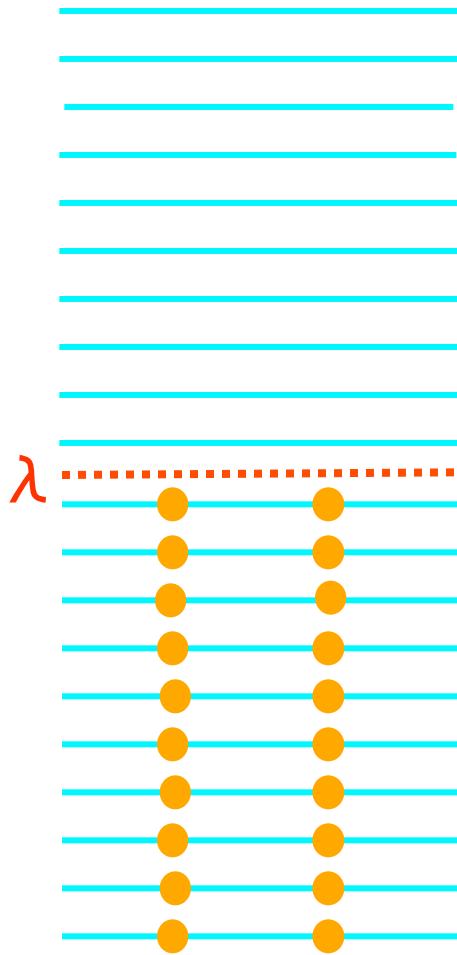


Fig. 7. Contour map of the gap parameter as a function both of temperature and angular momentum. The spacing in Δ between two successive lines is 0.05 MeV from $\Delta = 1.0$ MeV to $\Delta = 0.1$ MeV. The outer line corresponds to $\Delta = 0$ MeV.

Non-collective Rotation



L. G. Moretto, *Phys. Lett. B* **35**, 379 (1971);
Nucl. Phys. A **185**, 145 (1972); *Nucl. Phys. A* **216**, 1 (1973)



L. G. Moretto, Nucl. Phys. A 185, 145 (1972);

R. Balian, H. Flocard, M. Vénéroni, Phys. Rep. 317, 251 (1999)

Past Research Topics

Pairing Reentrance

Exact solution of degenerate model, canonical ensemble for cluster and nuclei

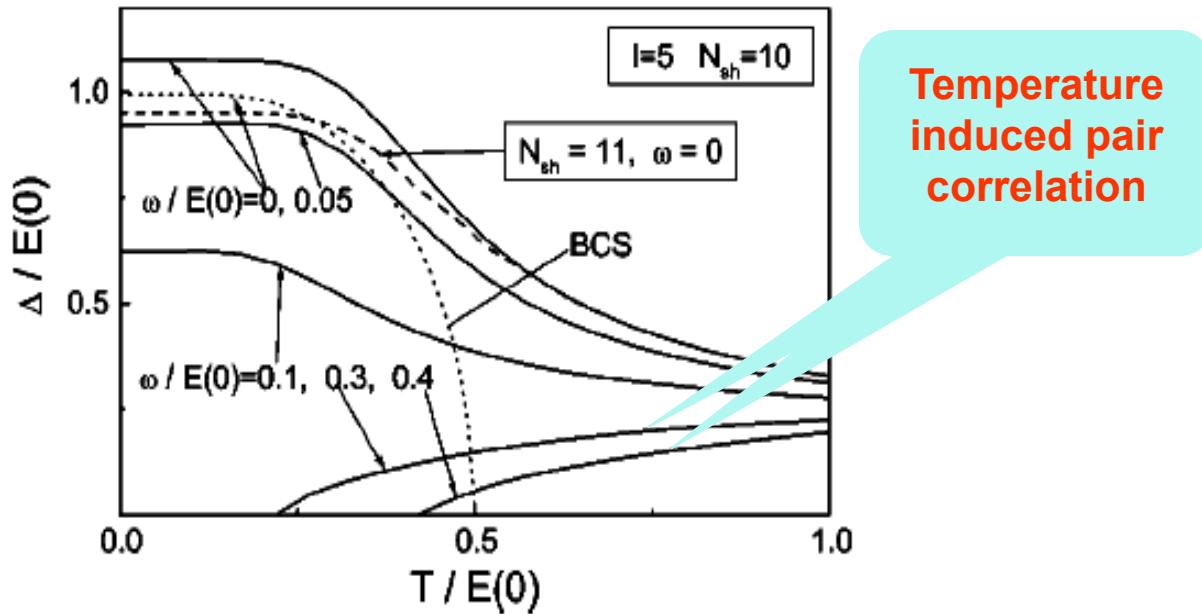
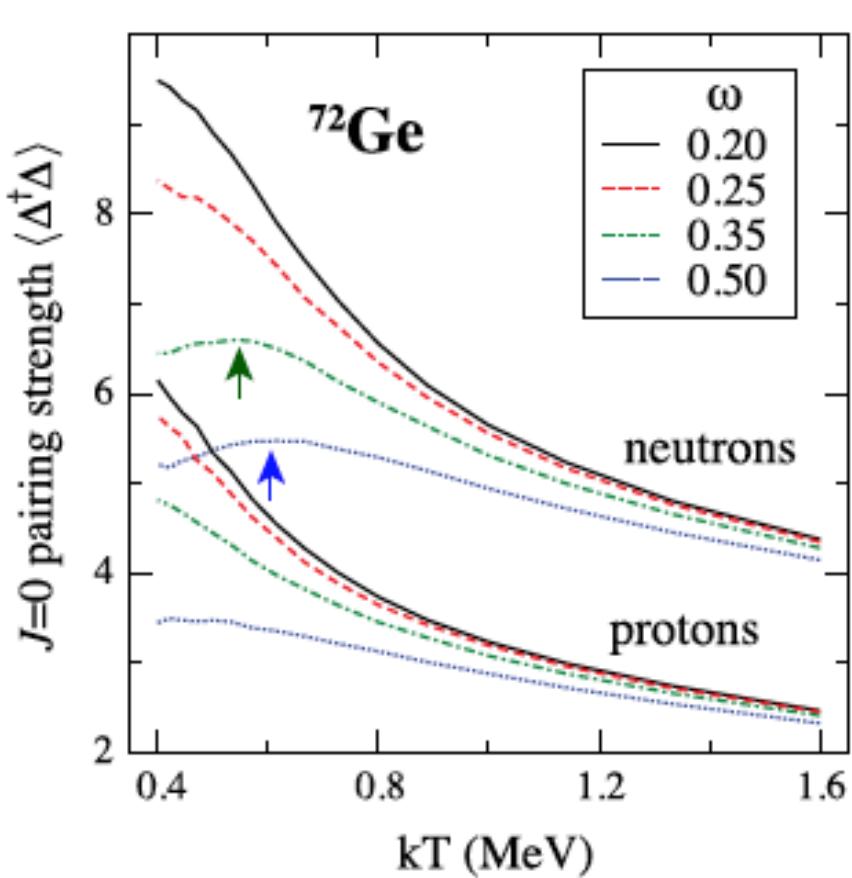


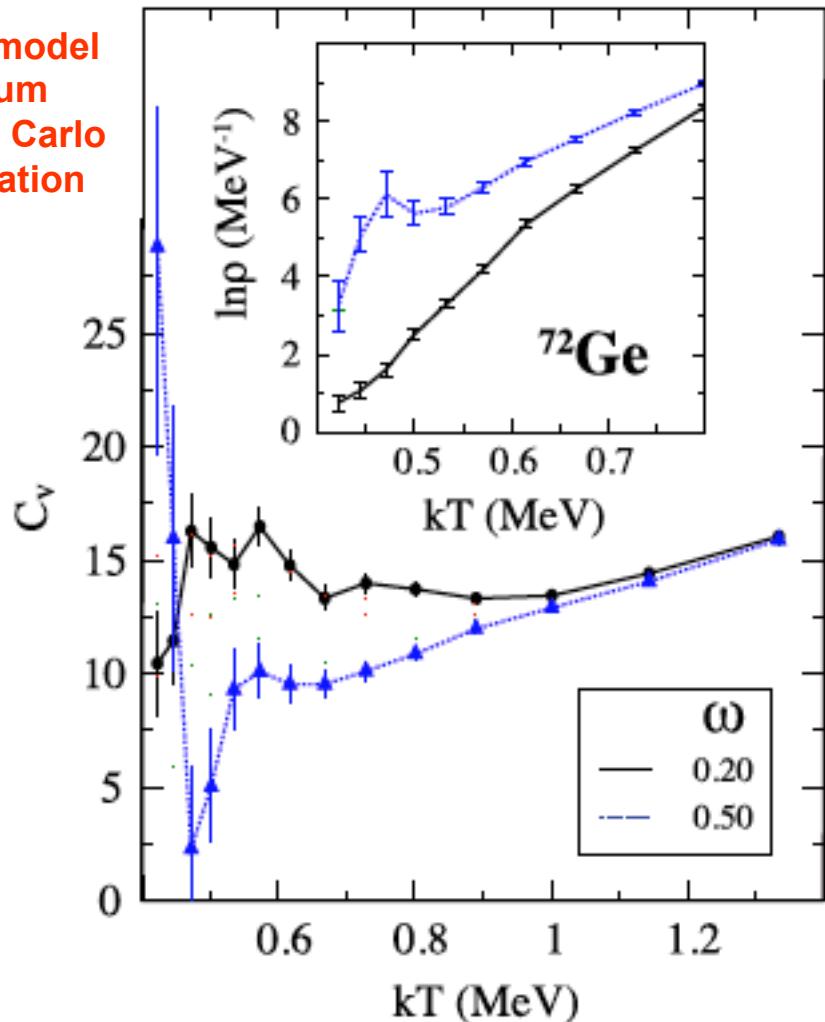
FIG. 2. Canonical gap $\Delta_{\text{can}}(T, \omega)$ for even (full lines) and odd (the dashed line) particle numbers, and the mean-field gap $\Delta_{\text{mf}}(T, \omega)$ (dotted line -BCS) vs the temperature T for a spherical shell.

Past Research Topics

Pairing Reentrance



Shell model
quantum
Monte Carlo
calculation



Magnetic Field-Induced Superconductivity in the Ferromagnet URhGe

F. Lévy *et al.*

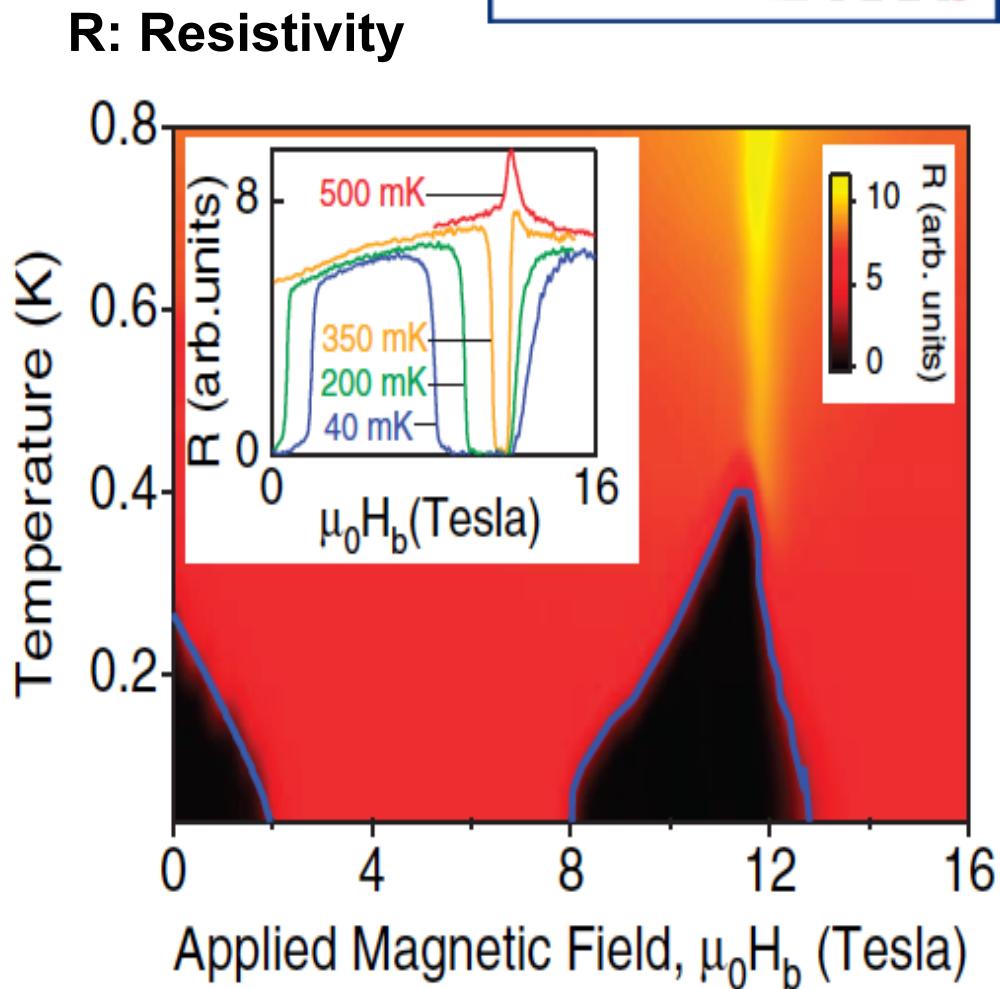
Science 309, 1343 (2005);

DOI: 10.1126/science.1115498

Science

AAAS

- ❖ $T < T_c$ (290 mK) and $H \sim 2T$:
superconductivity ($R = 0$)
- ❖ $2T < H < 8T$
no superconductivity
- ❖ $T \sim 400$ mK and $8T < H < 13T$:
superconductivity reappeared



FTBCS1 at T≠0 & M≠0

Pairing Hamiltonian including z-projection of total angular momentum:

$$H = \sum_{k,\sigma=\pm 1} \varepsilon_k a_{k\sigma}^+ a_{k\sigma} - G \sum_{kk'} a_{k+}^+ a_{k-}^+ a_{k'-} a_{k'+} ,$$

Bogoliubov transformation + variational procedure:

$$\Delta_k = \Delta + \delta\Delta_k ,$$

$$\Delta = G \sum_k u_k v_k \langle D_k \rangle , \quad \underbrace{\langle D_k \rangle = 1 - n_k^+ - n_k^-}_{},$$

$$\delta\Delta_k = G u_k v_k \frac{\delta N_k^2}{\langle D_k \rangle} ,$$

Quasiparticle-number fluctuation:

$$\delta N_k^2 = n_k^+ (1 - n_k^+) + n_k^- (1 - n_k^-)$$

FTBCS1: $n_k^\pm = \frac{1}{1 + \exp[\beta(E_k \mp \gamma m_k)]} , \quad \langle A_k^+ A_{k'}^+ \rangle = \langle A_k^+ A_{k'}^- \rangle = 0 .$

$$H' = H - \lambda \hat{N} - \gamma \hat{M} ,$$

$$N = \sum_k (a_{k+}^+ a_{k+} + a_{k-}^+ a_{k-}) ,$$

$$M = \sum_k m_k (a_{k+}^+ a_{k+} - a_{k-}^+ a_{k-}) .$$

$$N = 2 \sum_k \left[v_k^2 + \frac{1}{2} (1 - 2v_k^2) (n_k^+ + n_k^-) \right]$$

$$M = \sum_k m_k (n_k^+ - n_k^-)$$

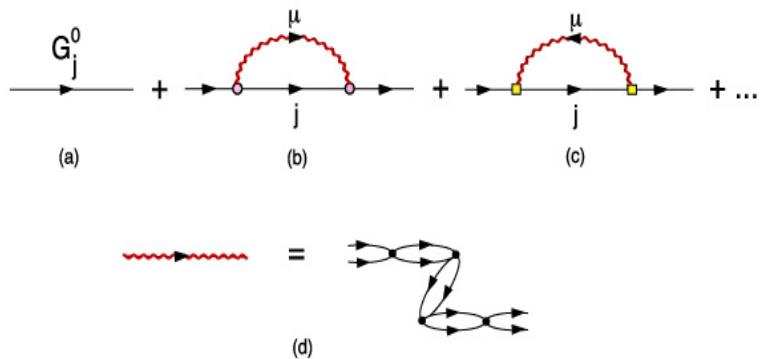
$$u_k^2 = \frac{1}{2} \left(1 + \frac{\varepsilon_k' - \lambda}{E_k} \right) , \quad v_k^2 = \frac{1}{2} \left(1 - \frac{\varepsilon_k' - \lambda}{E_k} \right)$$

$$E_k = \sqrt{(\varepsilon_k' - \lambda - G v_k^2)^2 + \Delta_k^2}$$

$$\varepsilon_k' = \varepsilon_k + \frac{G}{\langle D_k \rangle} \sum_k (u_{k'}^2 - v_{k'}^2) \left(\langle A_k^+ A_{k'}^+ \rangle + \langle A_k^+ A_{k'}^- \rangle \right)$$

$$A_k^+ = a_{k+}^+ a_{k-} .$$

FTBCS1+SCQRPA at T≠0 & M≠0



$$\begin{aligned} G_k^\pm(E) &= \frac{1}{2\pi} \frac{1}{E - \tilde{E}_k \mp \gamma m_k - M_k^\pm(E)} , \\ \tilde{E}_k &= b'_k + q_{kk} , \\ b'_k &= (\varepsilon_k - \lambda)(u_k^2 - v_k^2) + 2Gu_kv_k \sum_{k'} u_{k'}v_{k'} + Gv_k^4 , \\ q_{kk} &= -Gu_k^2v_k^2 , \quad g_k(k') = Gu_kv_k(u_{k'}^2 - v_{k'}^2) , \end{aligned}$$

$$M_k^\pm(E) = \sum_\mu \left(V_k^\mu \right)^2 \left[\frac{1 - n_k^\pm + \nu_\mu}{E - \tilde{E}_k \mp \gamma m_k - \omega_\mu} + \frac{n_k^\pm + \nu_\mu}{E - \tilde{E}_k \mp \gamma m_k + \omega_\mu} \right] ,$$

$$V_k^\mu = \sum_{k'} g_k(k') \sqrt{\langle D_{k'} \rangle} \left(X_{k'}^\mu + Y_{k'}^\mu \right) , \quad \gamma_k^\pm(\omega) = -\Im m \left[M_k^\pm(\omega \pm i\varepsilon) \right] .$$

$$n_k^\pm = \frac{1}{\pi} \int_{-\infty}^{\infty} \frac{\gamma_k(\omega) (e^{\beta\omega} + 1)^{-1}}{\left[\omega - \tilde{E}_k \mp \gamma m_k - M_k(\omega) \right]^2 + \gamma_k^2(\omega)} d\omega$$

Past Research Topics

Our methods:

- **FTBCS1**: FTBCS + Quasiparticle-number fluctuations (QNF)
- **FTLN1**: FTBCS1 + Lipkin-Nogami (approximate) particle-number projection
- **FTBCS1 + SCQRPA**: FTBCS1 self-consistently coupled to quasiparticle random-phase approximation (QRPA) vibrations
- **FTLN1 + SCQRPA**: FTLN1 self-consistently coupled to QRPA vibrations
- **CE(MCE)-LNBCS**: embed solutions of LNBCS equation at T=0 into the CE and MCE
- **CE(MCE)-LNSCQRPA**: embed solutions of LNSCQRPA equation at T=0 into the CE and MCE

N. Quang Hung and N. Dinh Dang, Phys. Rev. C 76, 054302 (2007).

N. Dinh Dang and N. Quang Hung, Phys. Rev. C 77, 064315 (2008).

N. Quang Hung and N. Dinh Dang, Phys. Rev. C 78, 064315 (2008).

N. Quang Hung and N. Dinh Dang, Phys. Rev. C 79, 054328 (2009).

N. Quang Hung and N. Dinh Dang, Phys. Rev. C 81, 044301 (2010).

N. Quang Hung and N. Dinh Dang, Phys. Rev. C 81, 057302 (2010).

N. Quang Hung and N. Dinh Dang, Phys. Rev. C 82, 044316 (2010).

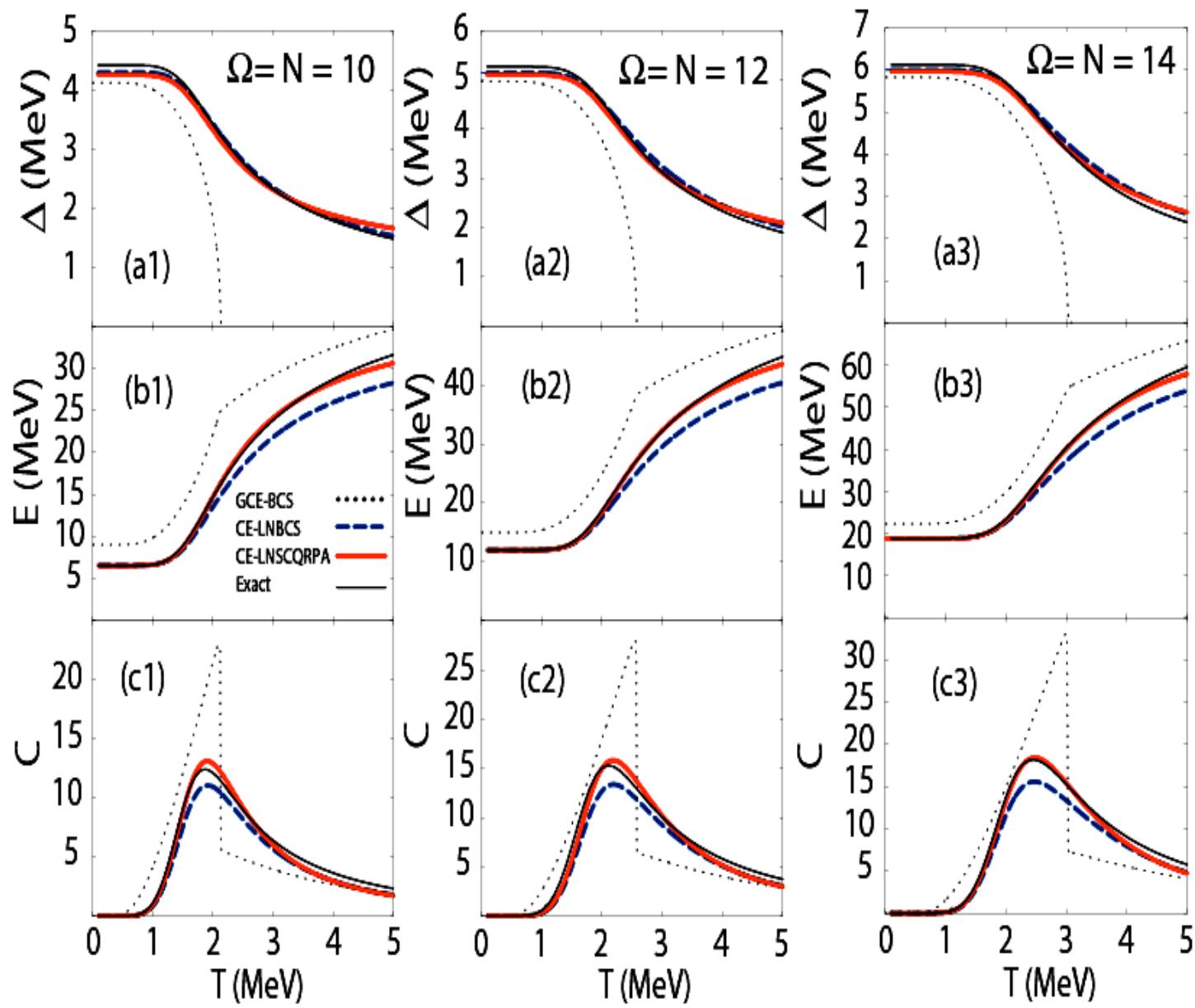
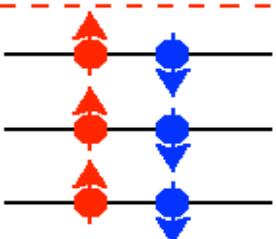
Hot Nuclei

Doubly-fold
equidistant multilevel
pairing model

$$\Omega = N = 6$$

$$G = 0$$

1 MeV



N. Quang Hung and N. Dinh Dang, Phys. Rev. C 81, 057302 (2010).
N. Quang Hung and N. Dinh Dang, Phys. Rev. C 82, 044316 (2010).

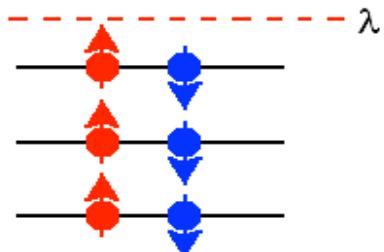
Hot Nuclei

Doubly-fold
equidistant multilevel
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$$\Omega = N = 6$$

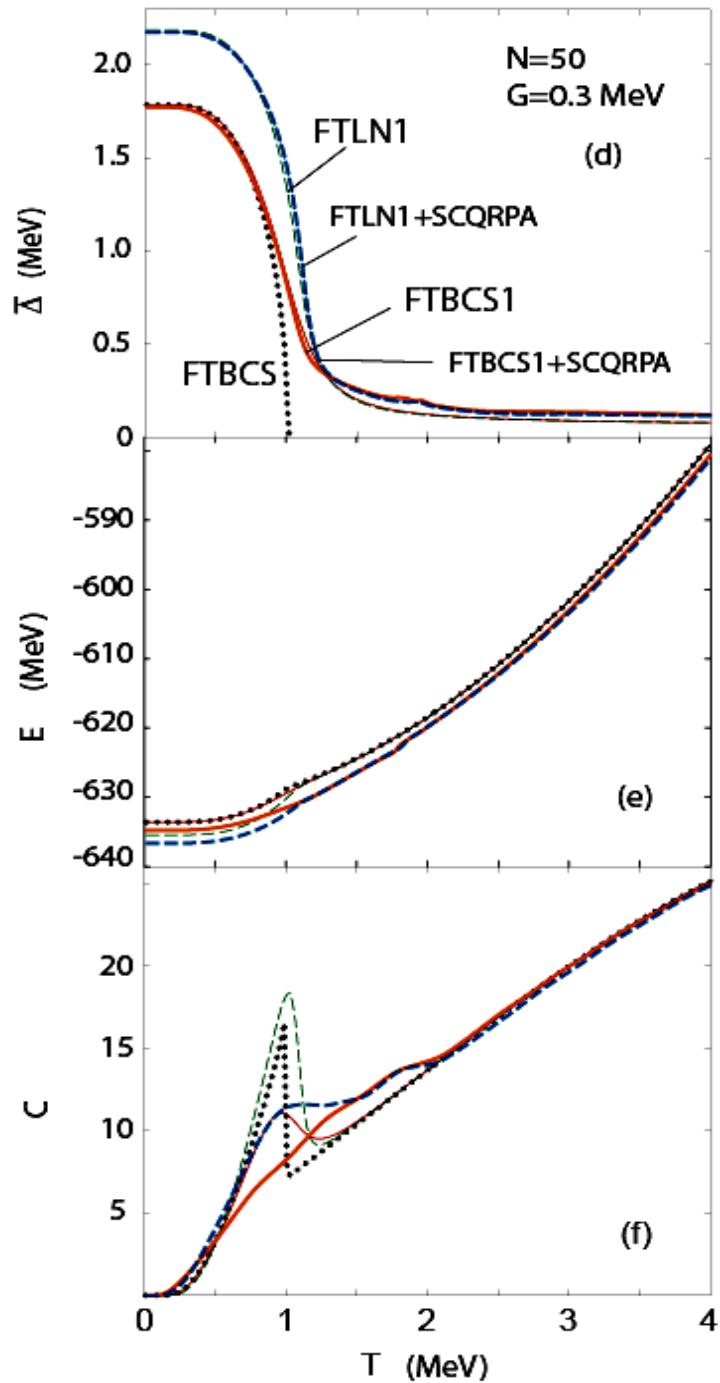
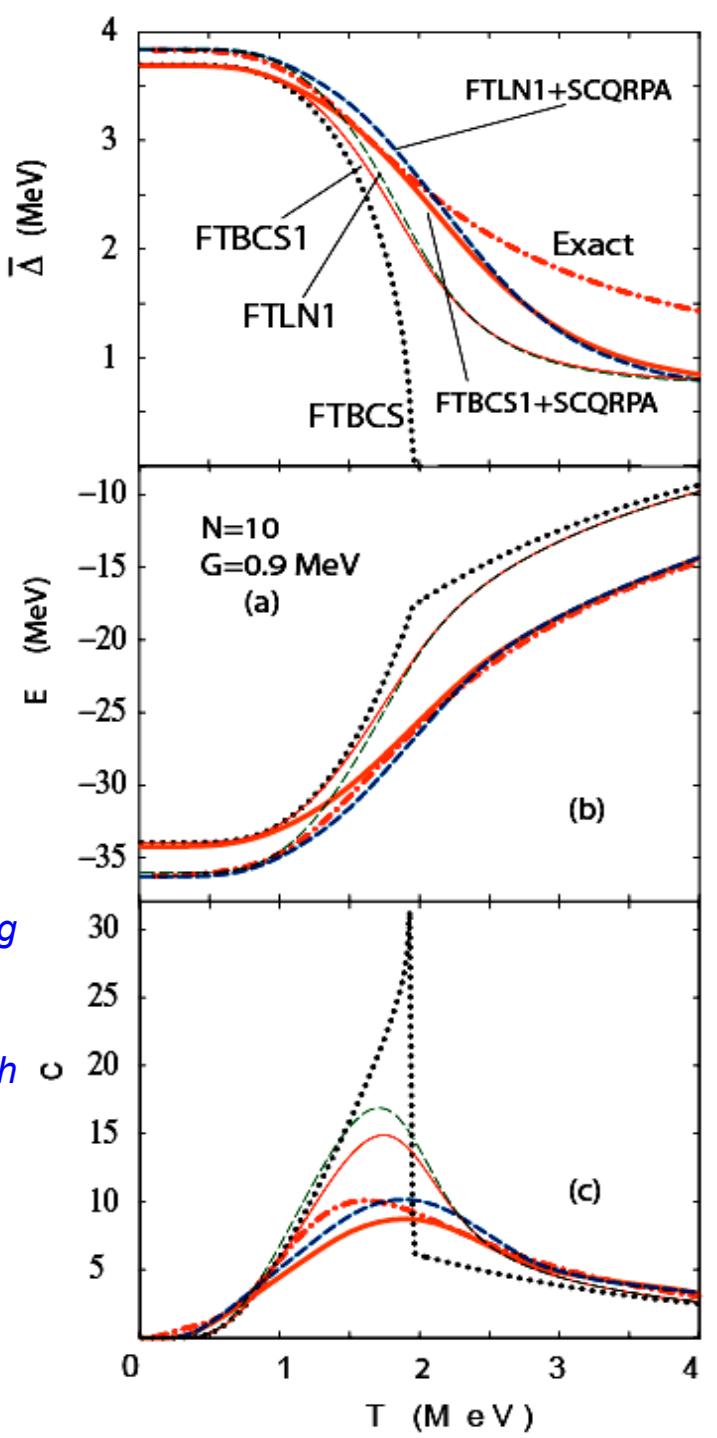
$$G = 0$$

1 MeV



N. Dinh Dang and N. Quang Hung, Phys. Rev. C 77, 064315 (2008).

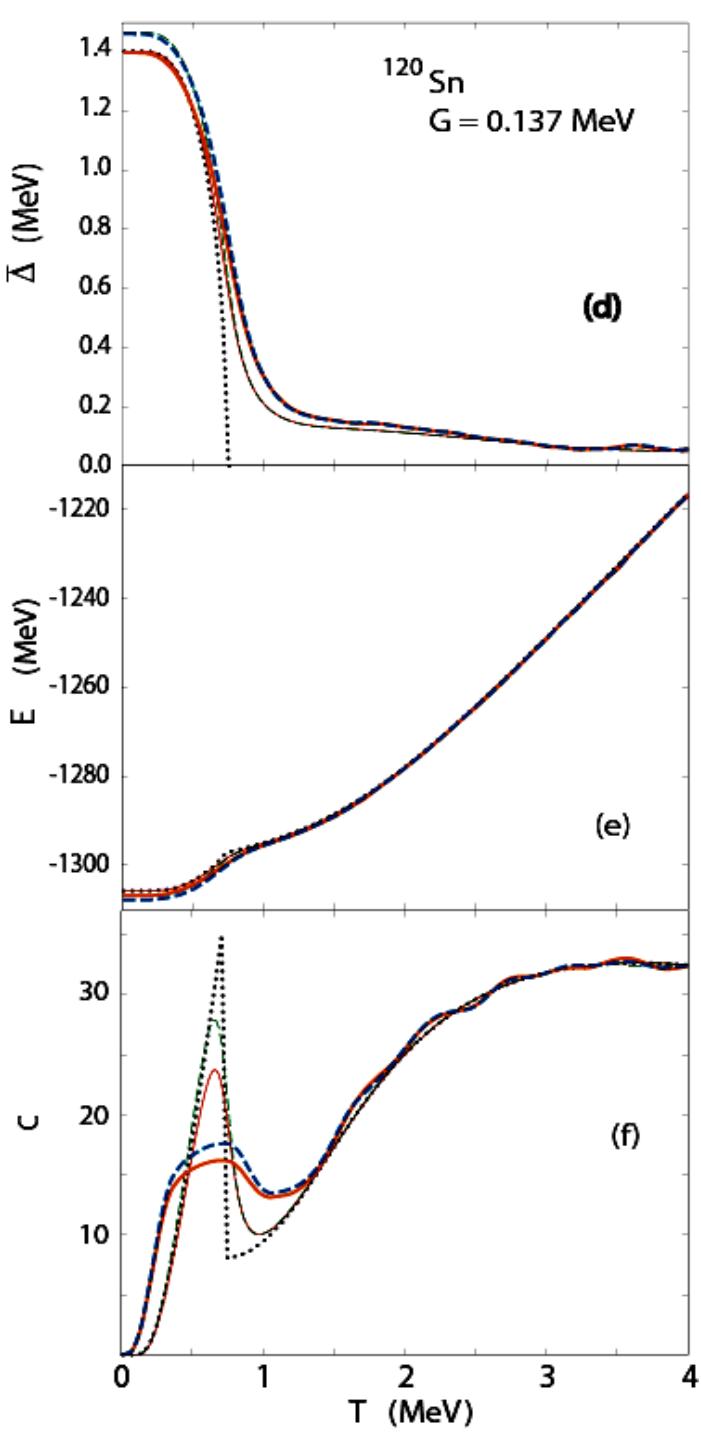
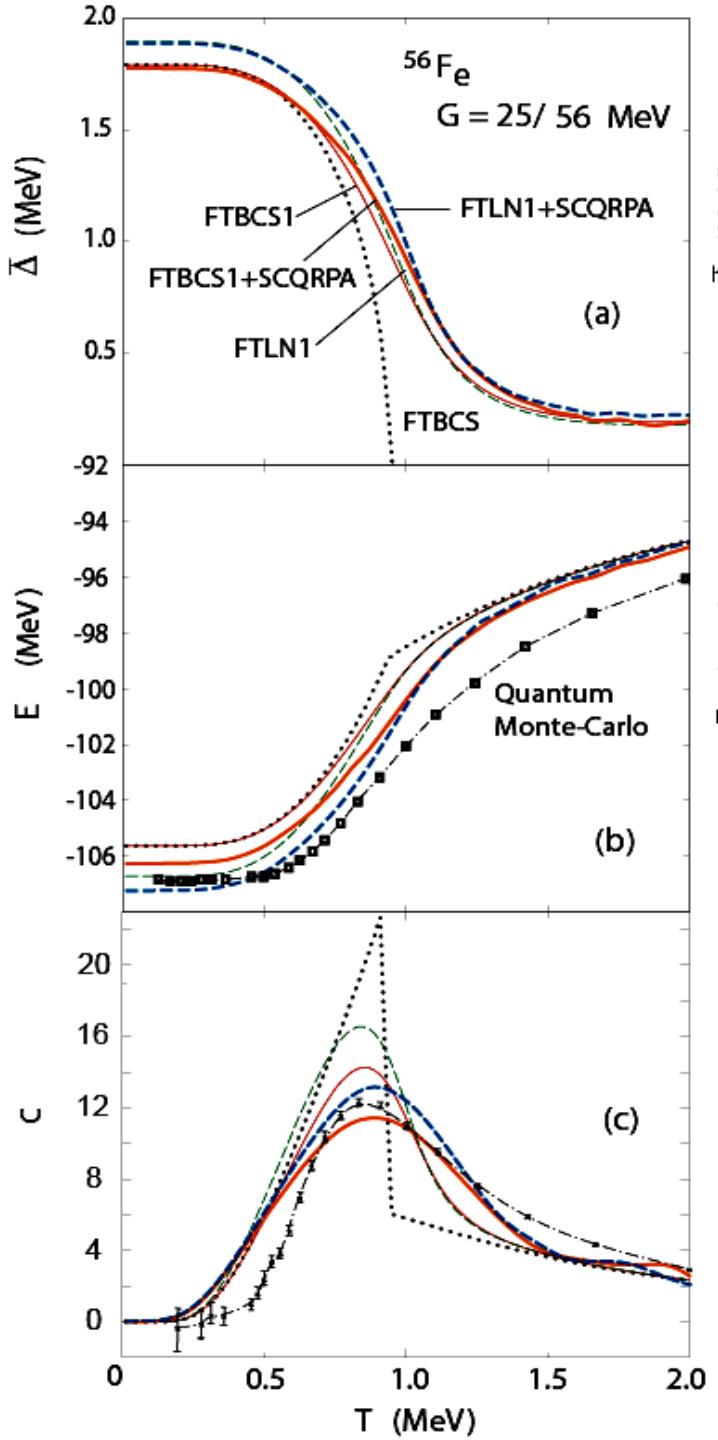
N. Quang Hung and N. Dinh Dang, Phys. Rev. C 79, 054328 (2009).



Hot Nuclei

N. Dinh Dang and N. Quang Hung, Phys. Rev. C 77, 064315 (2008).

N. Quang Hung and N. Dinh Dang, Phys. Rev. C 79, 054328 (2009).



CE-LNBCS(LNSCQRPA)

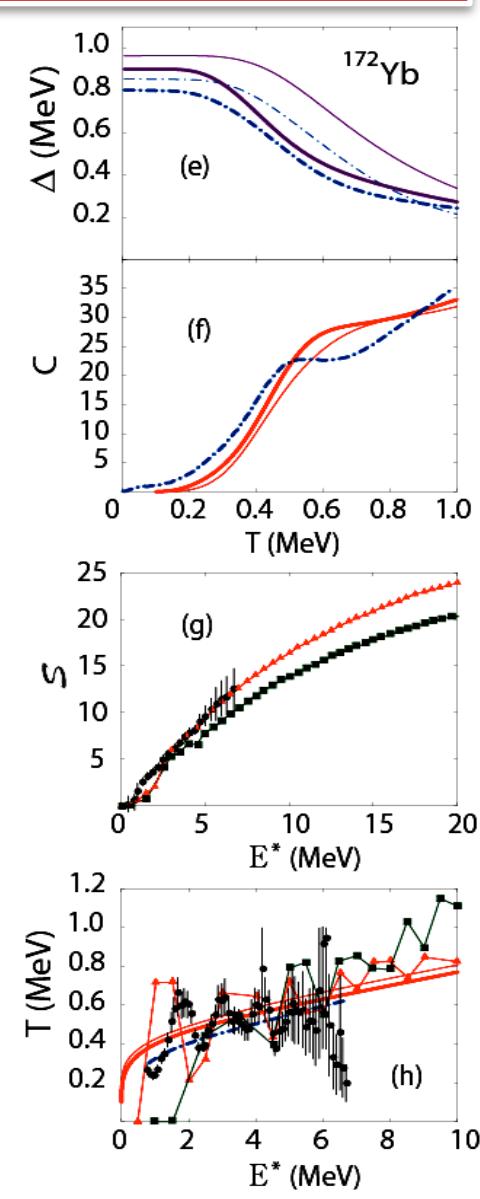
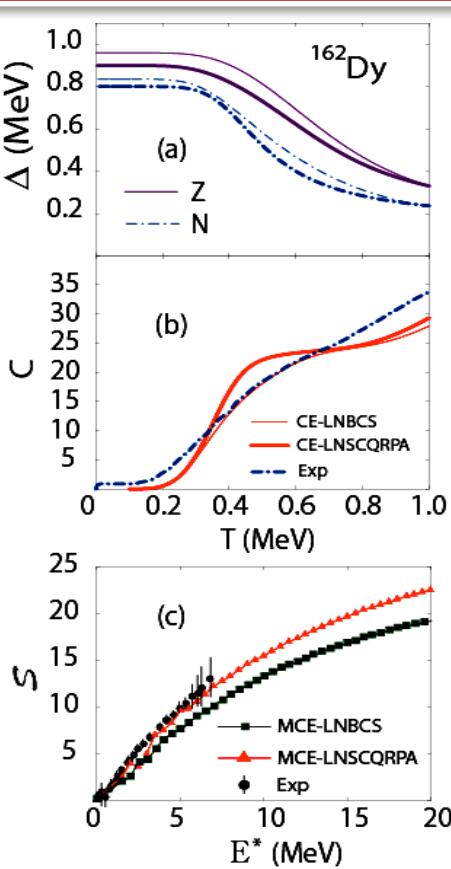
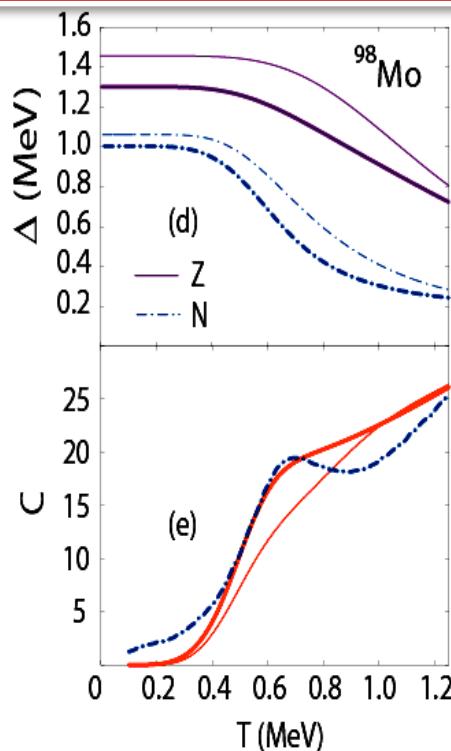
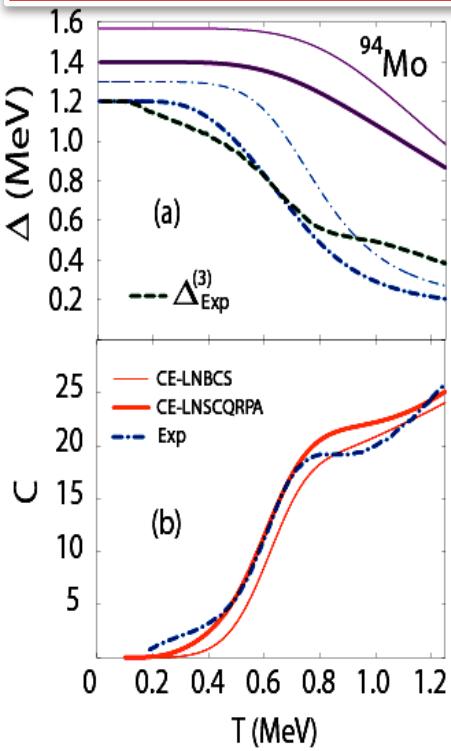
TABLE I. Number of eigenstates and computation time for the exact, CE-LNBCS and CE-LNSCQRPA calculations within the doubly-folded equidistant multilevel pairing model at several values of $N = \Omega$. The computation time is estimated based on a shared large memory computer Altix 450 with 512GB memory of RIKEN Integrated Cluster of Clusters (RICC) system.

N	Number of eigenstates			Computation time		
	Exact	LNBCS	LNSCQRPA	Exact	LNBCS	LNSCQRPA
10	8953	512	2560	1 hr	1 sec.	10 sec.
12	73789	2048	12288	10 hrs	10 sec.	1 min.
14	616227	8192	57344	24 hrs	1 min.	10 min.
16	5196627	32768	262144	-	10 min.	1 hr
18	44152809	131072	1179648	-	1 hr	3 hrs
20	377379369	524288	5242880	-	3 hrs	10 hrs

N. Quang Hung and N. Dinh Dang, Phys. Rev. C 81, 057302 (2010).

N. Quang Hung and N. Dinh Dang, Phys. Rev. C 82, 044316 (2010).

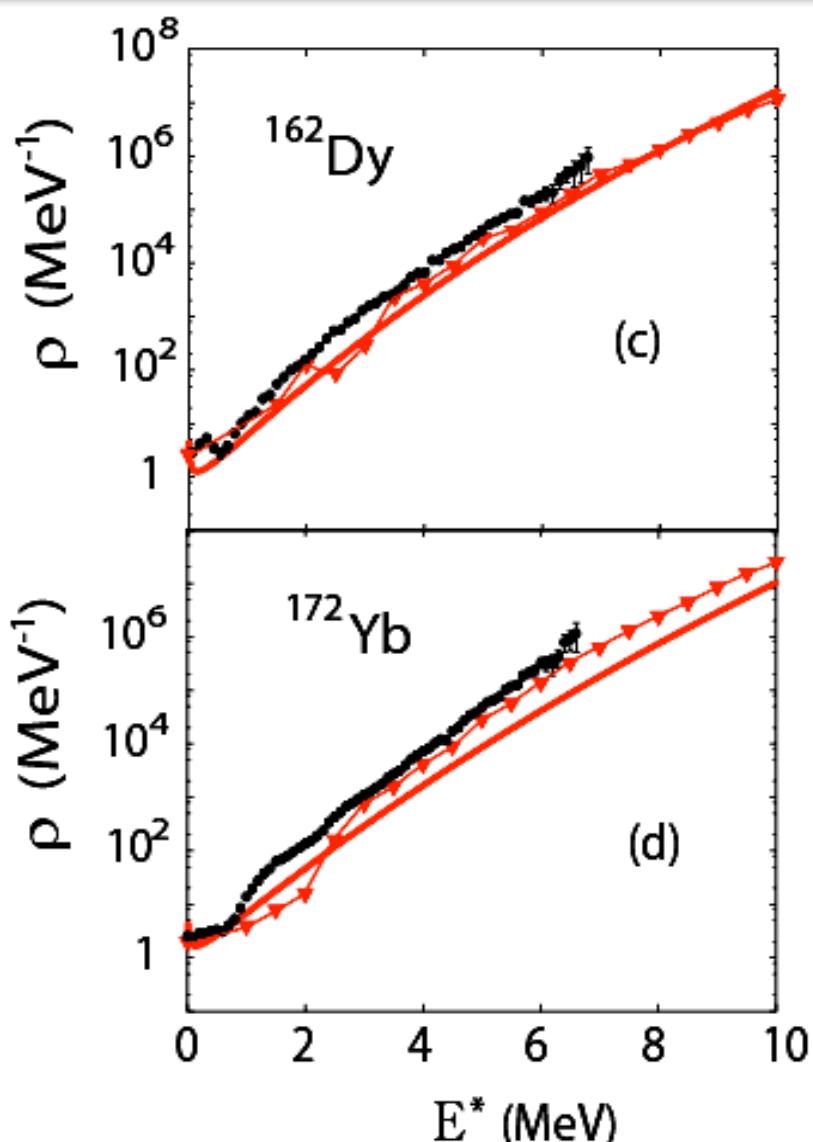
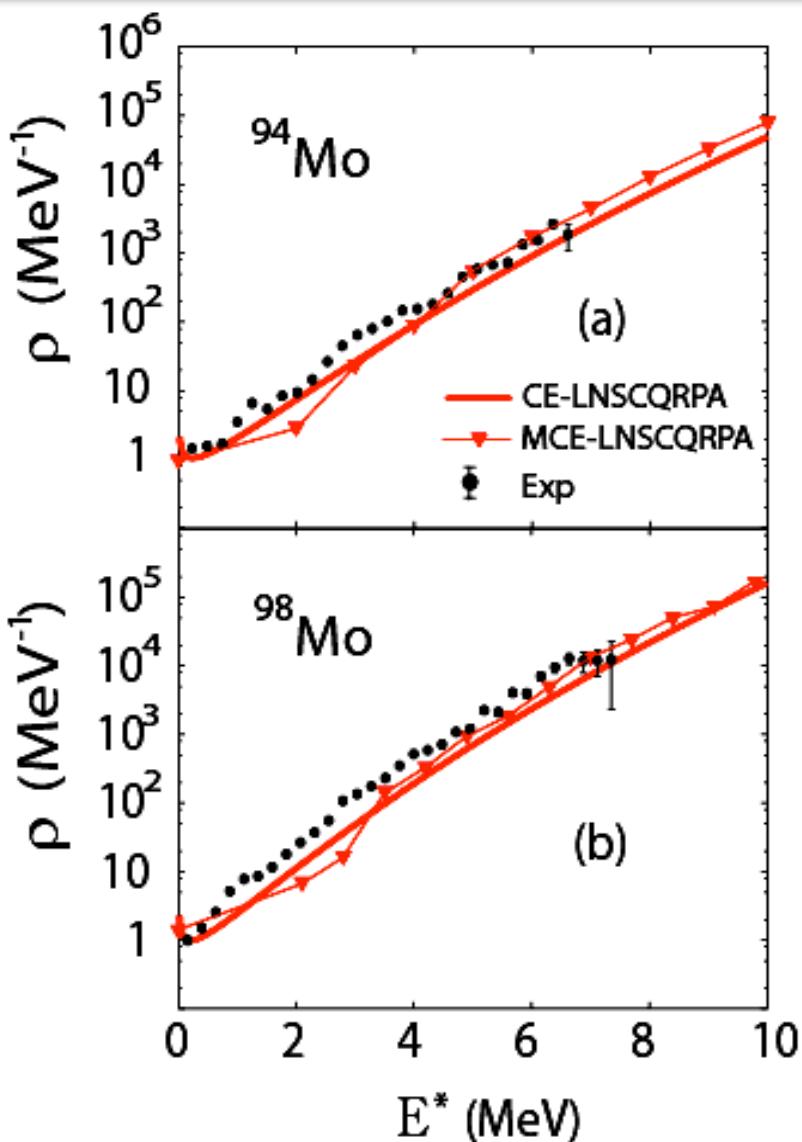
Hot Nuclei



N. Quang Hung and N. Dinh Dang, Phys. Rev. C 81, 057302 (2010).

N. Quang Hung and N. Dinh Dang, Phys. Rev. C 82, 044316 (2010).

Hot Nuclei

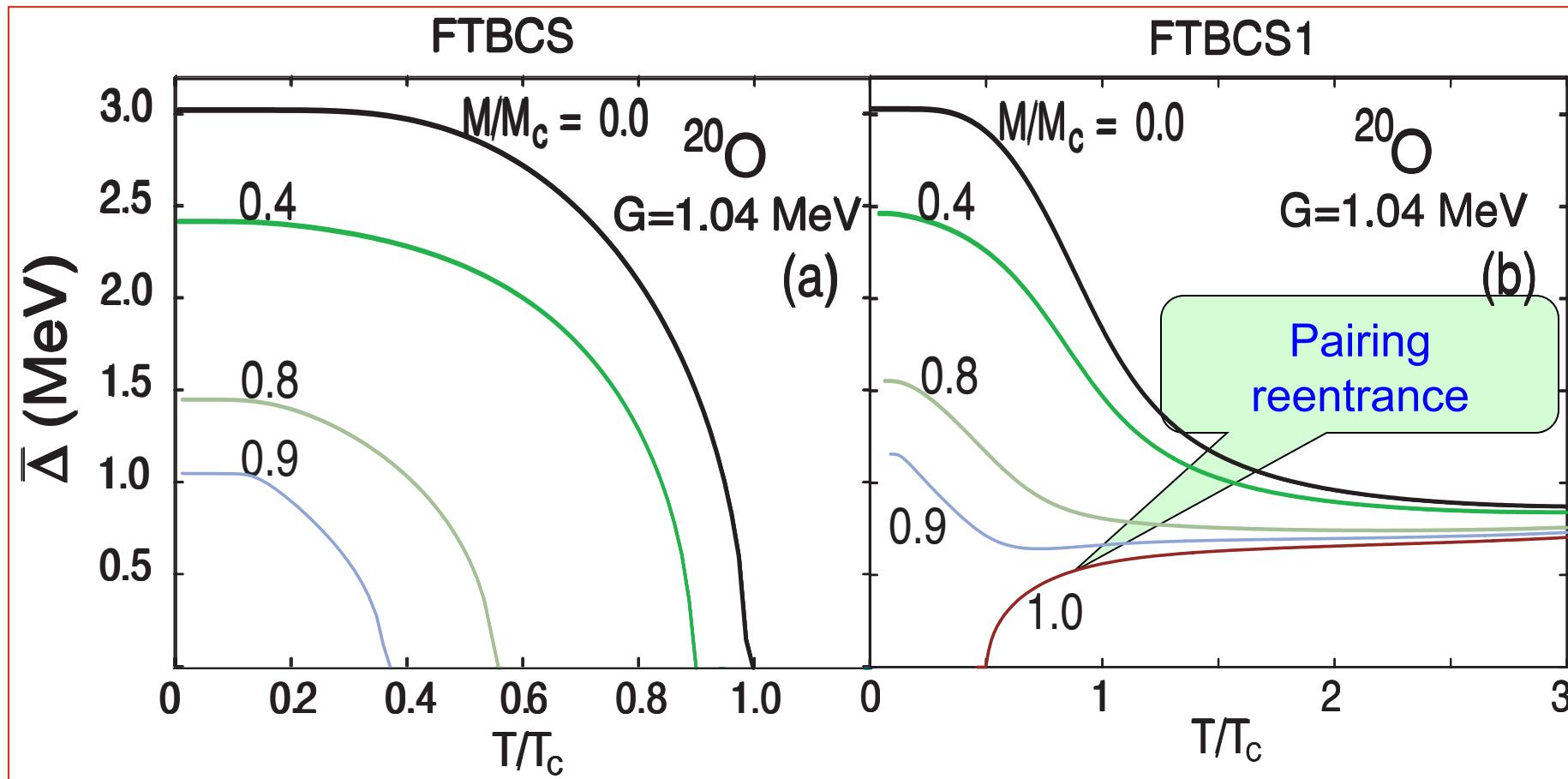


N. Quang Hung and N. Dinh Dang, Phys. Rev. C 81, 057302 (2010).

N. Quang Hung and N. Dinh Dang, Phys. Rev. C 82, 044316 (2010).

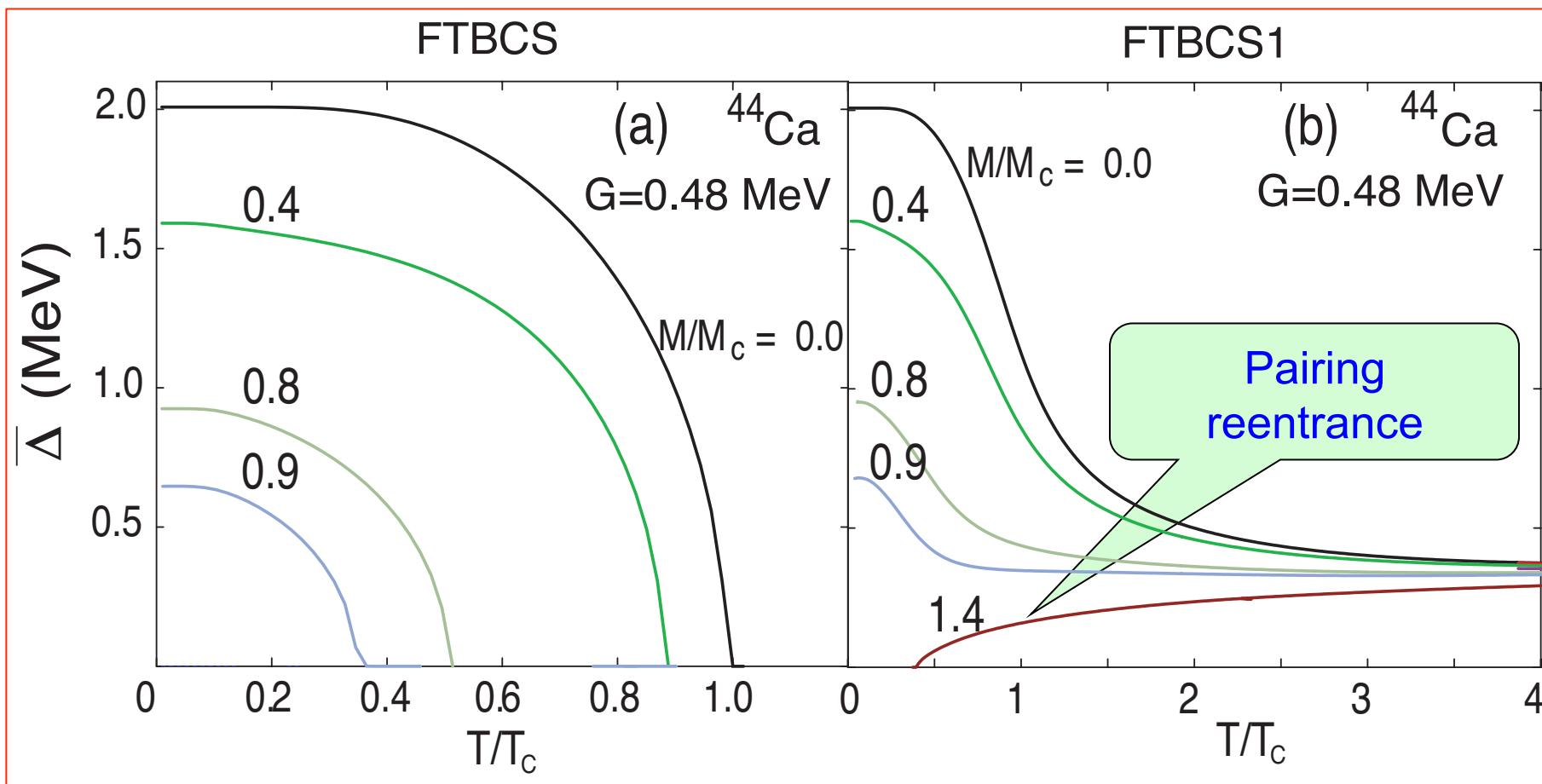
Hot Rotating Nuclei

22O



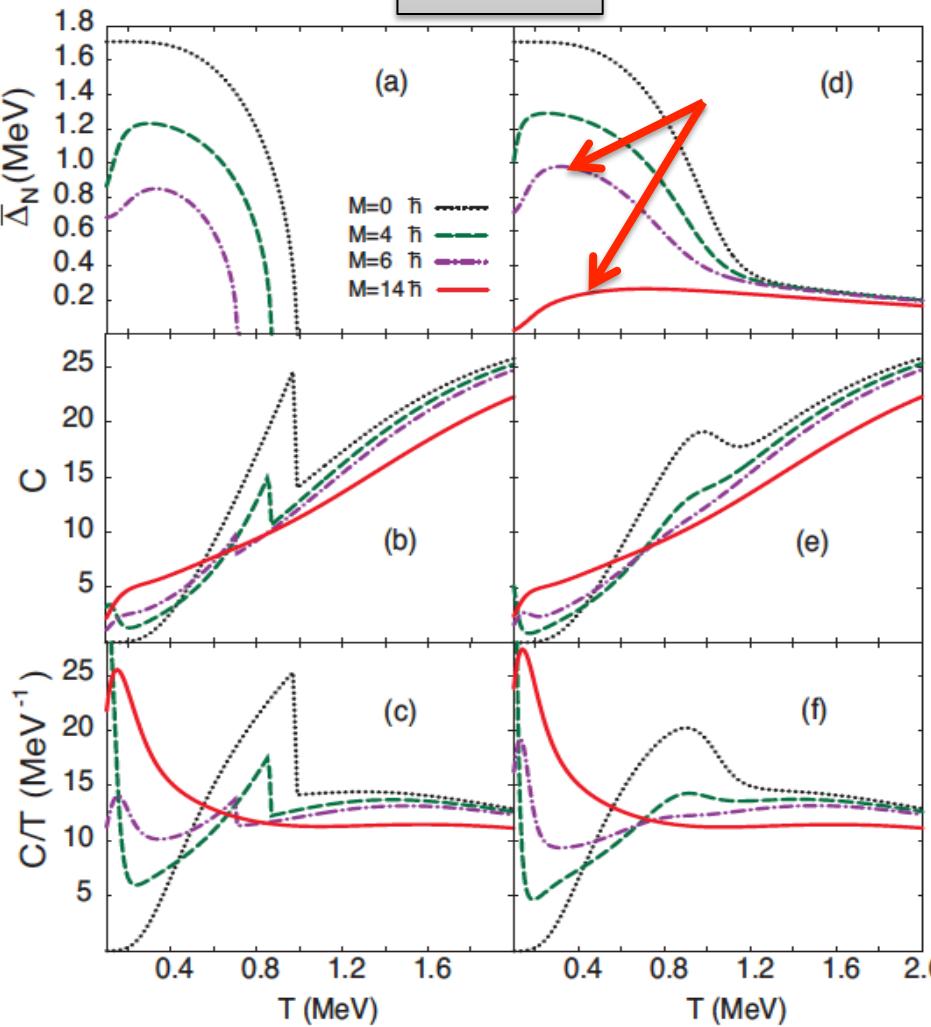
Hot Rotating Nuclei

44Ca

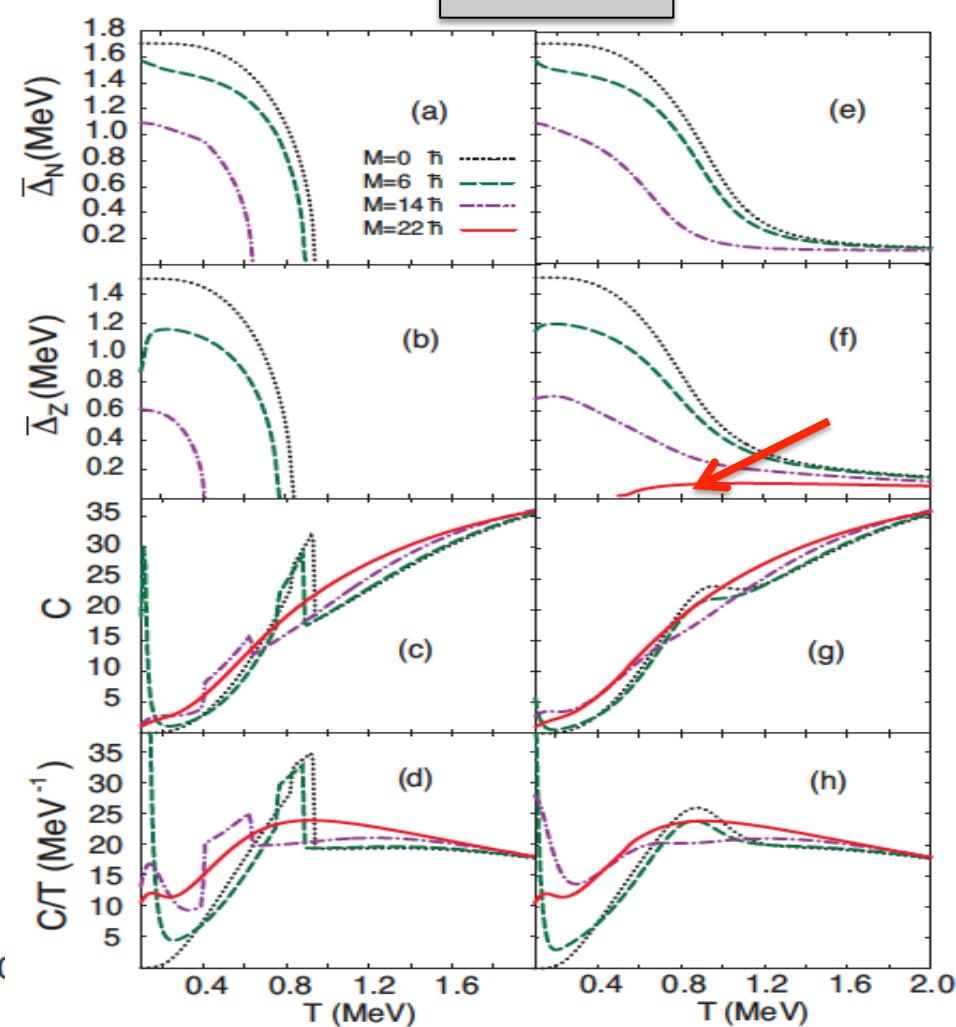


Hot Rotating Nuclei

60Ni



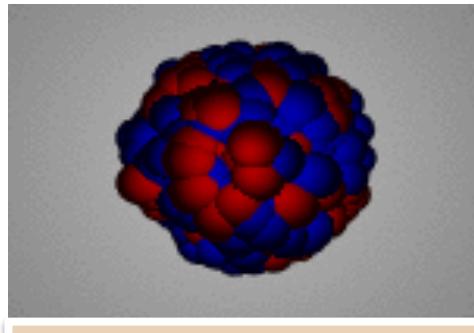
72Ge



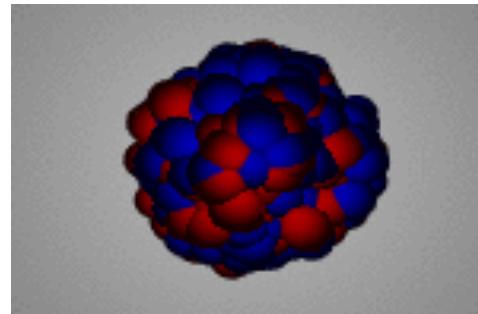
Research Topics

□ Past Research Topics:

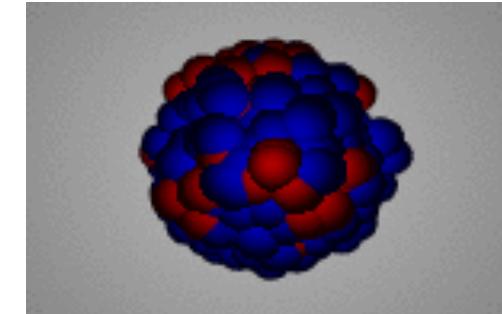
- ✧ *Pairing Properties in Hot Rotating Nuclei*
- ✧ *Nuclear Giant/Pigmy Dipole Resonances*



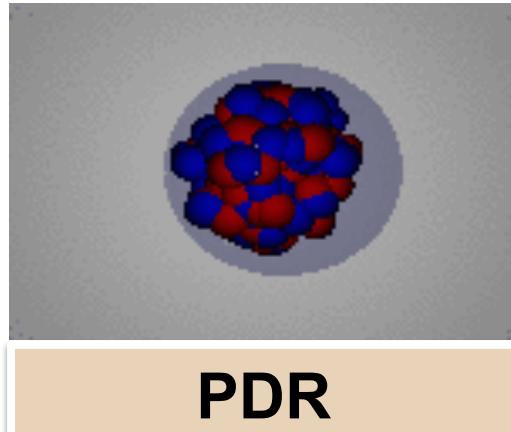
GMR



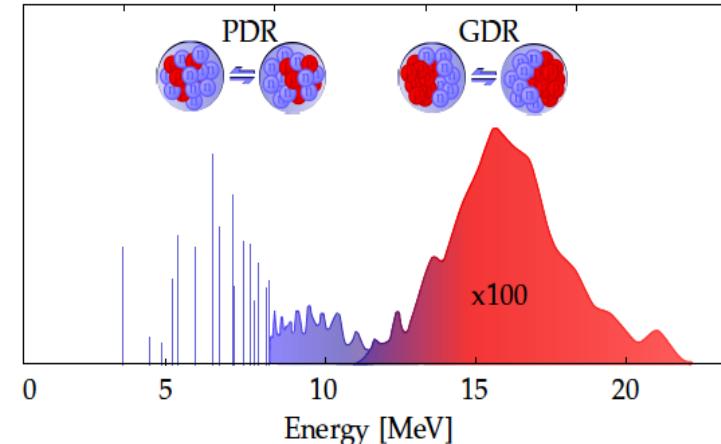
GDR



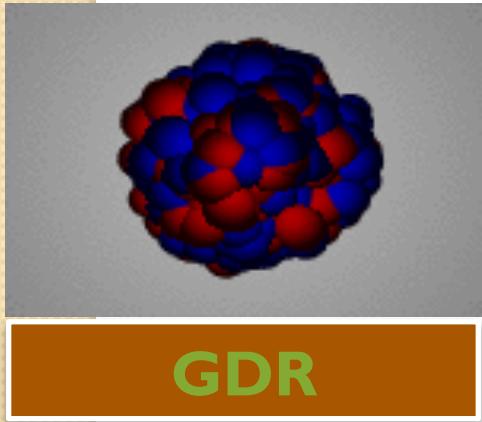
GQR



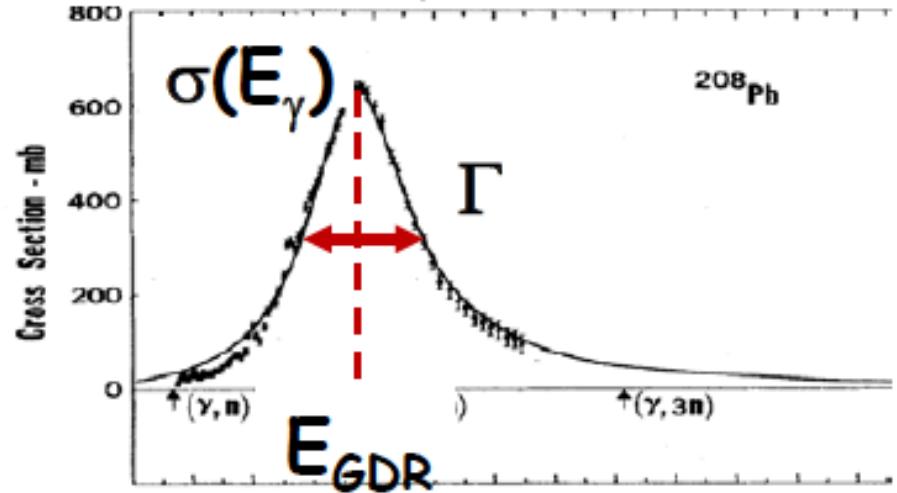
PDR



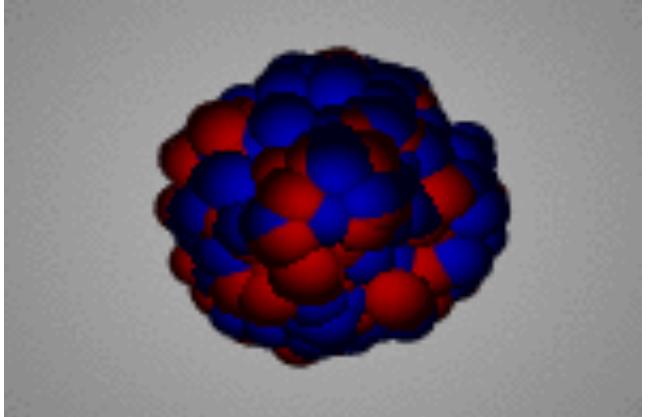
GDR



described with Lorentzian:

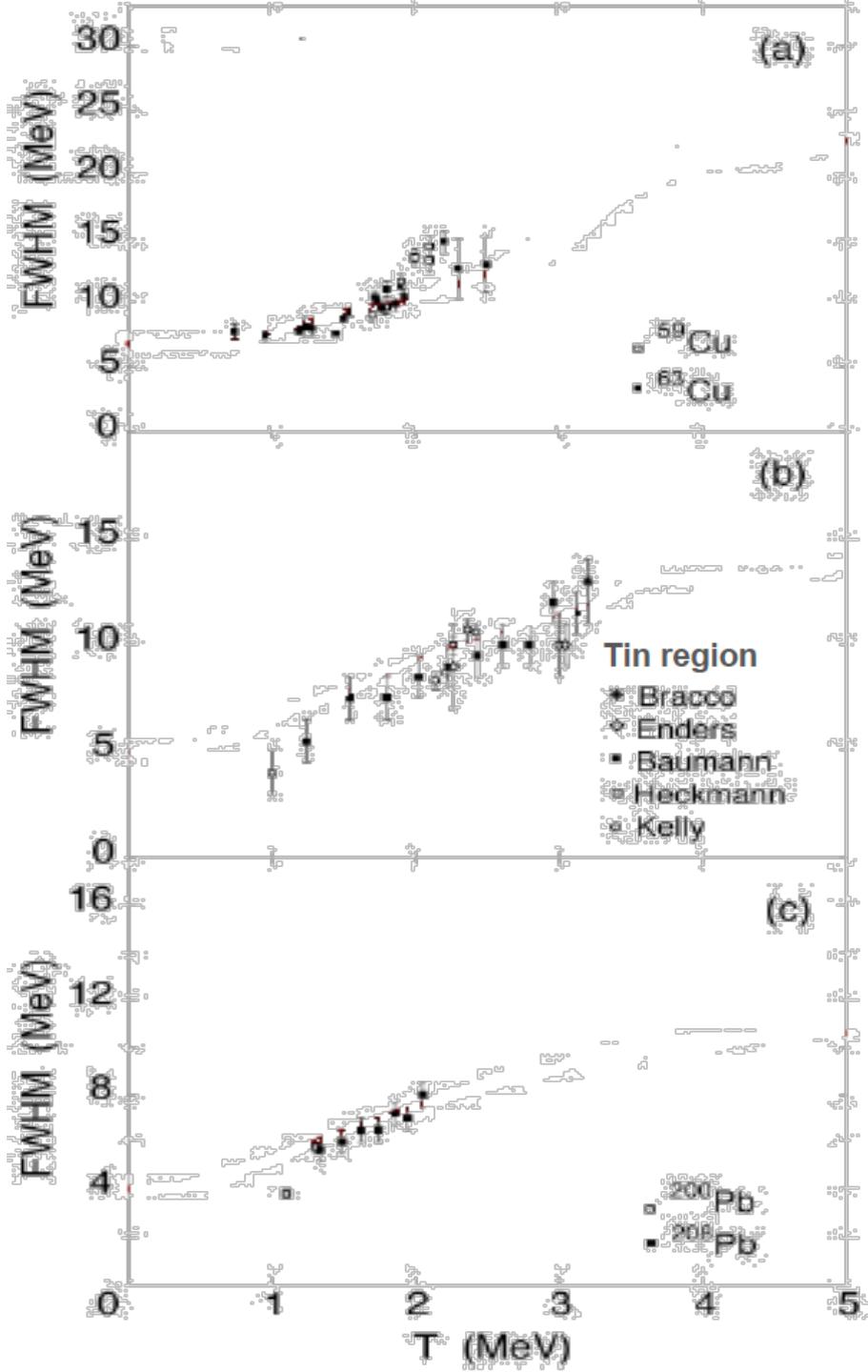


$$\sigma(E_\gamma) = \frac{\sigma_0 \Gamma_{GDR}^2 E_\gamma^2}{(E_\gamma^2 - E_{GDR}^2)^2 + \Gamma_{GDR}^2 E_\gamma^2}$$



GDR in Hot Nuclei

- Saturation of GDR width at high T ?
- Slight increase of GDR width at low T ?



Phonon Damping Model (PDM)

$$H = \sum_s E_s a_s^\dagger a_s + \sum_q \omega_q Q_q^\dagger Q_q + \sum_{ss'} F_{ss'}^{(q)} a_s^\dagger a_{s'} (Q_q^\dagger + Q_q)$$



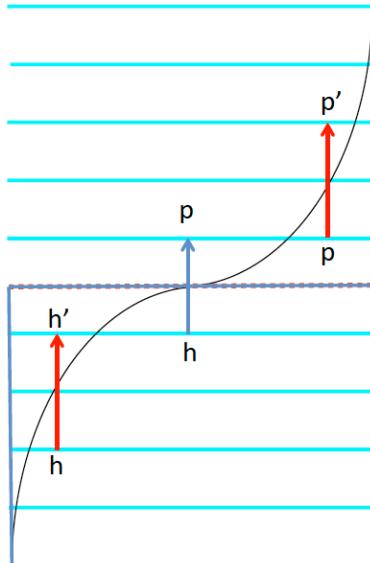
Topical conference on giant resonances, Varenna, May 1998

*N. Dinh Dang and A. Arima,
Phys. Rev. Lett. 80, 4145 (1998)*

$$G_q(E) = \frac{1}{2\pi} [E - \omega_q - P_q(E)]^{-1}$$

$$P_q(E) = \sum_{ss'} F_s^{(q)} F_{s'}^{(q)} \frac{f_s - f_{s'}}{E - E_{s'} + E_s},$$

$$\gamma_q(\omega) = \Im m P_q(\omega \pm i\varepsilon).$$



Quantal: $ss' = ph$

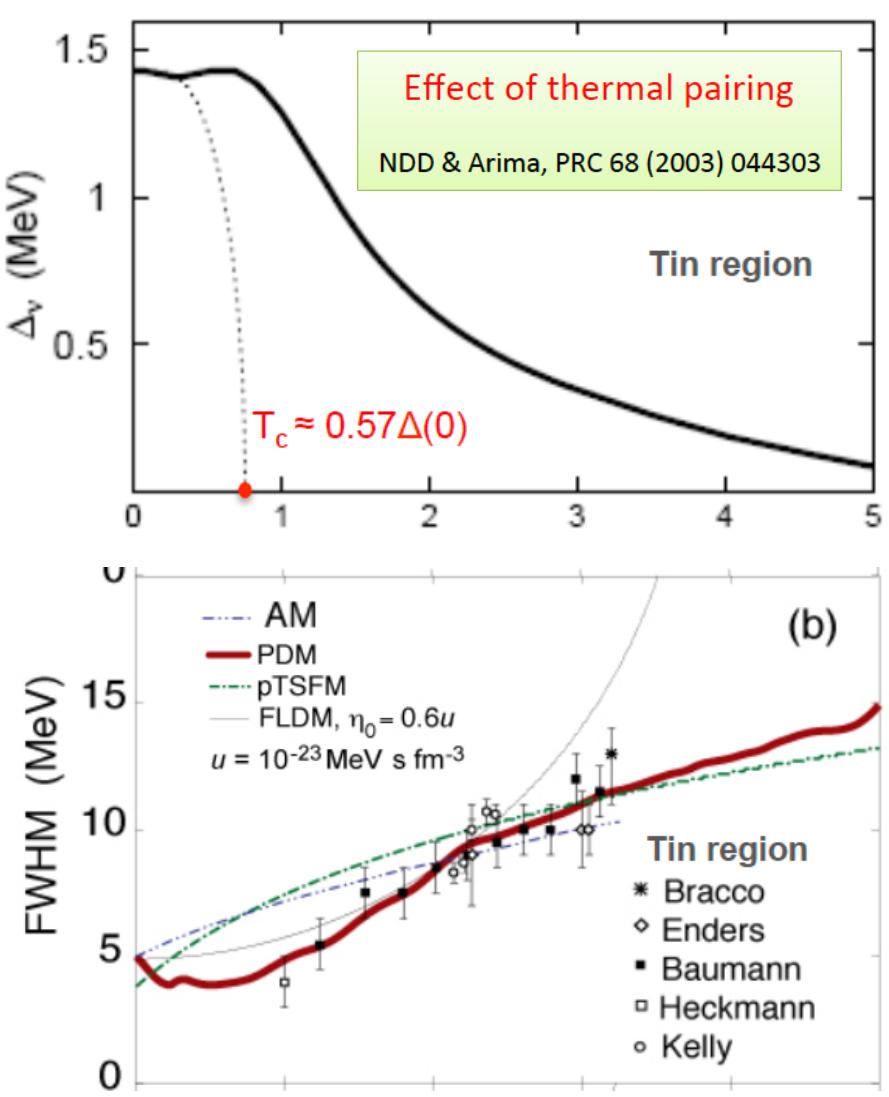
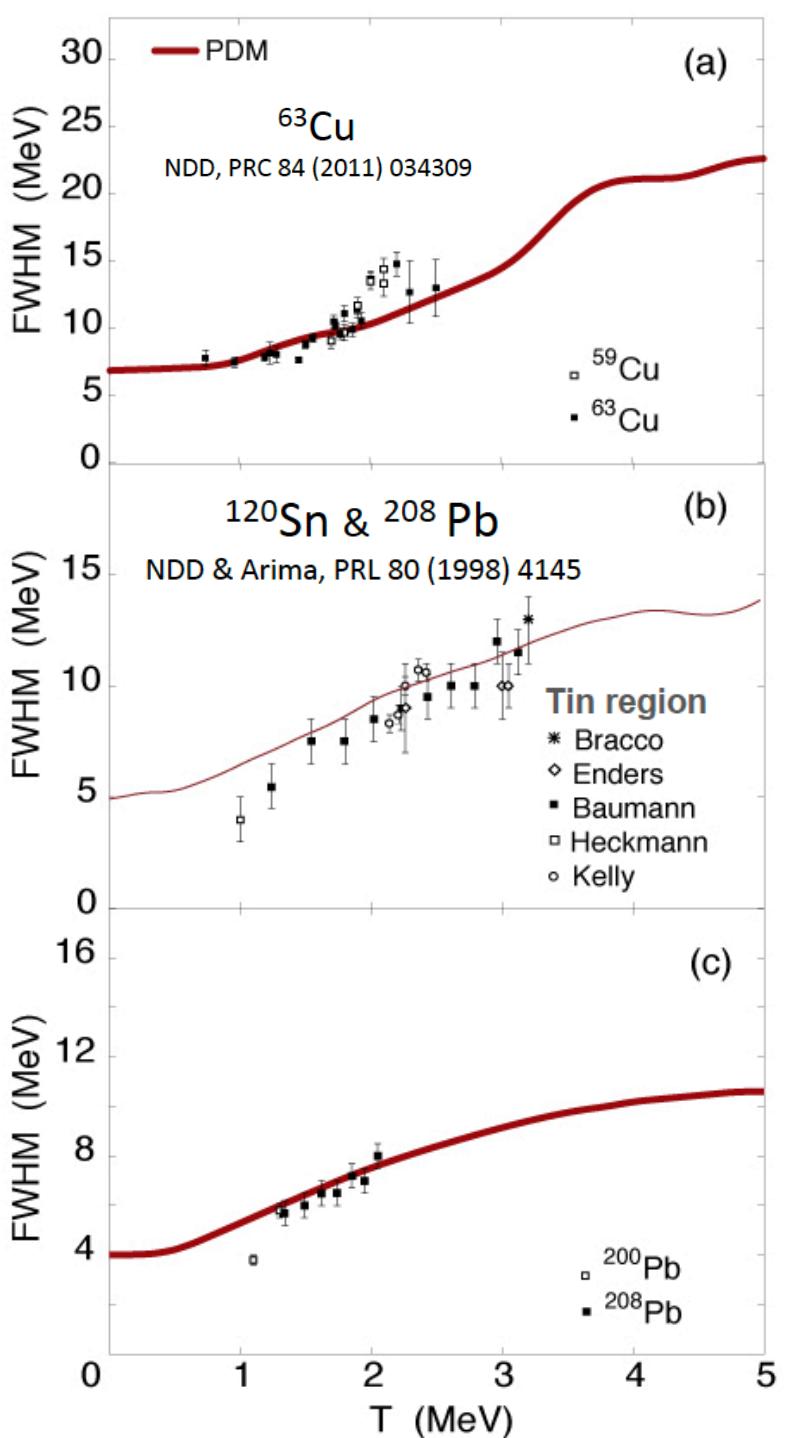
Thermal: $ss' = pp'$, $hh' = hh'$

$$\Gamma = \Gamma_Q + \Gamma_T = 2\gamma_q(E_{GDR})$$

$$E_{GDR} - \omega_q - P_q(E_{GDR}) = 0, \quad f_s = \left\{ \exp[(\varepsilon_s - \lambda)/T] + 1 \right\}^{-1}$$

GDR strength function:

$$S_q(\omega) = \frac{1}{\pi} \frac{\gamma_q(\omega)}{[\omega - E_{GDR}]^2 + \gamma_q^2(\omega)}.$$



FLDM: Fermi-liquid-drop model

V. M. Kolomietz and S. Shlomo, Phys. Rep. 390, 133 (2004)

pTSFM: Phenomenological thermal shape fluctuation model

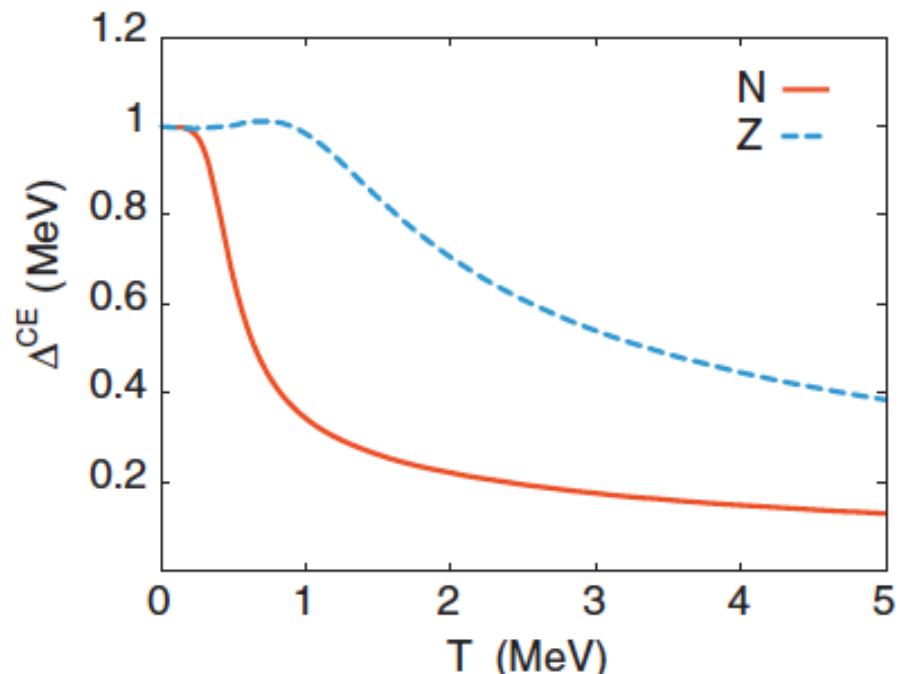
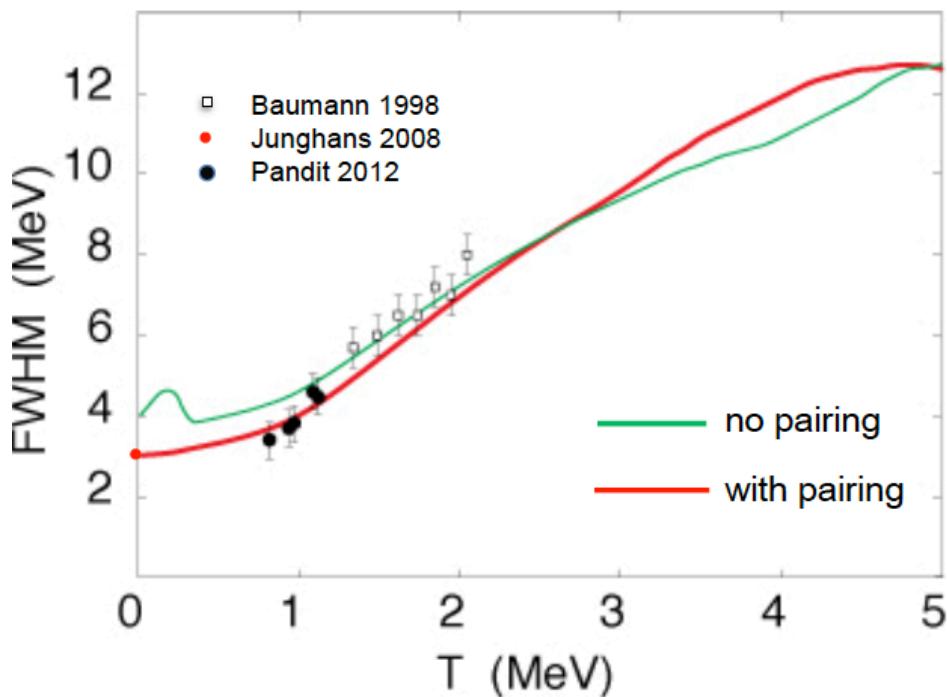
D. Kusnezov, Y. Alhassid, and K. A. Snover, Phys. Rev. Lett. 81, 532 (1998)

GDR: PDM + Exact Pairing at T \neq 0

201Tl

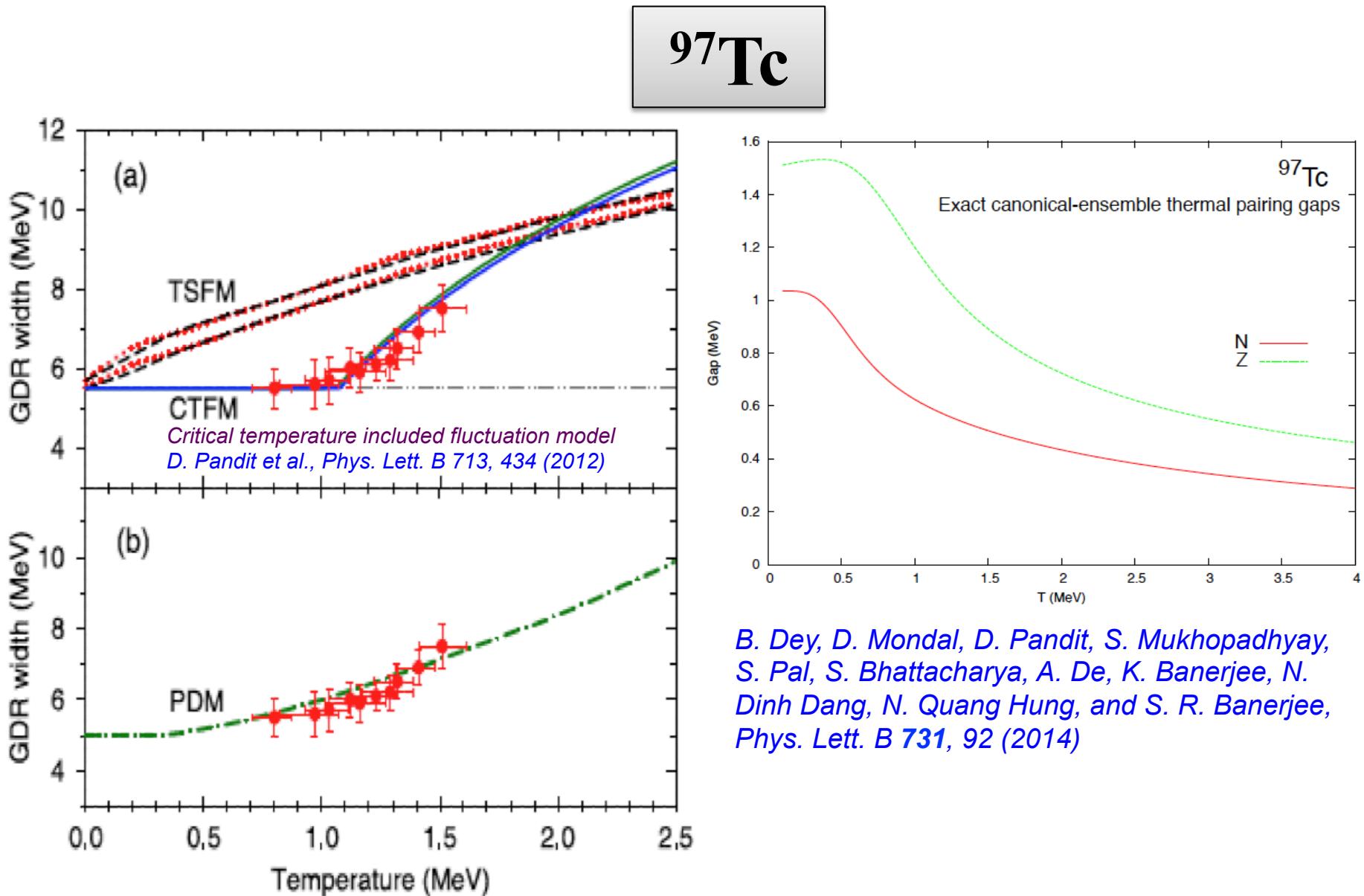
New data at low T

D. Pandit et al., Phys. Lett. B 713, 434 (2012)

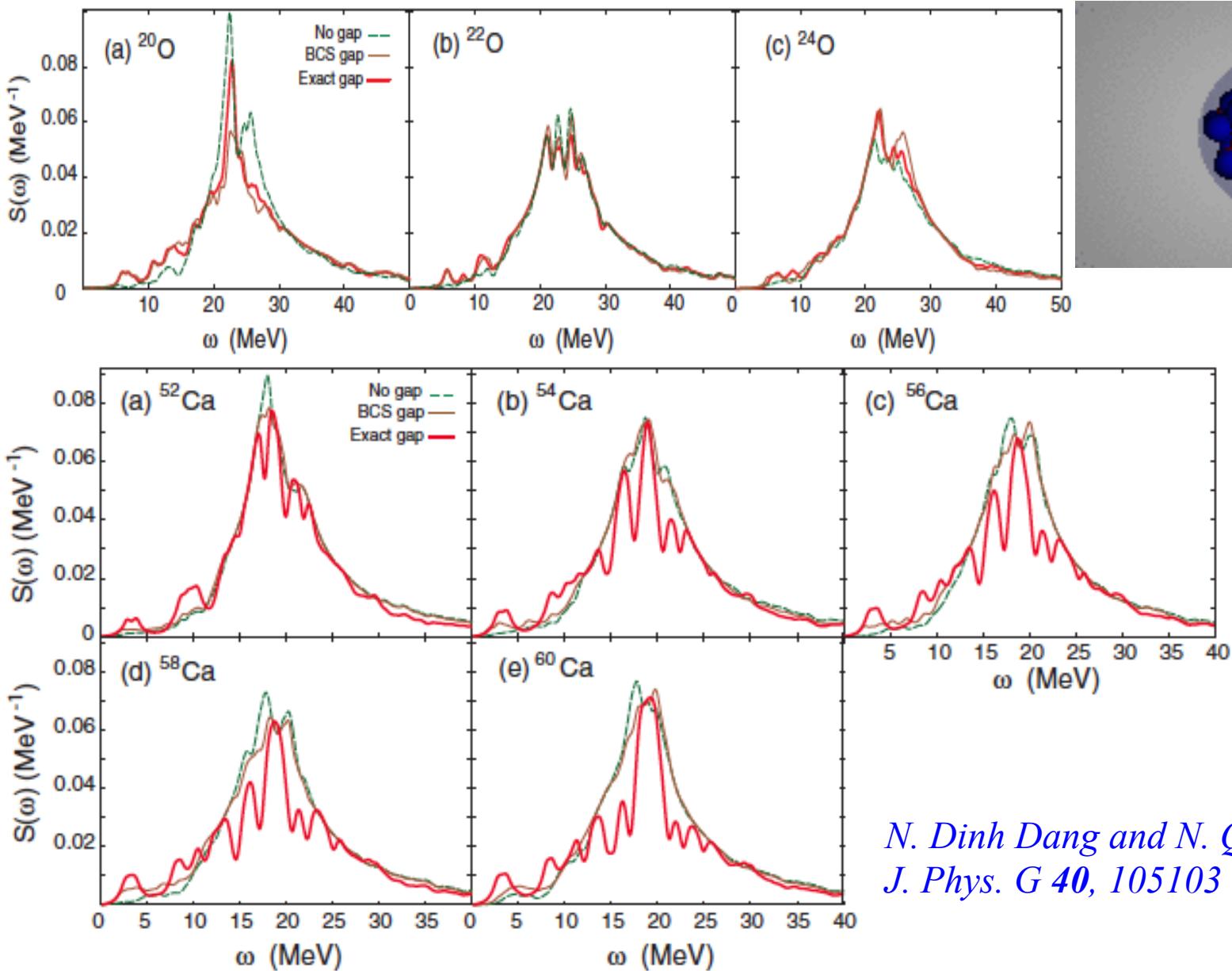


N. Dinh Dang and N. Quang Hung, Phys. Rev. C 86, 044333 (2012)

GDR: PDM + Exact Pairing at $T \neq 0$

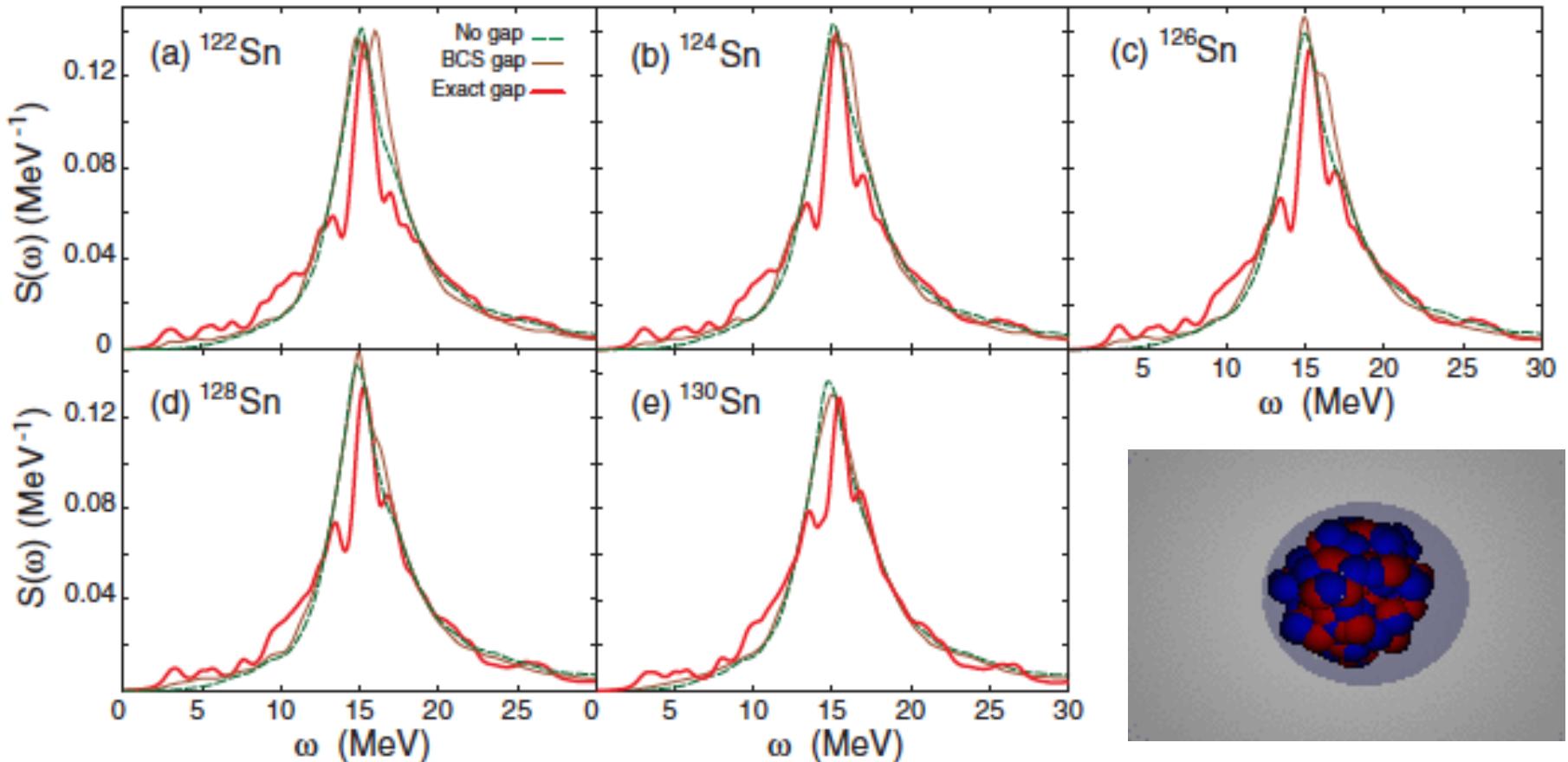


PDR: PDM + Exact Pairing at T=0



*N. Dinh Dang and N. Quang Hung,
J. Phys. G 40, 105103 (2013)*

PDR: PDM + Exact Pairing at T=0



N. Dinh Dang and N. Quang Hung, J. Phys. G 40 (2013) 105103

Research Topics

□ Past Research Topics:

- ✧ *Pairing Properties in Hot Rotating Nuclei*
- ✧ *Nuclear Giant/Pigmy Dipole Resonances*
- ✧ *Viscosity in Hot Rotating Nuclei*

$$\frac{\eta}{s} = \frac{\hbar}{4\pi k_B}, \quad s = \frac{\rho}{A} S$$

KSS conjecture: Universal lower bound for all fluids

η/s in Finite Nucleus

“Nuclear giant resonances can be described as vibrations of proton and neutron fluids. The isoscalar vibrations consist of proton and neutron fluids collectively vibrating in phase, while the isovector ones are described as vibrations of the proton liquid out of phase, with the neutron fluid”.

N. Auerbach & S. Shlomo, *PRL* 103 (2009) 172501



N. Auerbach

Direct calculations using Hydrodynamical (Fermi Liquid-Drop) Model:

$\eta/s = (4 - 19)$ KSS for heavy, $(2.5 - 12.5)$ KSS for light nuclei



S. Shlomo

Shortcomings:

- 1) The GDR width does not agree with experimental systematic at high T
- 2) The entropy $S = 2aT$ with constant level density parameter a
- 3) Large uncertainties.

η/s in Hot Nuclei

PHYSICAL REVIEW C 84, 034309 (2011)

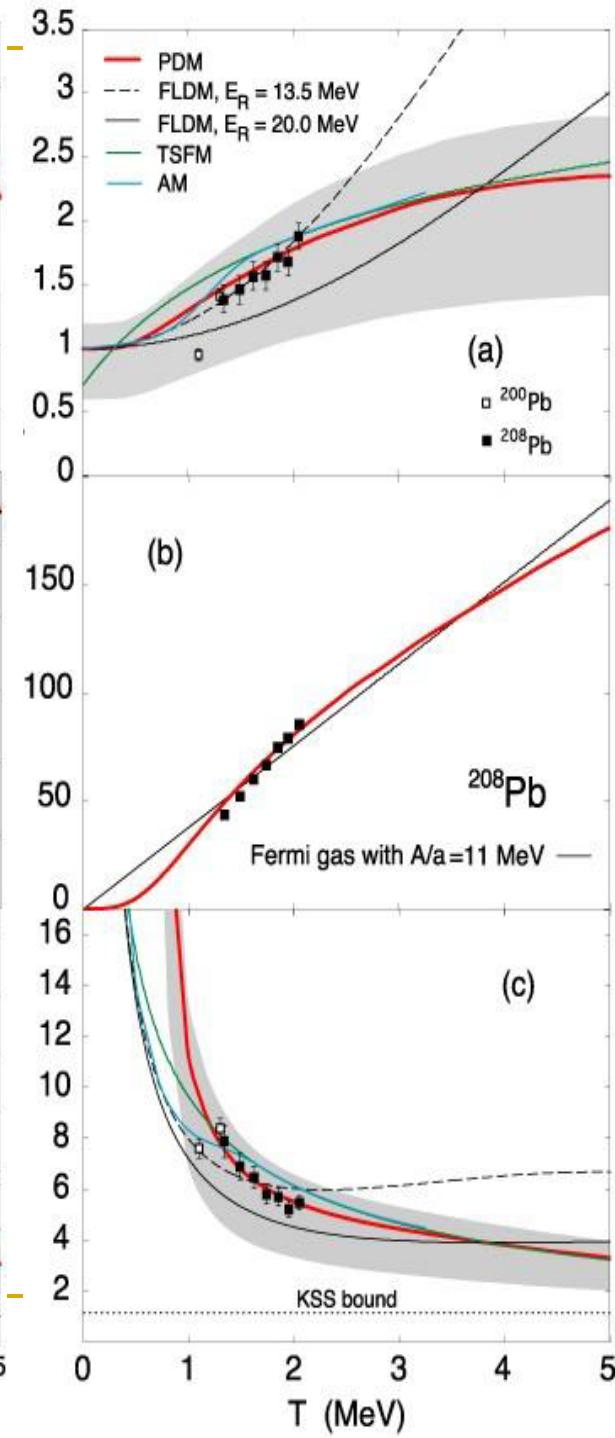
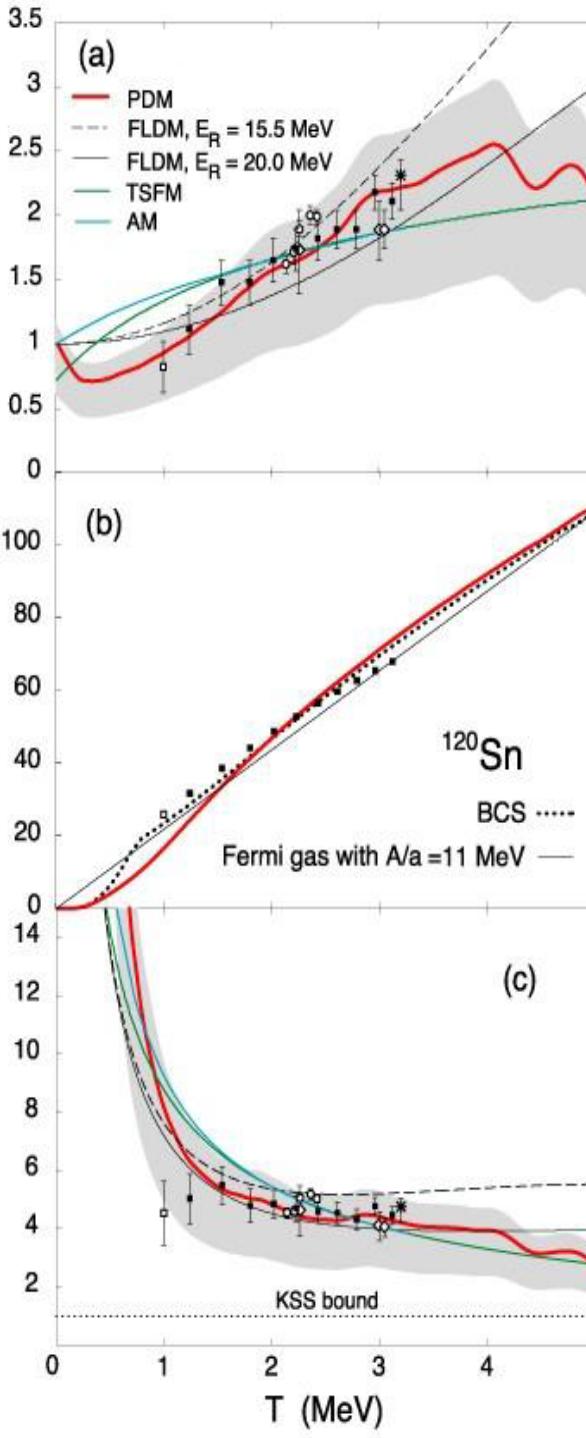
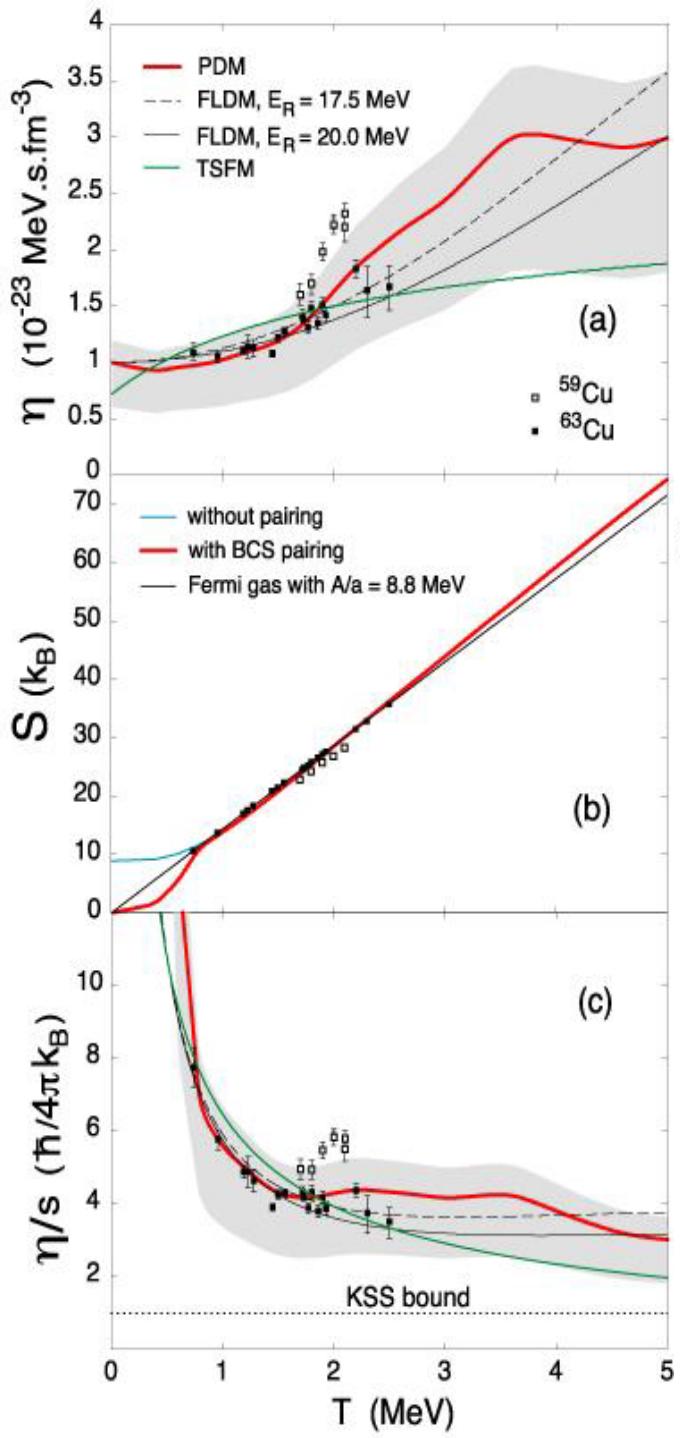
Shear-viscosity to entropy-density ratio from giant dipole resonances in hot nuclei

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(Received 20 December 2010; revised manuscript received 17 June 2011; published 7 September 2011)

The Green-Kubo relation and fluctuation-dissipation theorem are employed to calculate the shear viscosity η of a finite hot nucleus directly from the width and energy of the giant dipole resonance (GDR) of this nucleus. The ratio η/s of shear viscosity η to entropy density s is extracted from the experimental systematics of the GDR in copper, tin, and lead isotopes at finite temperature T . These empirical results are then compared with the predictions by several independent models as well as with almost model-independent estimations. Based on these results, it is concluded that the ratio η/s in medium and heavy nuclei decreases with increasing temperature T to reach $(1.3\text{--}4) \times \hbar/(4\pi k_B)$ at $T = 5$ MeV.

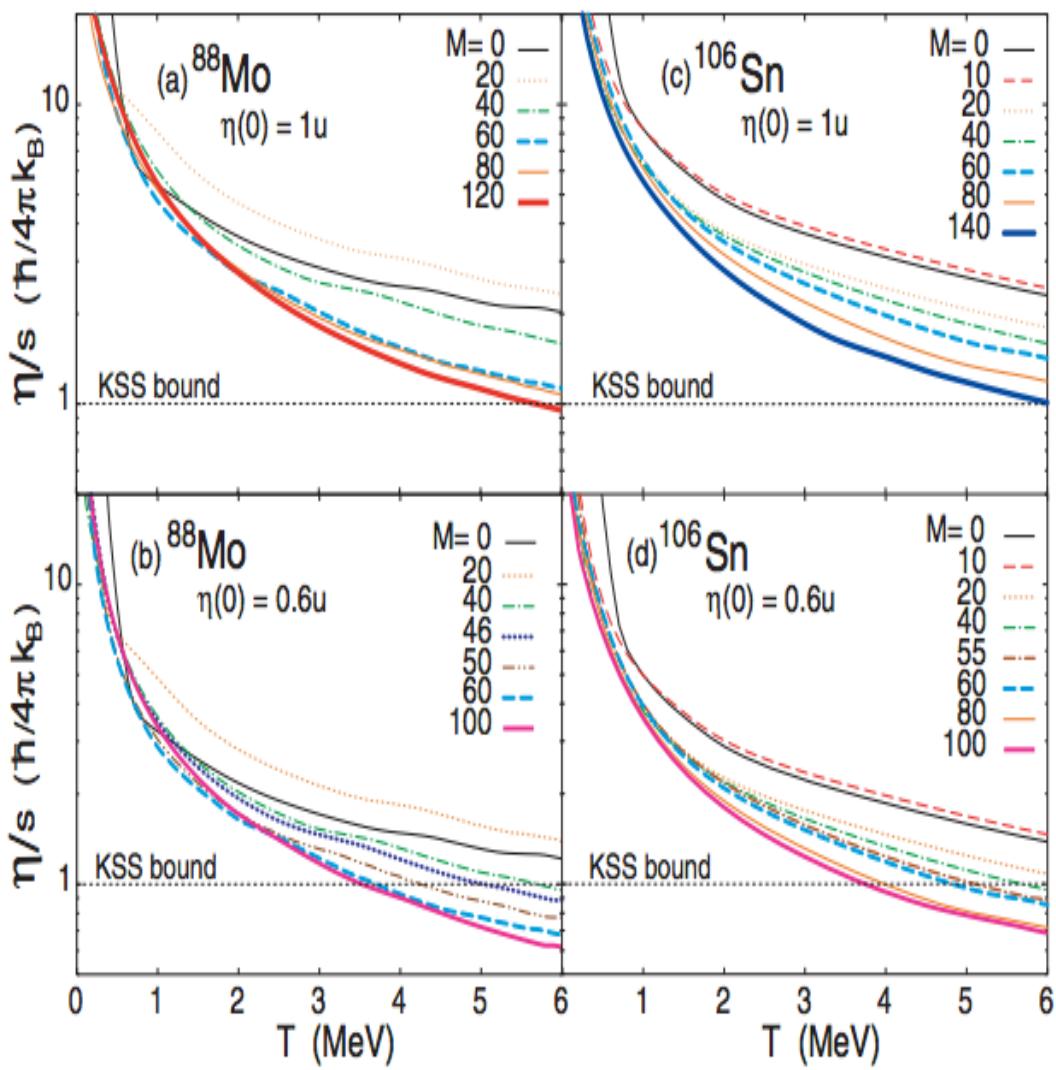


η/s in Hot Nuclei

- 1) The shear viscosity η increases with T up to $T \sim 3 - 3.5$ MeV, and saturates at higher T ; η ($T = 5$ MeV) $\sim (1.3 - 3.5)$ u ($u = 10^{-23}$ MeV s fm $^{-3}$).
- 2) η/s decreases with increasing T , to reach ($1.3 \sim 4.0$) KSS at $T = 5$ MeV. These values are lower and of less uncertainty than the prediction by the FLDM ($4 \sim 19$ KSS).

Nucleons inside a hot nucleus at $T \sim 5$ MeV has nearly the same viscosity as that of QGP (2 – 3 KSS units) at $T > 175$ MeV.

- The GDR width increases with M at a given value of T for $T \leq 3$ MeV. At higher T, the GDR width approaches a saturation at $M \geq 60\hbar$ for ^{88}Mo and $M \geq 80\hbar$ for ^{106}Sn
- The region of $M \geq 60$ goes beyond the maximum value of M up to which the specific shear viscosity η/s has values not smaller than the KSS lower-bound conjecture for this quantity. This maximum value of M is found to be equal to $46\hbar$ and $55\hbar$ for ^{88}Mo and ^{106}Sn , respectively, if the value $\eta(0) = 0.6u$ ($u=10^{-23}$ MeV s fm $^{-3}$) for the shear viscosity at $T = 0$ is used



N. Dinh Dang, Phys. Rev. C 85, 064323 (2012)

η/s in Hot Rotating Nuclei

PHYSICAL REVIEW C 86, 024302 (2012)

Specific shear viscosity in hot rotating systems of paired fermions

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³*Institute for Nuclear Science and Technique, Hanoi, Vietnam*

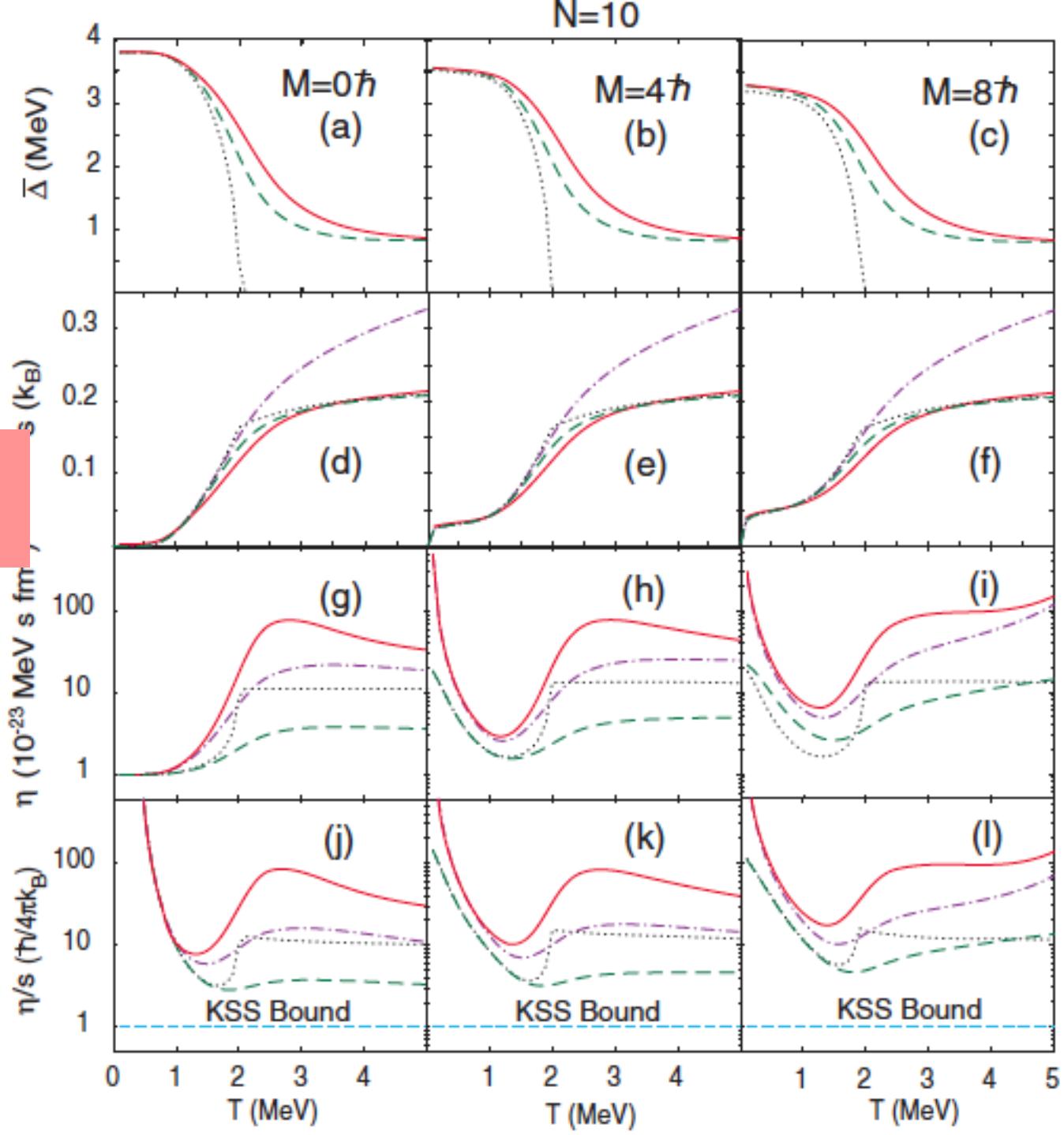
(Received 26 June 2012; revised manuscript received 18 July 2012; published 3 August 2012)

The specific shear viscosity $\bar{\eta}$ of a classically rotating system of nucleons that interact via a monopole pairing force is calculated including the effects of thermal fluctuations and coupling to pair vibrations within the self-consistent quasiparticle random-phase approximation. It is found that $\bar{\eta}$ increases with angular momentum M at a given temperature T . In medium and heavy systems, $\bar{\eta}$ decreases with increasing T at $T \geq 2$ MeV and this feature is not affected much by angular momentum. However, in lighter systems (with the mass number $A \leq 20$), $\bar{\eta}$ increases with T at a value of M close to the maximal value M_{\max} , which is defined as the limiting angular momentum for each system. The values of $\bar{\eta}$ obtained within the schematic model as well as for systems with realistic single-particle energies are always larger than the universal lower-bound conjecture $\hbar/(4\pi k_B)$ up to $T = 5$ MeV.

N=10

Schematic model
N = 10

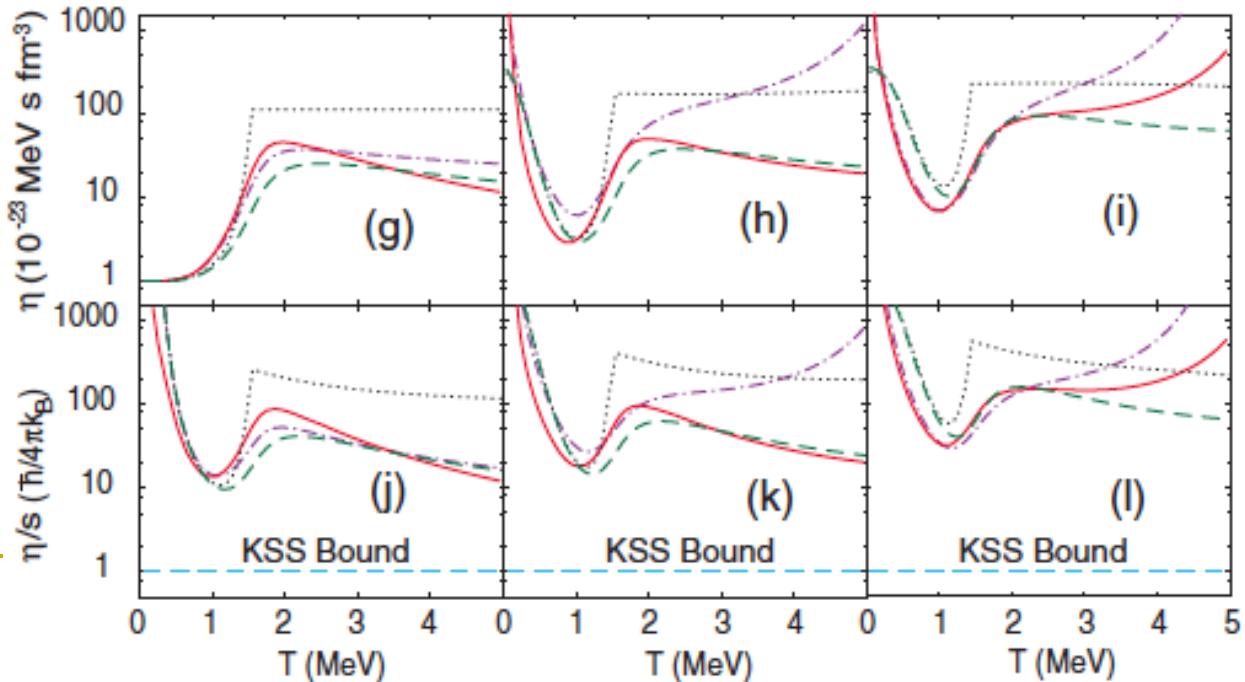
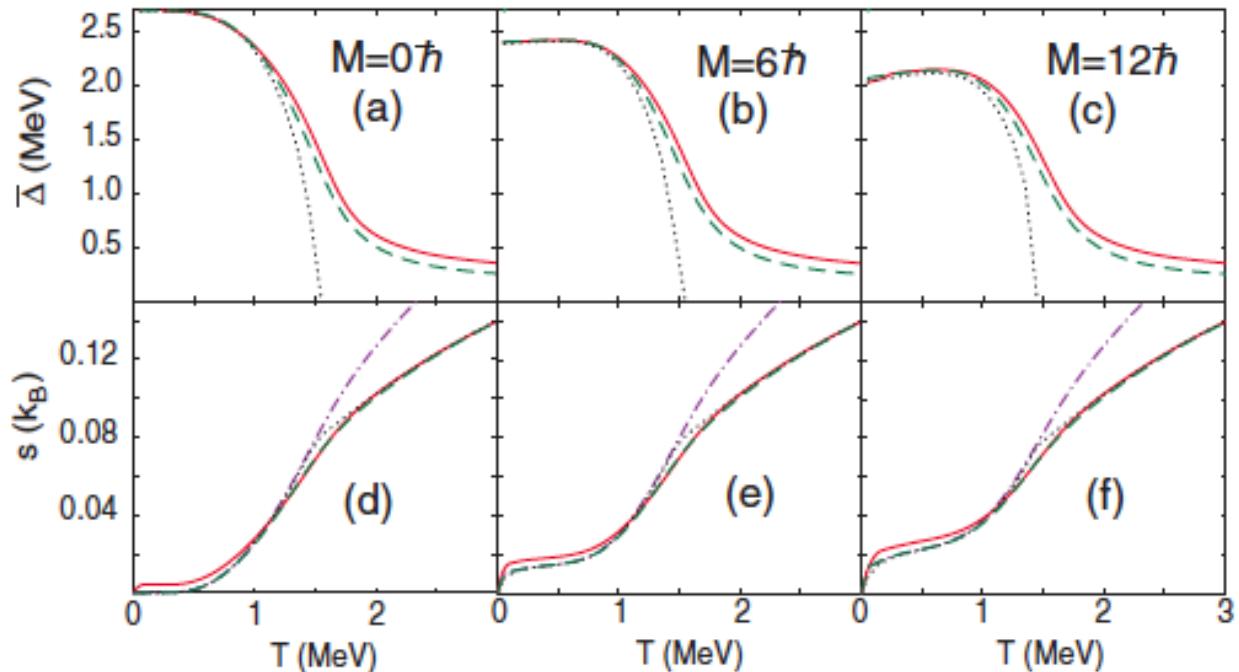
*N. Quang Hung and N.
Dinh Dang, Phys. Rev. C
86, 024302 (2012)*



Schematic model $N = 20$

*N. Quang Hung and N.
Dinh Dang, Phys. Rev. C
86, 024302 (2012)*

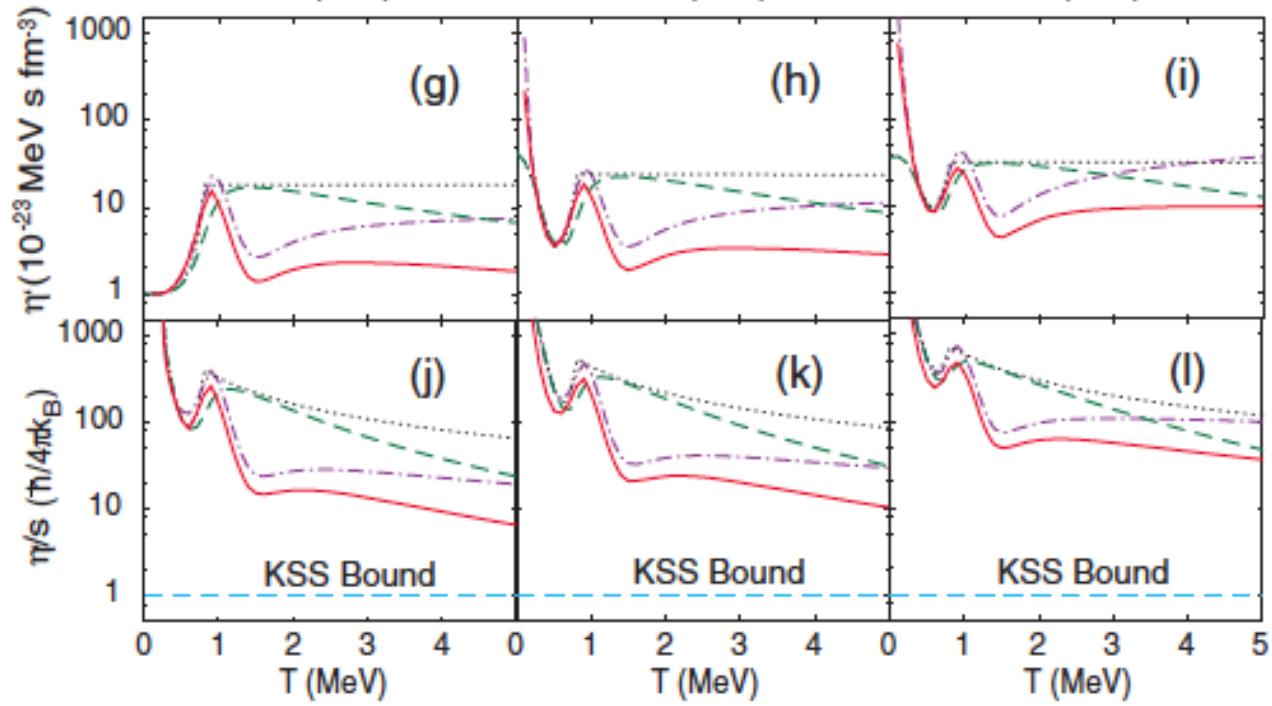
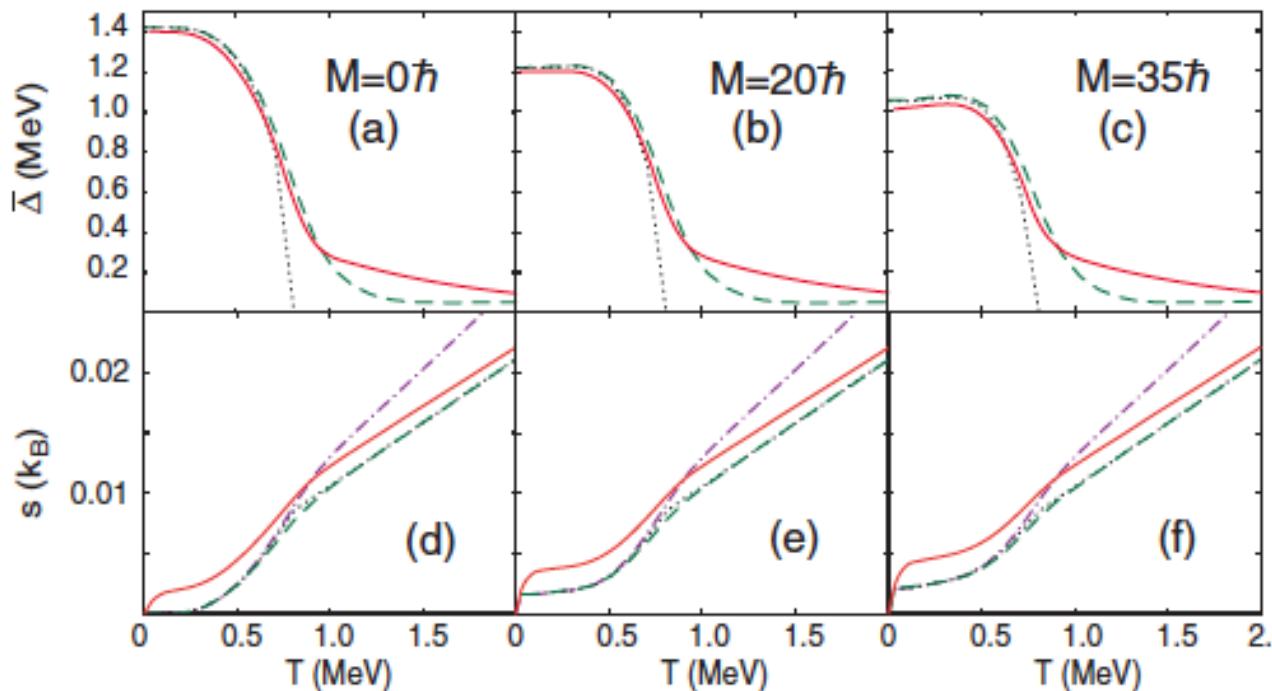
$N=20$



Schematic model $N = 100$

*N. Quang Hung and N.
Dinh Dang, Phys. Rev. C
86, 024302 (2012)*

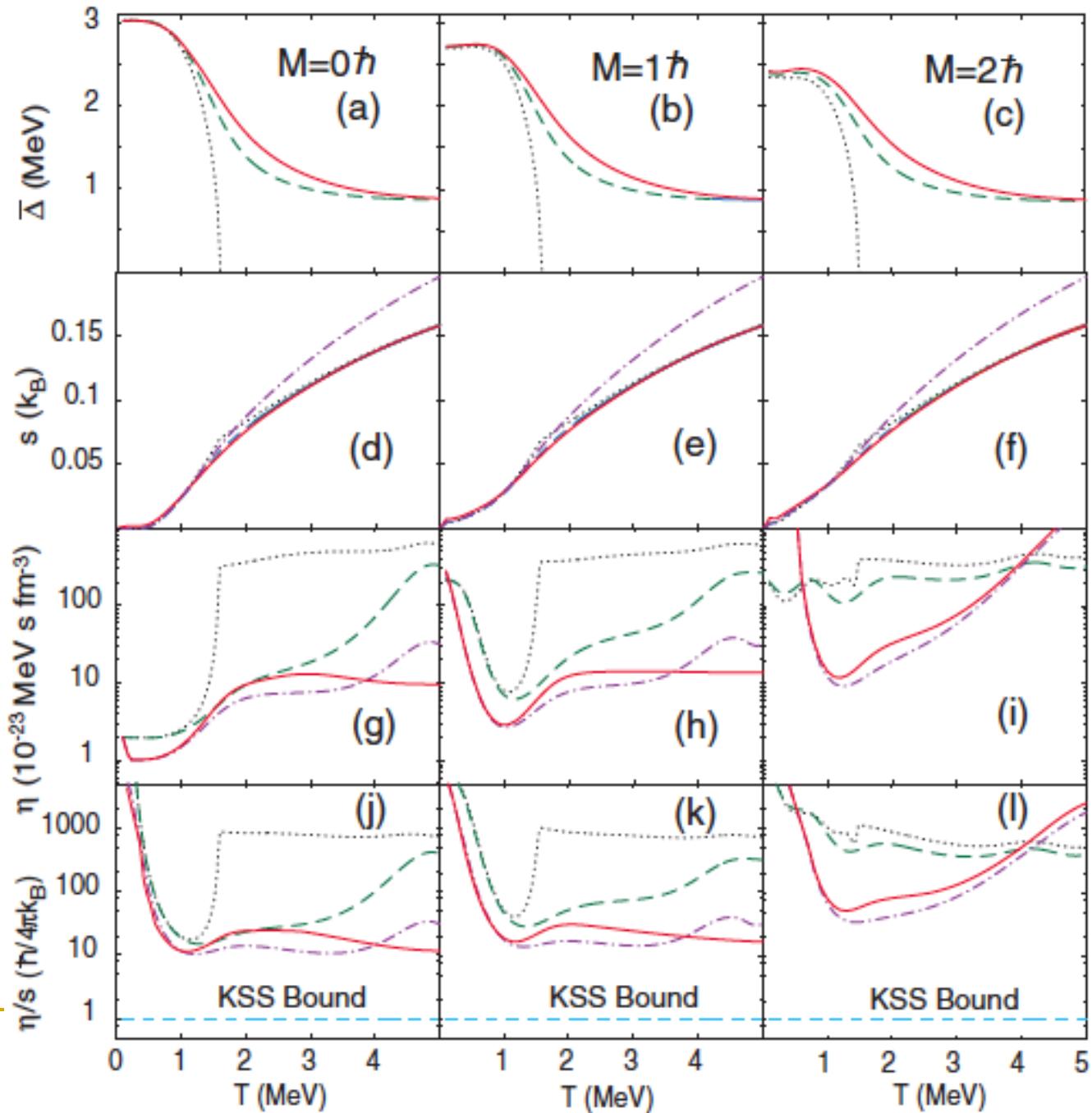
$N=100$



20O

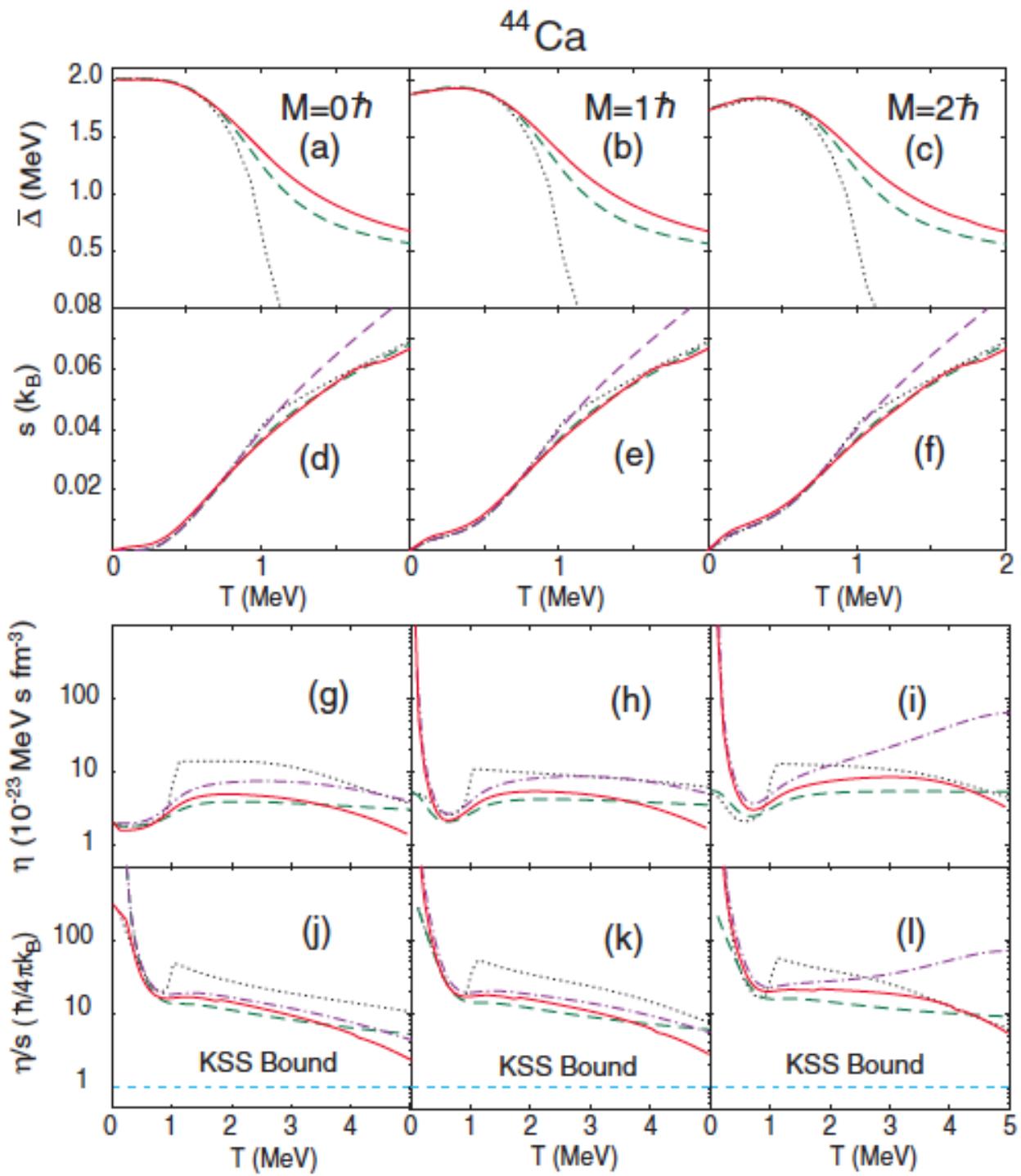
N. Quang Hung and N.
Dinh Dang, Phys. Rev. C
86, 024302 (2012)

²⁰O



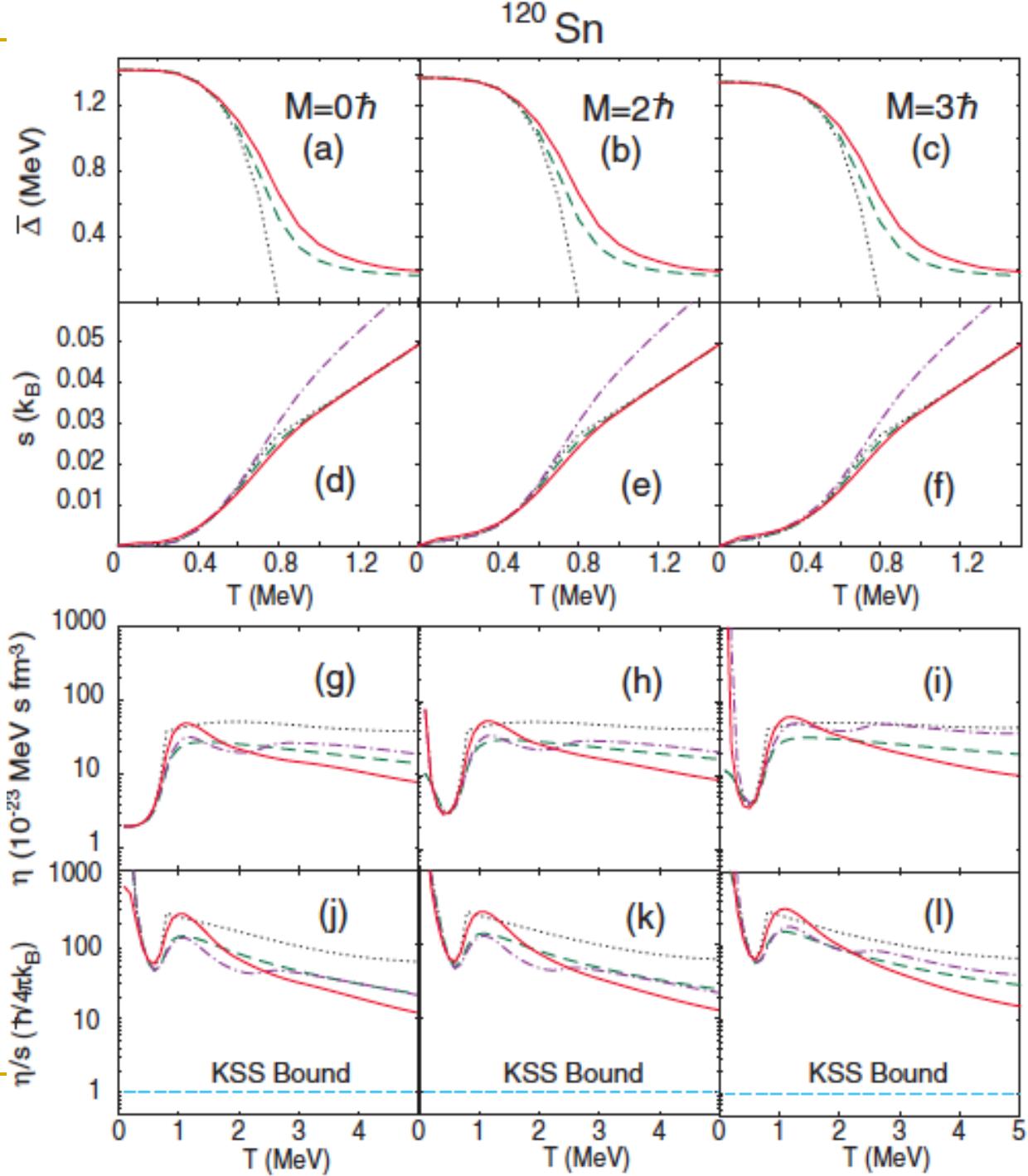
^{44}Ca

N. Quang Hung and N.
Dinh Dang, Phys. Rev. C
86, 024302 (2012)



^{120}Sn

*N. Quang Hung and N.
Dinh Dang, Phys. Rev. C
86, 024302 (2012)*



η/s in Hot Rotating Nuclei

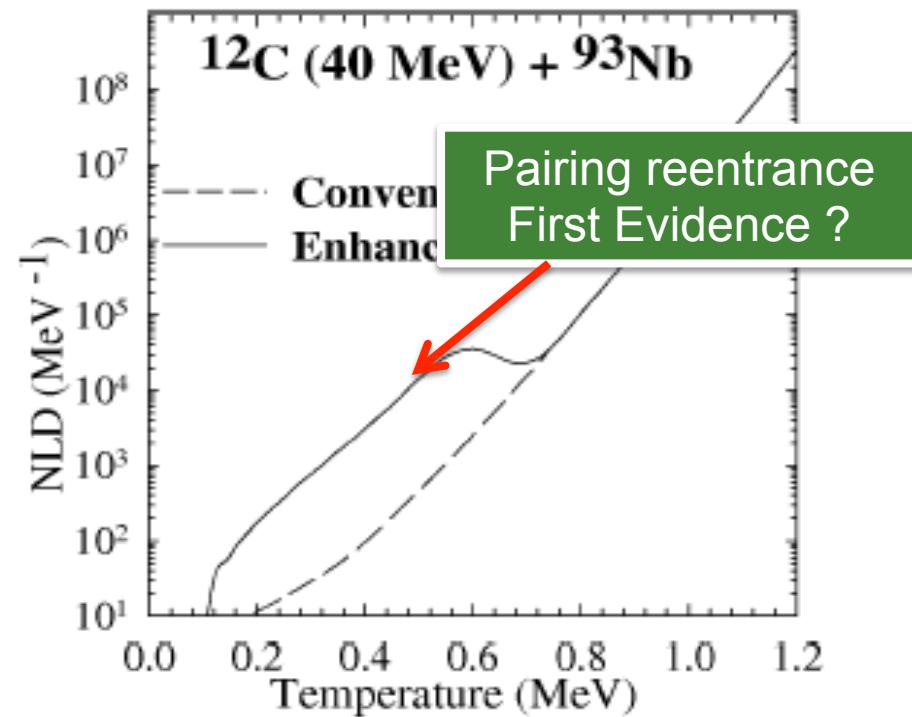
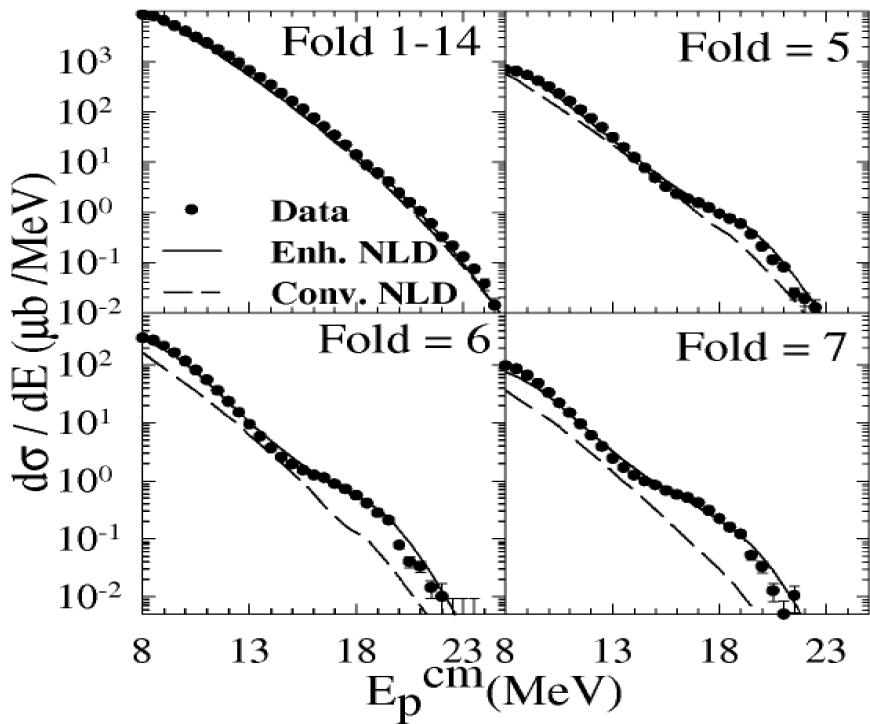
- In medium and heavy systems, η/s decreases with increasing T at $T \geq 2$ MeV and this feature is not affected much by angular momentum, whereas it increases with T in light systems (with mass number $A \leq 20$)
- The values of η/s obtained within the schematic model as well as for systems with realistic single-particle energies are always larger than the universal lower-bound conjecture $\hbar/(4\pi k_B)$ up to $T = 5$ MeV.

Research Topics

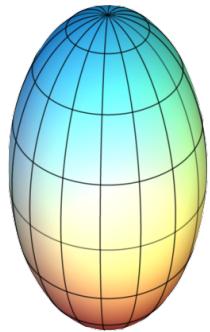
□ Present Research Topics:

❖ *Pairing Reentrance Phenomenon*

$$^{12}\text{C} + ^{93}\text{Nb} \text{ at } E(^{12}\text{C}) = 40 - 45 \text{ MeV}$$

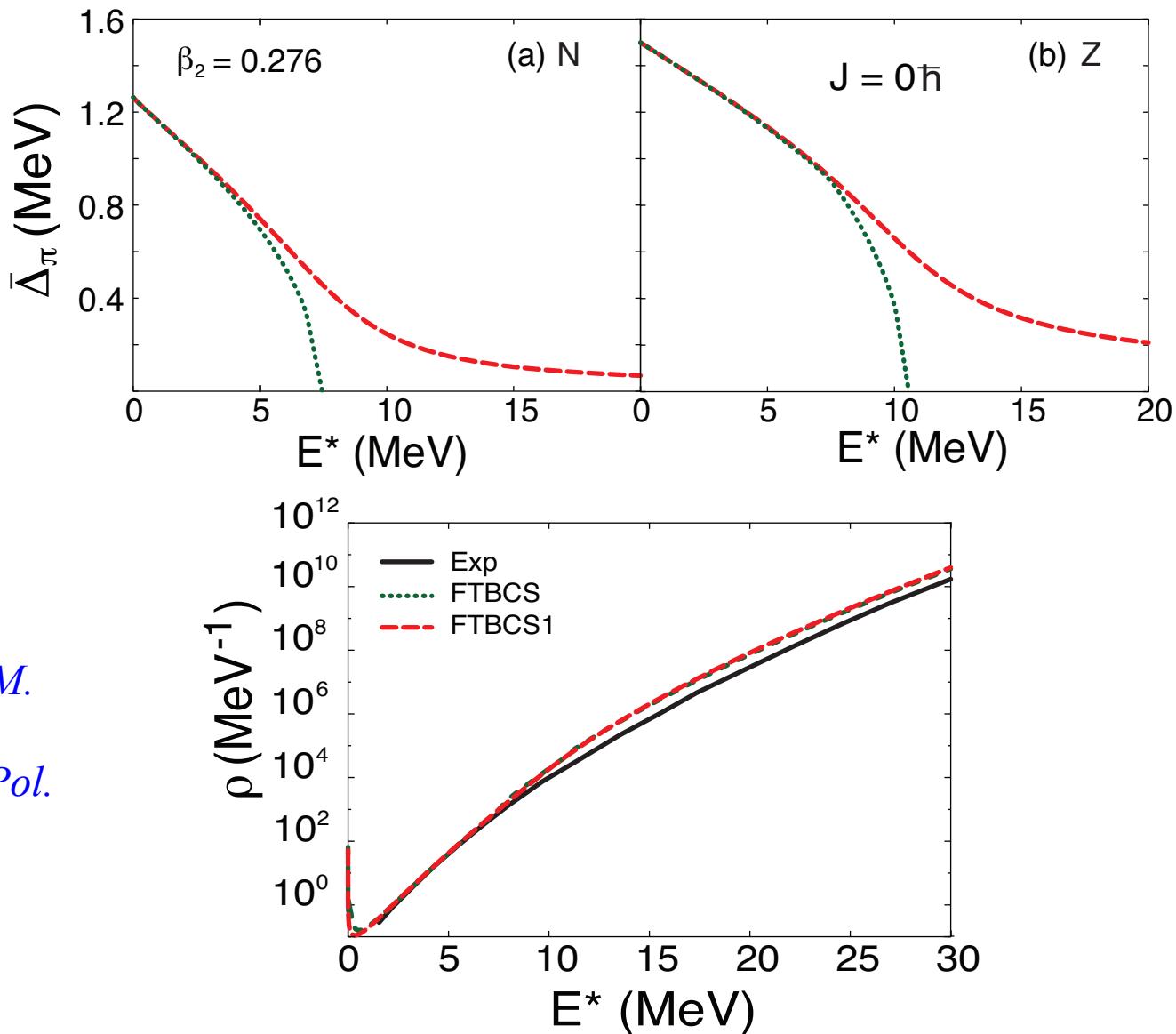


FTBCS1 vs Exp

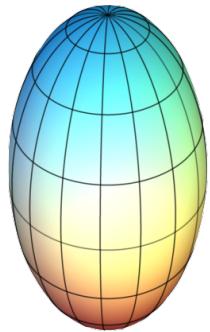


^{104}Pd

*N. Quang Hung, N. Dinh
Dang, B. K. Agrawal, V. M.
Data, A. Mitra, and D. R.
Chakrabarty, Act. Phys. Pol.
B 8, 551 (2015)*

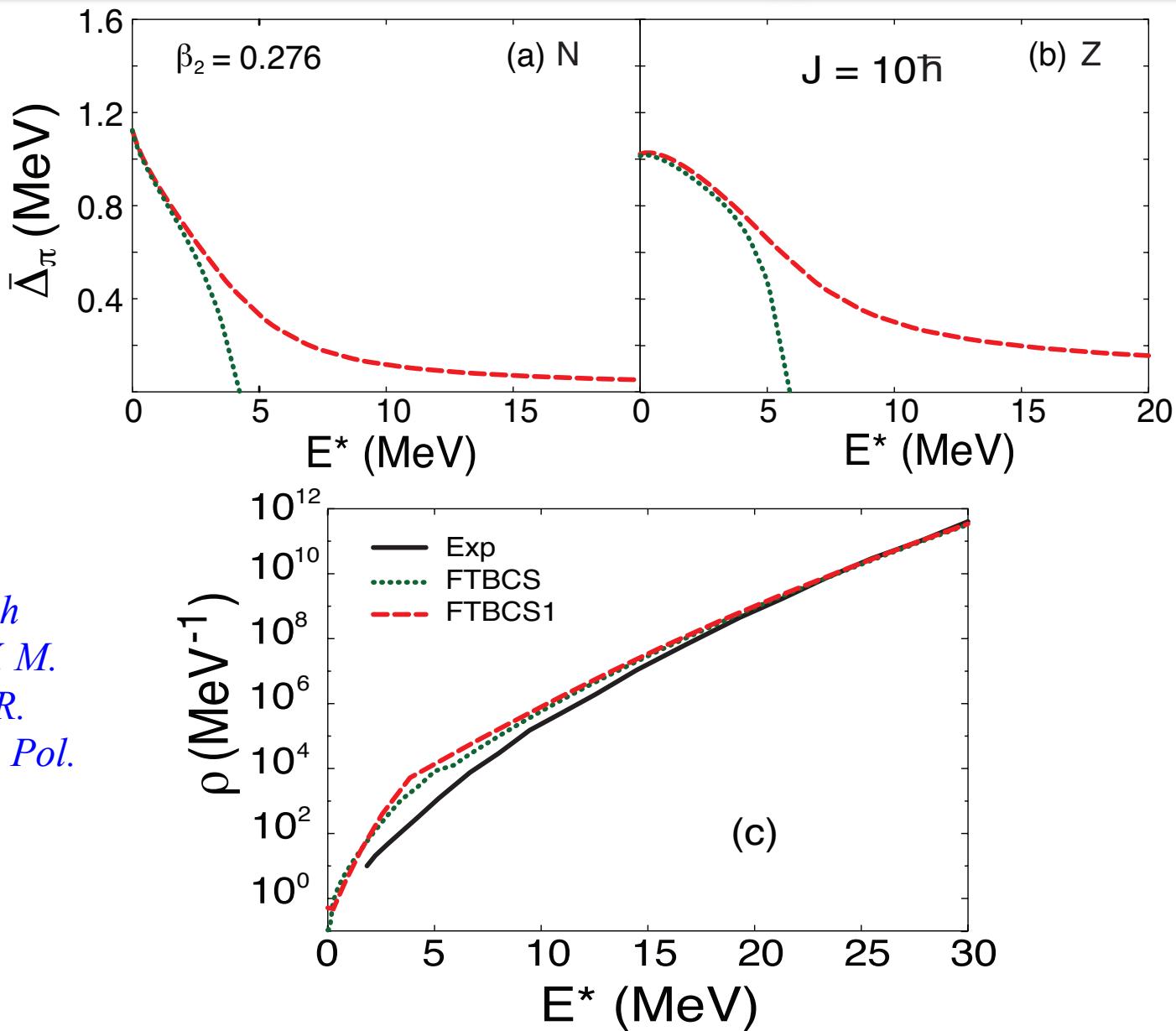


FTBCS1 vs Exp

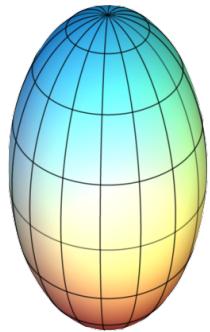


^{104}Pd

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B 8, 551 (2015)*

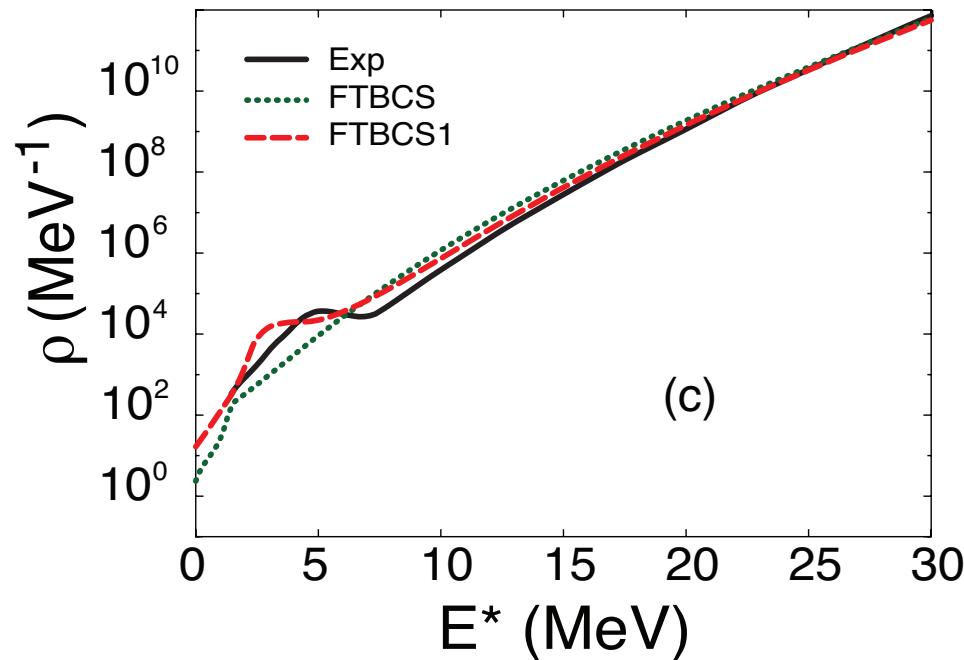
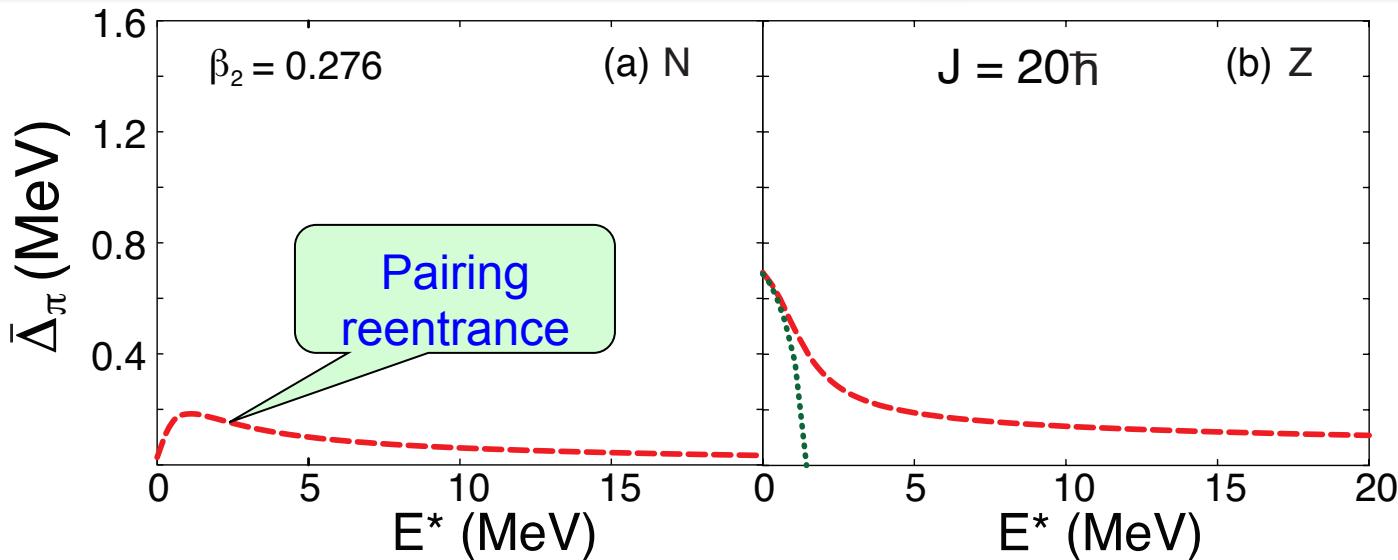


FTBCS1 vs Exp

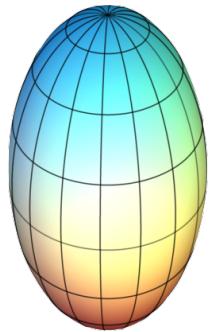


^{104}Pd

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Dang, B. K. Agrawal, V. M.
Data, A. Mitra, and D. R.
Chakrabarty, Act. Phys. Pol.
B 8, 551 (2015)*

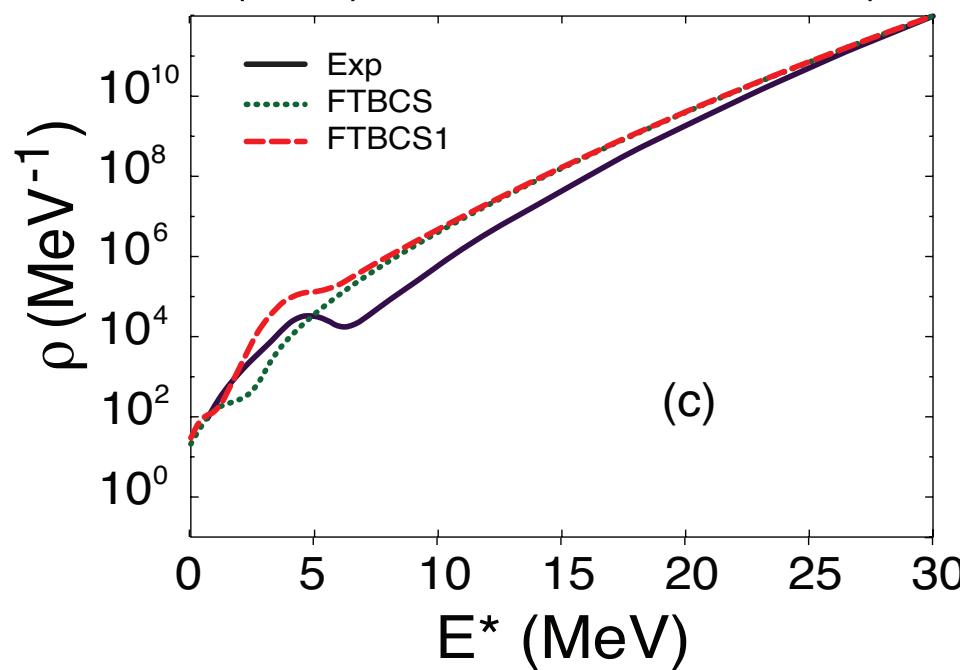
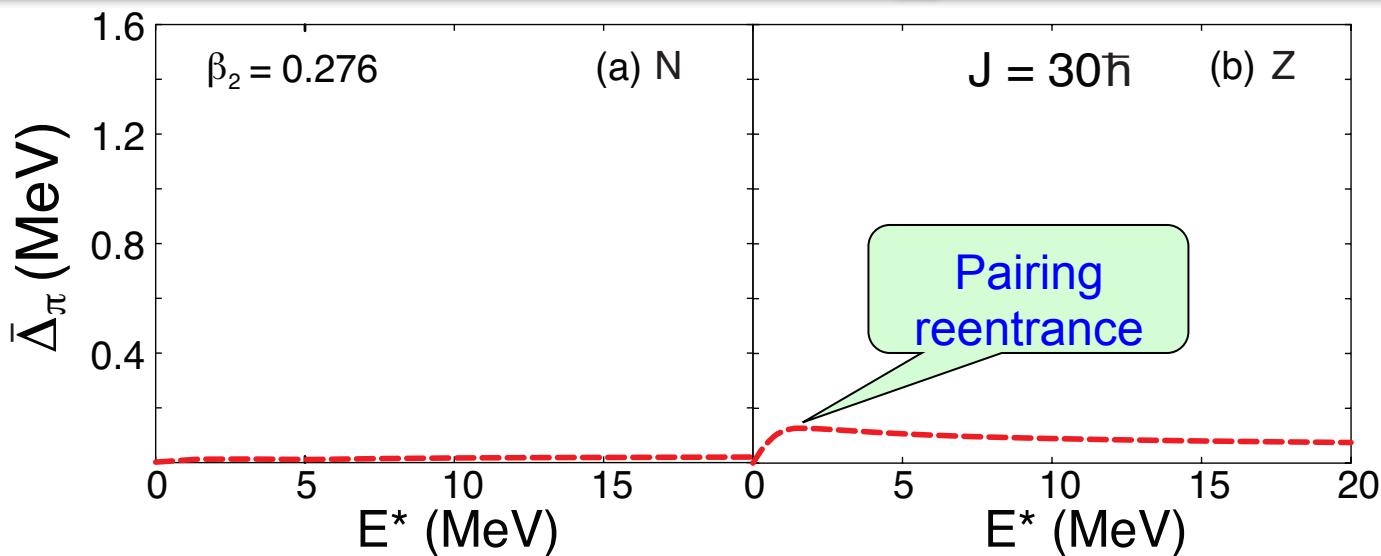


FTBCS1 vs Exp

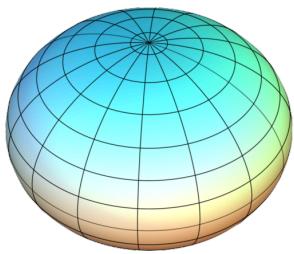


^{104}Pd

*N. Quang Hung, N. Dinh
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B 8, 551 (2015)*

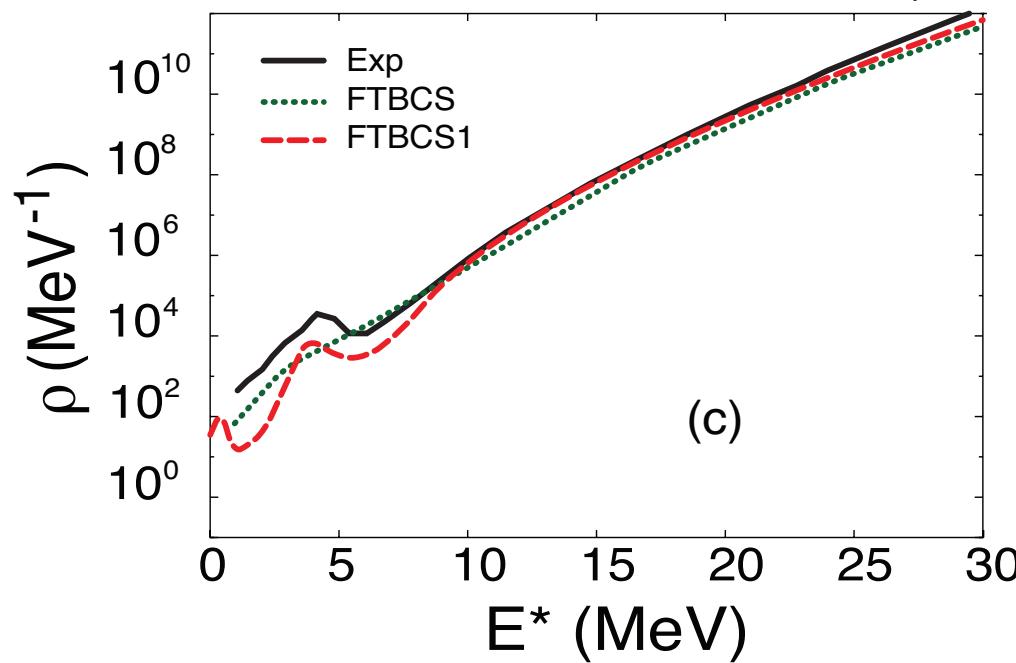
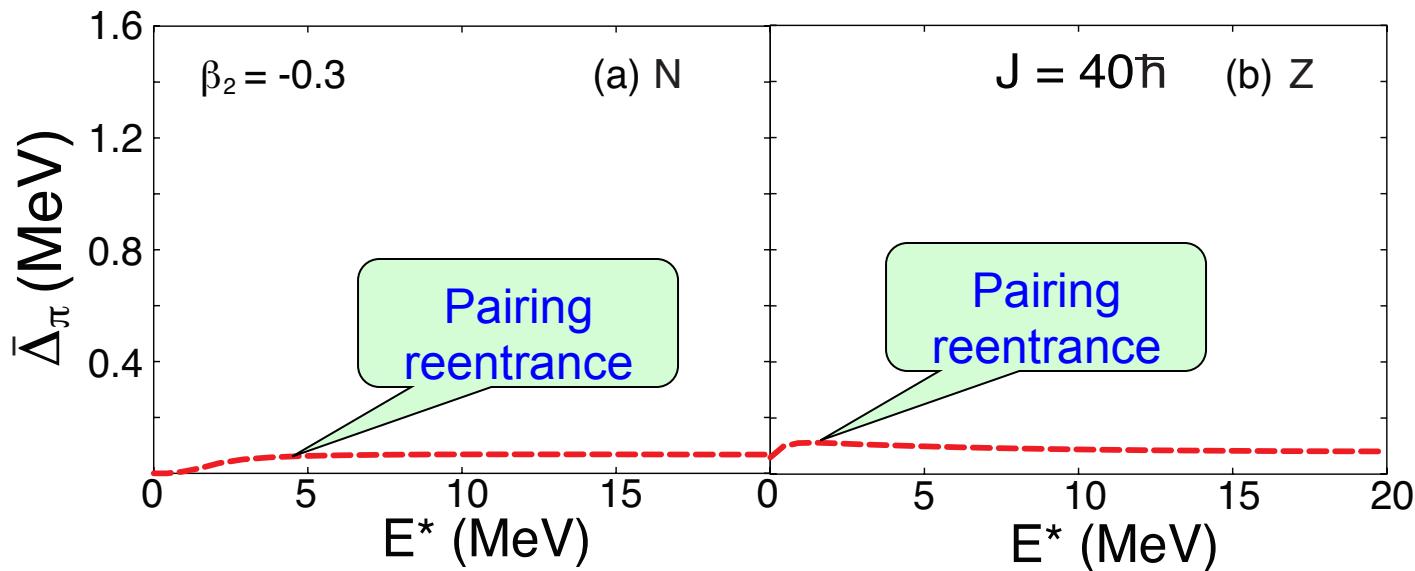


FTBCS1 vs Exp



^{104}Pd

*N. Quang Hung, N. Dinh
Dang, B. K. Agrawal, V. M.
Data, A. Mitra, and D. R.
Chakrabarty, Act. Phys. Pol.
B 8, 551 (2015)*



Research Topics

□ Present Research Topics:

✧ *Pairing Reentrance Phenomenon*

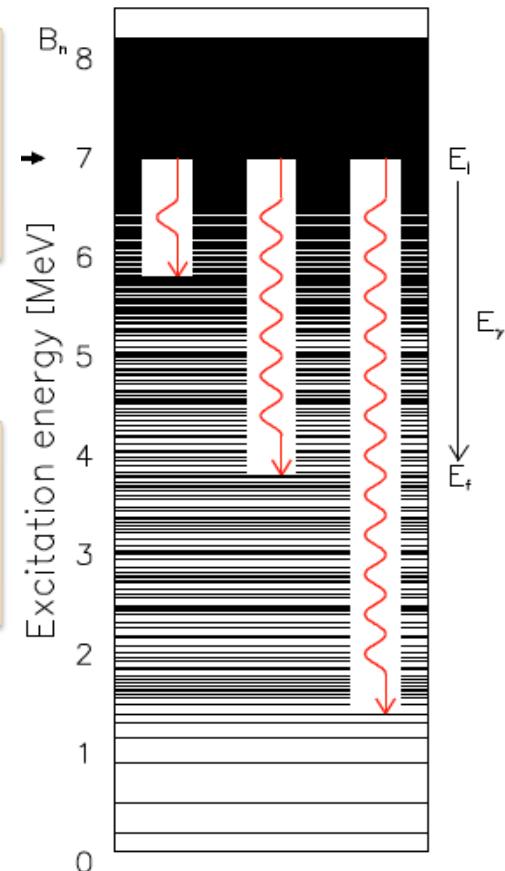
✧ *Nuclear Level Density and Radiative Strength Function*

❖ NLD = number of excited levels
per unit of excitation energy

H. A. Bethe, Phys. Rev. C 50, 332 (1936)

❖ RSF = average transition
probability per γ -ray energy

J. M. Blatt and V. F. Weisskopf, Theoretical Nuclear Physics (Wiley, New York, 1952).





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■ Measured NLDs and
RSFs

■ Presentations at
group meetings

Level densities and gamma-ray strength functions

<http://www.mn.uio.no/fysikk/english/research/about/infrastructure/OCL/nuclear-physics-research/compilation/>

The data are extracted according to the Oslo-method (A. Schiller et al., Nucl. Instrum. Methods A 447 (2000) 498). For the present data set, both the ($^3\text{He}, ^3\text{He}$) and ($^3\text{He}, ^4\text{He}$) reactions have been used. A comparison between the two reactions is performed in Ref.: A. Schiller et al., Phys. Rev. C61, 044324 (2000).

Some papers show, together with new data, also previously published data. These may be identical, however, in some cases small adjustments have been made from more recent information, e.g. new (n,g) neutron resonance spacing data. Therefore, the data from the most recent paper should be adopted.

You may download these data and pdf figures. If you publish them, please give references to the method and the journal where the data were published (see below).

If you have comments or questions, please contact magne.guttormsen@fys.uio.no

Level densities

You may download pdf figures for some of these data here:

[SmDyErYb](#), [Dy](#), [Yb](#), [Mo](#), [Fe](#), [V](#), [new 96Mo](#), [Sc](#), [new 56,57Fe](#), [116,117Sn](#)

Gamma-ray strength functions (radiative strength functions RSF)

You may download pdf figures for some of these data here:

[SmDyErYb](#), [Dy](#), [Yb](#), [Mo](#), [Fe](#), [50V](#), [51V](#), [new 96Mo](#), [Sc](#), [new 56,57Fe](#)

A. Voinov et al., Phys. Rev. C63, 044313 (2001): ($^3\text{He}, ^4\text{He}$) ^{161}Dy

A. Voinov et al., Phys. Rev. C63, 044313 (2001): ($^3\text{He}, ^4\text{He}$) ^{162}Dy

E. Melby et al., Phys. Rev. C63, 044309 (2001): ($^3\text{He}, ^4\text{He}$) ^{166}Er

E. Melby et al., Phys. Rev. C63, 044309 (2001): ($^3\text{He}, ^3\text{He}$) ^{167}Er

A. Voinov et al., Phys. Rev. C63, 044313 (2001): ($^3\text{He}, ^4\text{He}$) ^{172}V

A. Voinov et al., Phys. Rev. C63, 044313 (2001): ($^3\text{He}, ^4\text{He}$) ^{172}V

$$P(E_i, E_\gamma) \propto \rho(E_f) \cdot T(E_\gamma)$$

M. Guttormsen et al., Phys. Rev. C68, 064306 (2003): ($^3\text{He}, ^4\text{He}$) ^{160}Dy

M. Guttormsen et al., Phys. Rev. C68, 064306 (2003): ($^3\text{He}, ^3\text{He}$) ^{161}Dy

M. Guttormsen et al., Phys. Rev. C68, 064306 (2003): ($^3\text{He}, ^4\text{He}$) ^{161}Dy

M. Guttormsen et al., Phys. Rev. C68, 064306 (2003): ($^3\text{He}, ^3\text{He}$) ^{162}Dy

M. Guttormsen et al., Phys. Rev. C68, 064306 (2003): ($^3\text{He}, ^4\text{He}$) ^{162}Dy

U. Agvaanluvsan et al., Phys. Rev. C70, 054611 (2004): ($^3\text{He}, ^4\text{He}$) ^{170}Yb

U. Agvaanluvsan et al., Phys. Rev. C70, 054611 (2004): ($^3\text{He}, ^3\text{He}$) ^{171}Yb

U. Agvaanluvsan et al., Phys. Rev. C70, 054611 (2004): ($^3\text{He}, ^4\text{He}$) ^{171}Yb

U. Agvaanluvsan et al., Phys. Rev. C70, 054611 (2004): ($^3\text{He}, ^3\text{He}$) ^{172}Yb

U. Agvaanluvsan et al., Phys. Rev. C70, 054611 (2004): ($^3\text{He}, ^4\text{He}$) ^{172}Yb

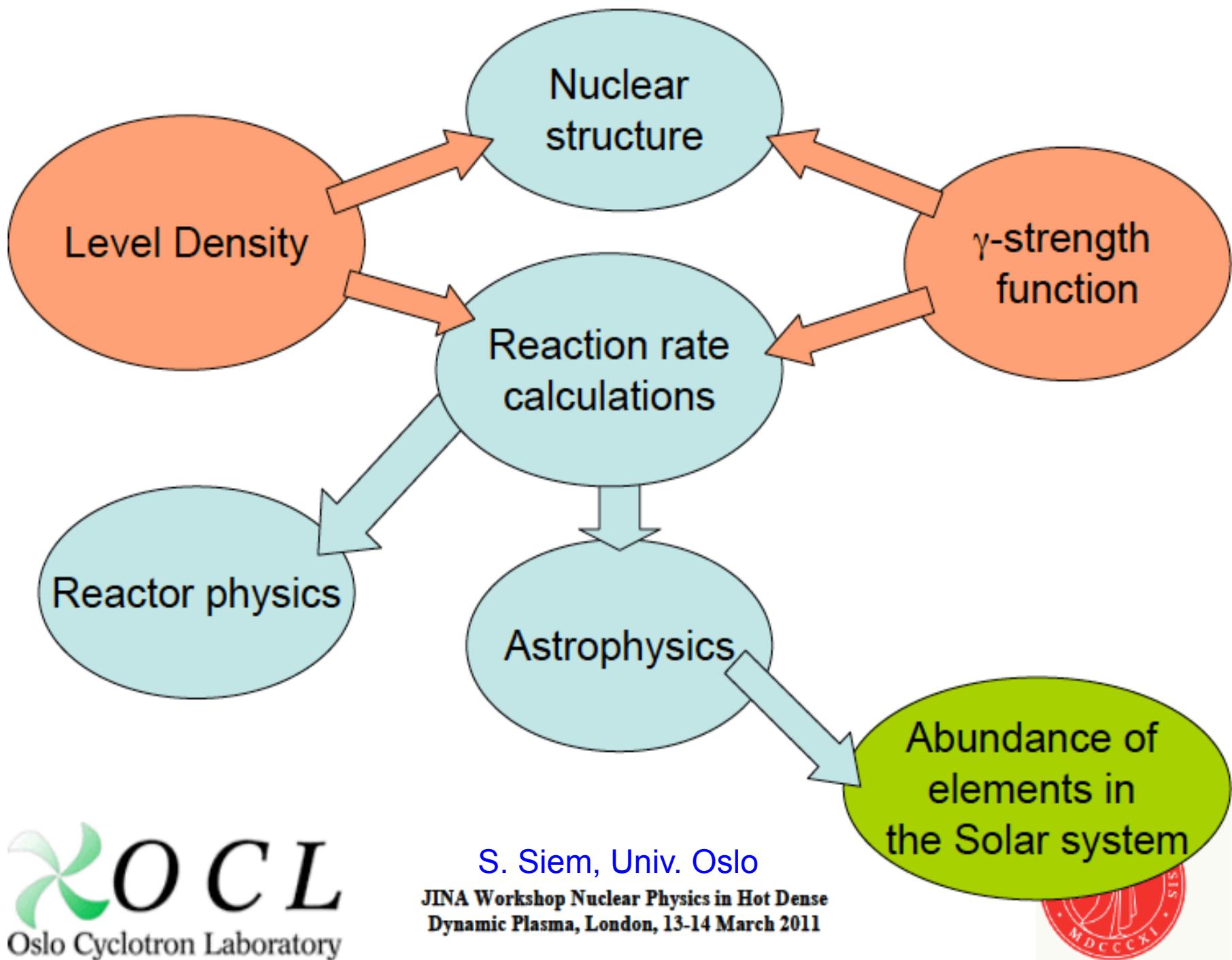
A. Voinov et al., Phys. Rev. Lett. 93, 142504 (2004): ($^3\text{He}, ^4\text{He}$) ^{56}Fe

A. Voinov et al., Phys. Rev. Lett. 93, 142504 (2004): ($^3\text{He}, ^3\text{He}$) ^{57}Fe

M. Guttormsen et al., Phys. Rev. C71, 044307 (2005): ($^3\text{He}, ^4\text{He}$) ^{93}Mo

M. Guttormsen et al., Phys. Rev. C71, 044307 (2005): ($^3\text{He}, ^3\text{He}$) ^{94}Mo

M. Guttormsen et al., Phys. Rev. C71, 044307 (2005): ($^3\text{He}, ^4\text{He}$) ^{95}Mo



Nuclear level density and the determination of thermonuclear rates for astrophysics

Thomas Rauscher

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Friedrich-Karl Thielemann

Institut für Physik, Universität Basel, Basel, Switzerland

Karl-Ludwig Kratz

Institut für Kernchemie, Universität Mainz, Germany

Hauser-Feshbach Theory

$$d\sigma(E) \sim T(E)\rho(E^*)dE$$

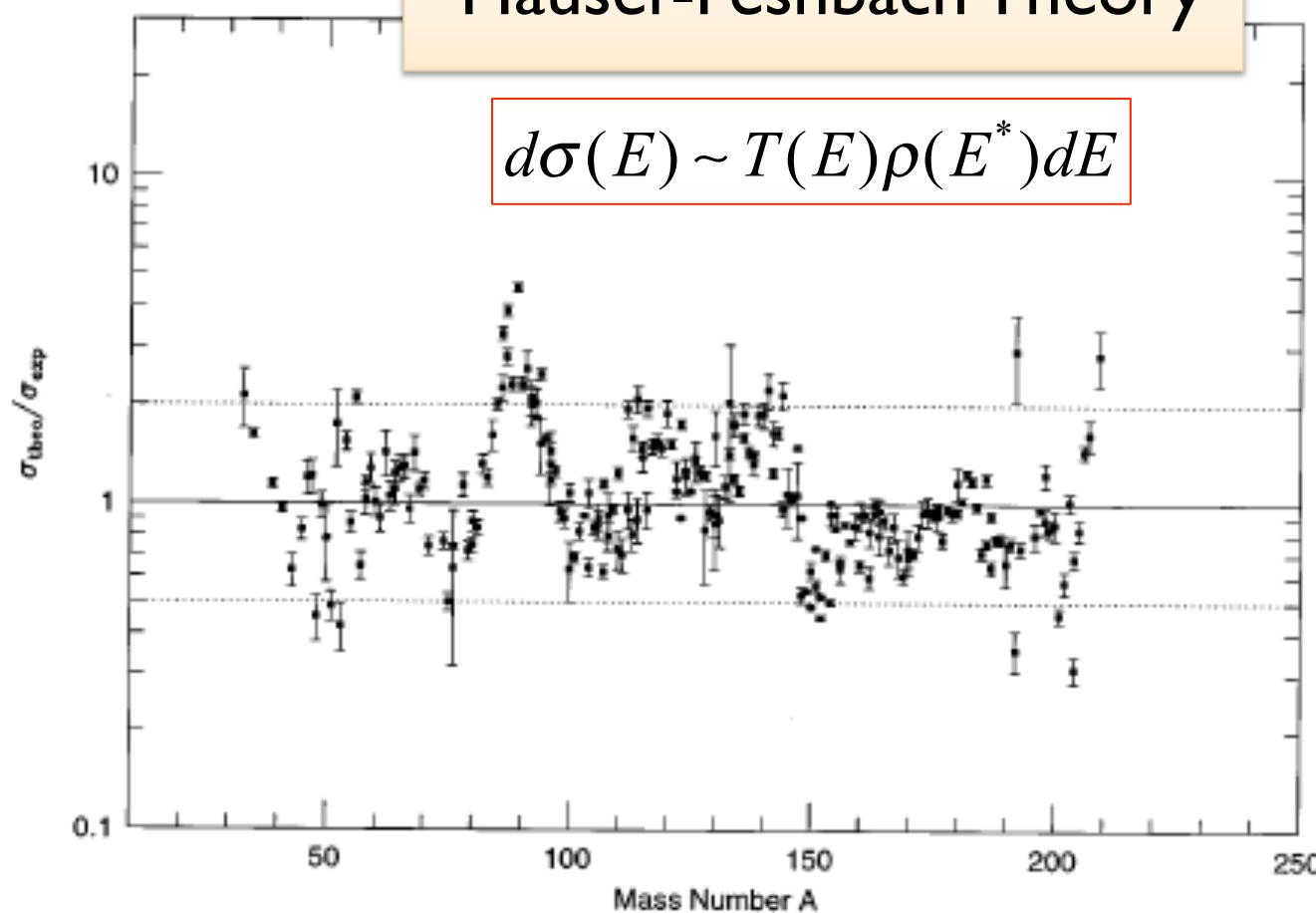


FIG. 5. Ratio of theoretical to experimental [50] neutron capture cross sections at 30 keV. Cross sections for light nuclei ($A < 30$) are not plotted because the statistical model cannot be applied in that region for neutron-capture reactions (compare Fig. 7).

Present Research Topics

Phenomenological Models for NLD

Back-Shifted Fermi-gas model

Non-interacting Fermi particles moving in a potential

$$\rho(U) = \frac{1}{12\sqrt{2}\sigma} \frac{\exp(2\sqrt{aU})}{a^{1/4} U^{5/4}}$$

$$\sigma^2 = \frac{I_{\text{rigid}}}{\hbar^2} \sqrt{\frac{U}{a}}, \quad I_{\text{rigid}} = \frac{2}{5} m_u A R^2, \quad U = E - \delta$$

$$a(U, Z, N) = \tilde{a}(A) \left[1 + C(Z, N) \frac{f(U)}{U} \right]$$

$$\tilde{a} = \alpha A + \beta A^{2/3}, \quad f(U) = 1 - e^{-\gamma U}$$

Constant temperature model

Classical ideal gas (used for low excitation-energy region)

$$\rho(U) = \frac{1}{T} \exp\left(\frac{U - E_0}{T}\right)$$

A. Gilbert and A. G. W. Cameron,
Can. J. Phys. 43, 1446 (1965)

H. A. Bethe, Phys. Rev. 50, 332 (1936)

Present Research Topics

Microscopic Models for NLD

- ◆ Hartree-Fock-Bogoliubov plus Combinatorial Method (**HFBC**)
- ◆ Shell Model Monte Carlo (**SMMC**)



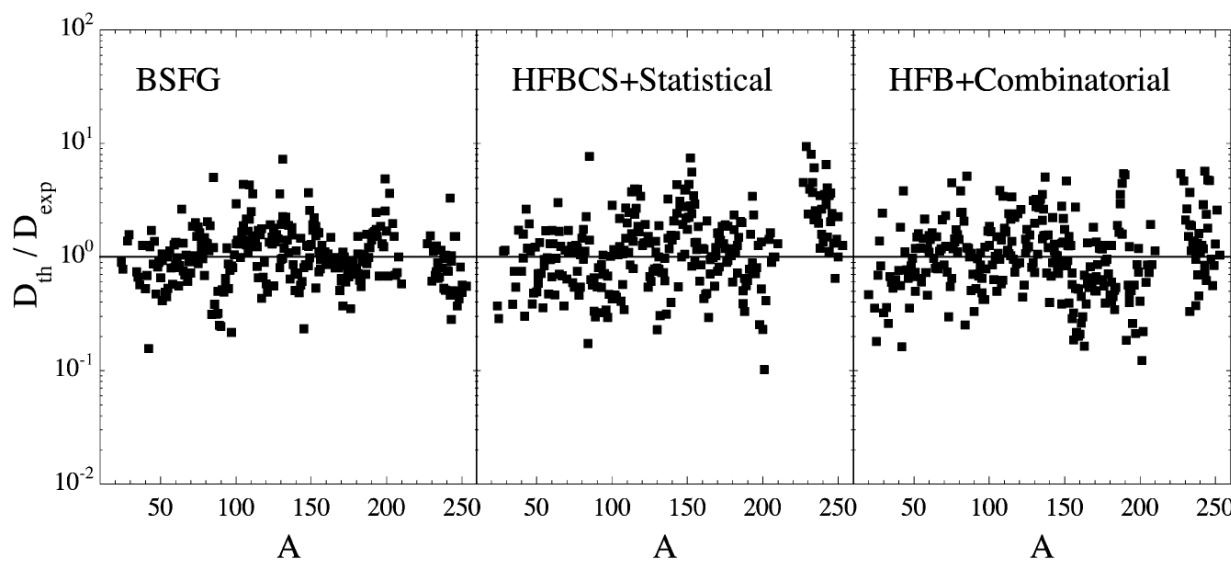
HFBC

- Single-particle levels: Hartree Fock Bogoliubov with Skyrme NN effective interactions (BSk14)
- Combinatorial Method:
 - Construct incoherent particle-hole (ph) state densities as function of E^* , M , and π .
 - Incoherent ph states plus vibrational enhancement treated by using the boson partition function including quadrupole, octupole, and hexadecapole vibrational modes are then used to compute the total state densities and NLD.

[S. Hilaire and S. Goriely, Nucl. Phys. A 779, 63 \(2006\)](#)

[S. Goriely et al., Phys. Rev. C 75, 064312 \(2007\)](#)

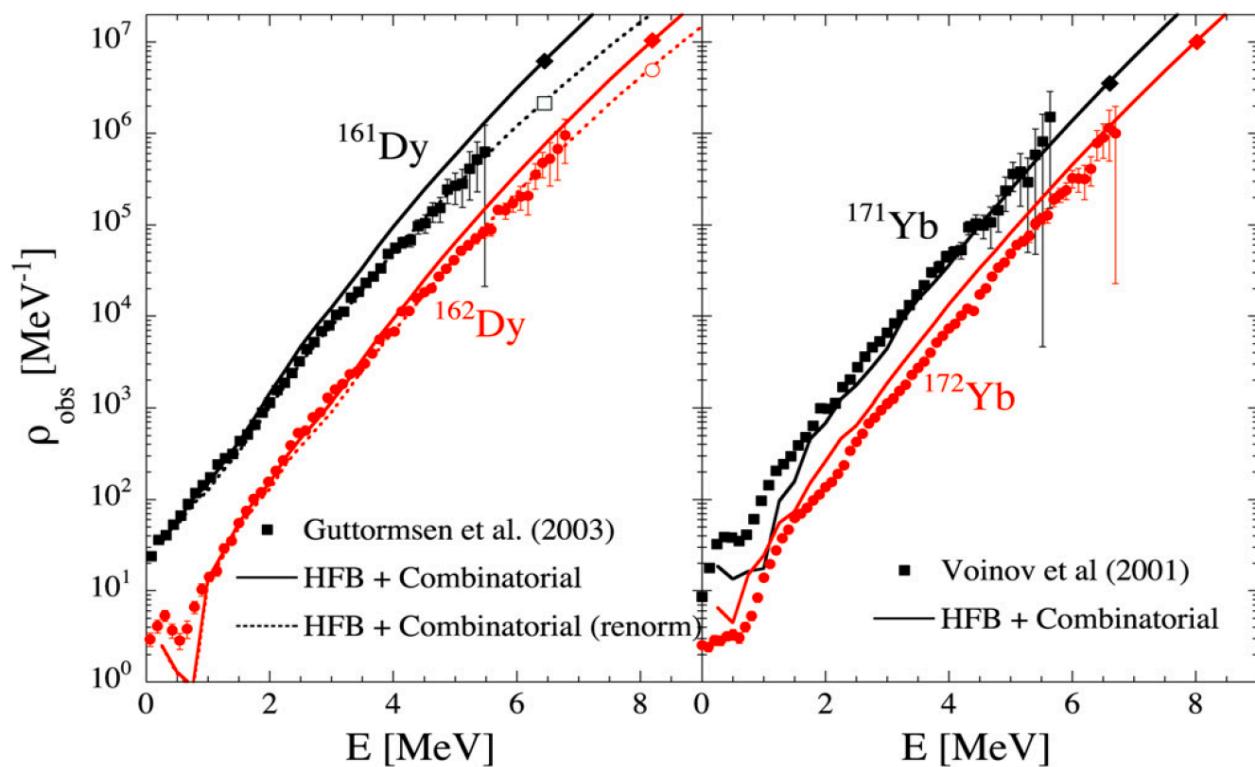
[S. Goriely et al., Phys. Rev. C 78, 064307 \(2008\)](#)



[S. Hilaire and S. Goriely, Nucl. Phys. A 779, 63 \(2006\)](#)

$$D_0 = \begin{cases} \frac{1}{\rho(S_n, J_0 + 1/2, P_0) + \rho(S_n, J_0 - 1/2, P_0)} & \text{for } J_0 > 0, \\ \frac{1}{\rho(S_n, 1/2, P_0)} & \text{for } J_0 = 0. \end{cases}$$

The most
microscopic
approach to NLD
up to date !



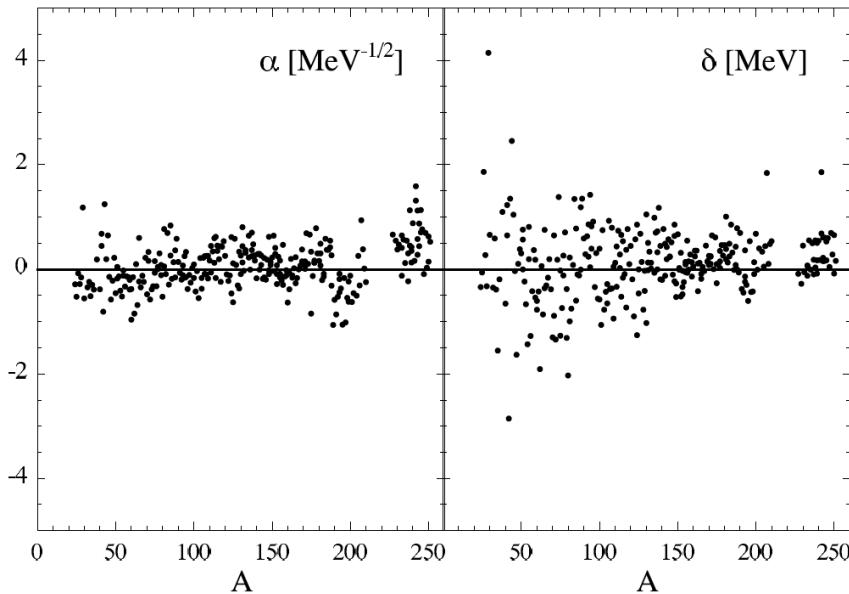
<https://www-nds.iaea.org/RIPL-3/>

HFBC

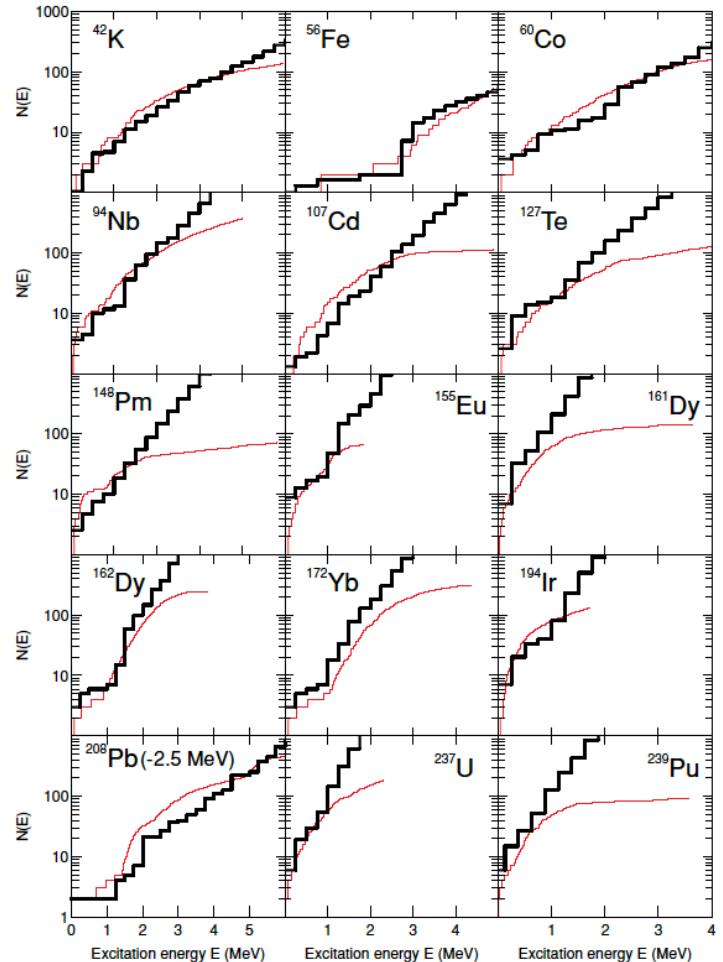
$$\rho(U, J, P)_{\text{renom}} = e^{\alpha \sqrt{(U-\delta)}} \times \rho(U - \delta, J, P),$$

δ : adjusted to fit the experimental cumulative levels at low U

α : adjusted to fit the experimental NLD at neutron separating energy B_n



[S. Goriely, S. Hilaire, and A. J. Koning, Phys. Rev. C 78, 064307 \(2008\)](#)



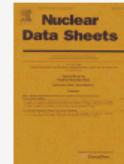


Archive
RIPL-1
RIPL-2
CRP (RIPL-3)
Related Links
Nuclear Data Services
Nuclear Data on CD's
ENSDF
NuDat
EMPIRE-II
Nuclear Data Sheets



Reference Input Parameter Library (RIPL-3)

R. Capote, M. Herman, P. Oblozinsky, P.G. Young, S. Goriely, T. Belgya, A.V. Ignatyuk, A.J. Koning, S. Hilaire, V.A. Plujko, M. Avrigeanu, O. Bersillon, M.B. Chadwick, T. Fukahori, Zhigang Ge, Yinlu Han, S. Kailas, J. Kopecky, V.M. Maslov, G. Reffo, M. Sin, E.Sh. Soukhanovskii and P. Talou



Nuclear Data Sheets - Volume 110, Issue 12, December 2009, Pages 3107-3214

RIPL discrete levels database updated in August 2015 - it contains the correction for +X,.. levels

[Introduction] [MASSES] [LEVELS] [RESONANCES] [OPTICAL] [DENSITIES] [GAMMA] [FISSION] [CODES] [Contacts]

Level Densities Segment

Total Level Densities

<https://www-nds.iaea.org/RIPL-3/>

Back-Shifted Fermi Gas Model (BSFG)

Level density parameters for the BSFG model obtained by fitting the Fermi-gas model formula to the recommended spacings of s-wave neutron resonances and to the cumulative number of low-lying levels.

[Data File \(34.3kB\)](#) [README File \(2.2kB\)](#)

Gilbert-Cameron Model

Level density parameters for the Gilbert-Cameron model obtained by fitting the Fermi-gas model formula to the recommended spacings of s-wave neutron resonances and by matching the corresponding level density to discrete levels.

[Data File \(42.8kB\)](#) [README File \(2.4kB\)](#)

Enhanced Generalized Superfluid Model (EGSM)

Level density parameters for the Enhanced Generalized Superfluid Model (EGSM), which takes into account collective enhancement of the nuclear level density in addition to shell and superfluid effects. The parameters were obtained by fitting the corresponding model formulas to the recommended spacings of s-wave neutron resonances and by matching level densities to discrete levels.

[Data File \(26.1kB\)](#) [README File \(2.4kB\)](#)

Z Systematics:

[Data File \(1.3kB\)](#) [README File \(1.3kB\)](#)

HFB Total Level Densities

The data files (*.dat) contains the HFB plus combinatorial nuclear level densities at ground state deformations^[1]. The nuclear level density is coherently obtained on the basis of the single-particle level scheme and pairing energy derived at the ground state deformation based on the BSk14 Skyrme force^[2].

Retrieval of Total Level Density Parameters

Atomic number (Z)
 Mass number (A)
 (blank for all mass numbers)

Plot of Total Level Density Parameters (a-parameters)

Select one of below and input no.:

Atomic number (Z)
 Mass number (A)
 Neutron number (N)

X-axis: A

Plot of Total Level Densities

Atomic number (Z)
 Mass number (A)

Retrieval of HFB

SMMC

The Gibbs ensemble $e^{-\beta H}$ describing a nucleus with Hamiltonian H at inverse temperature β , can be decomposed as a superposition of ensembles U_σ of non-interacting nucleons in external auxiliary fields $\sigma(\tau)$ that depend on imaginary time τ ($0 \leq \tau \leq \beta$)

$$e^{-\beta H} = \int D[\sigma] G_\sigma U_\sigma$$

G_σ is a Gaussian weight.

Hubbard-Stratonovich transformation

$$\langle O \rangle = \frac{\text{Tr}(O e^{-\beta H})}{\text{Tr}(e^{-\beta H})} = \frac{\int D[\sigma] W_\sigma \Phi_\sigma \langle O \rangle_\sigma}{\int D[\sigma] W_\sigma \Phi_\sigma}$$

$$W_\sigma = G_\sigma |\text{Tr } U_\sigma| \quad \langle O \rangle_\sigma = \text{Tr}(O U_\sigma) / \text{Tr } U_\sigma$$

$\Phi_\sigma = \text{Tr } U_\sigma / |\text{Tr } U_\sigma|$ is the Monte Carlo sign

$$E(\beta) = \langle H \rangle \quad Z(\beta) \equiv \text{Tr } e^{-\beta H}$$

$$\rho(E) \approx \left(-2\pi \frac{dE}{d\beta} \right)^{-1/2} e^{S(E)}$$



SMMC

$$\rho_J(E_x) = \rho(E_x) \frac{(2J+1)}{2\sqrt{2\pi}\sigma_c^3} e^{-\frac{J(J+1)}{2\sigma_c^2}},$$

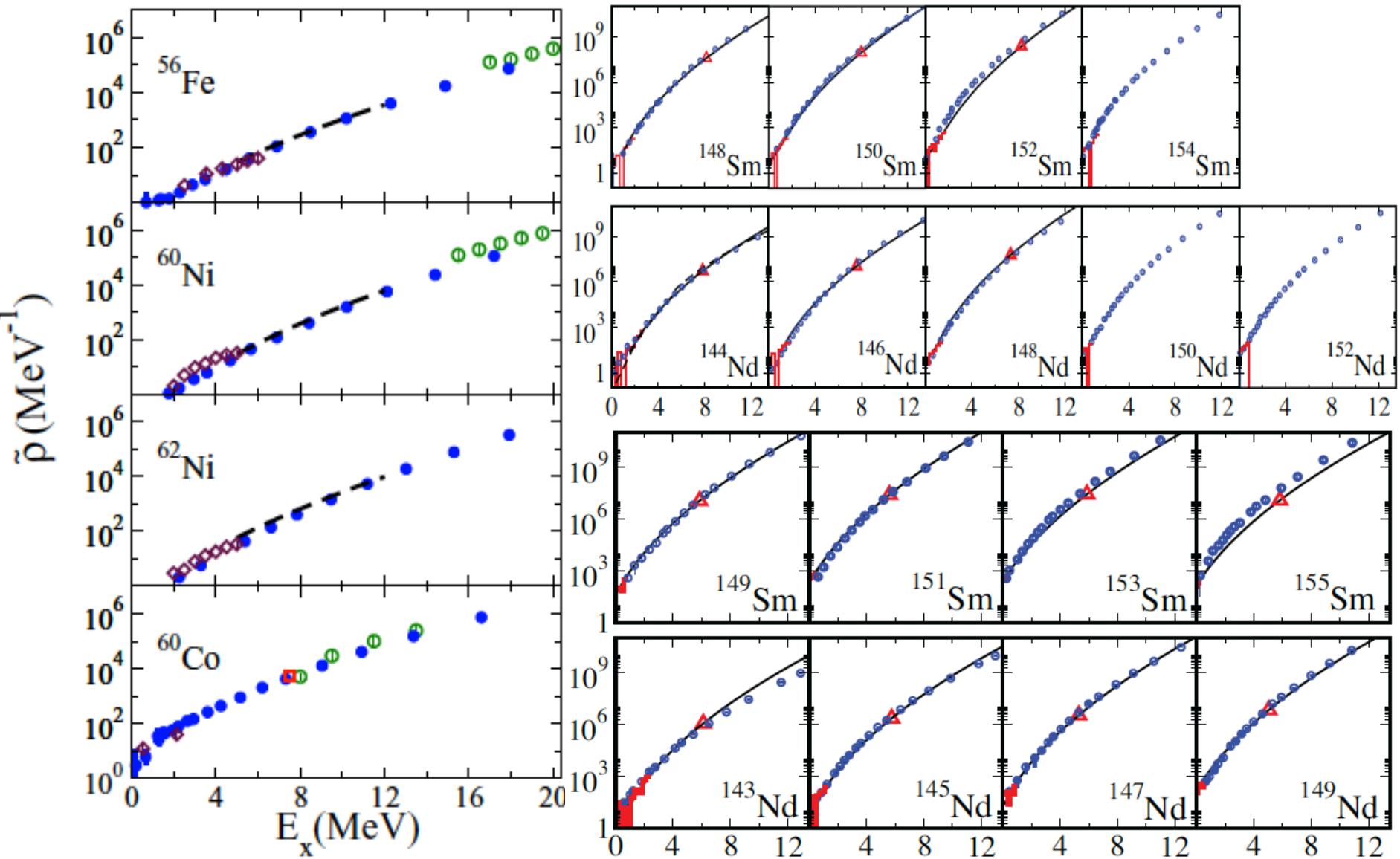
$$\tilde{\rho}(E_x) = \sum_J \rho_J(E_x) \approx \frac{1}{\sqrt{2\pi}\sigma_c} \rho(E_x),$$

$$\sigma_c(E_x) = (2\pi)^{-1/2} \rho(E_x)/\tilde{\rho}(E_x).$$

σ_c : obtained by fitting the theoretical NLD with exp

- H. Nakada and Y. Alhassid, Phys. Rev. Lett. 79, 2939 (1997).
Y. Alhassid, S. Liu, and H. Nakada, Phys. Rev. Lett. 83, 4265 (1999).
S. Liu and Y. Alhassid, Phys. Rev. Lett. 87, 022501 (2001).
Y. Alhassid, S. Liu, and H. Nakada, Phys. Rev. Lett. 99, 162504 (2007).
Y. Alhassid, L. Fang, and H. Nakada, Phys. Rev. Lett. 101, 082501 (2008).
C. Ozen, Y. Alhassid, and H. Nakada, Phys. Rev. Lett. 110, 042502 (2013).

SMMC



Models for RSF

□ Phenomenological

- *Kadmenski-Markushev-Furman (KMF)*
- *Standard Lorentzian (SLO)*
- *Generalized Lorentzian (GLO)*
- *Enhanced Generalized Lorentzian (EGLO)*
- *Generalized Fermi Liquid (GFL)*

□ Microscopic

- *Hartree-Fock-BCS + Quasiparticle Random-Phase Approximation (HFBCS + QRPA)*
-

KMF Model

<http://www.talys.eu/>

$$f(E_\gamma) = \kappa [f_{E1}(E_\gamma) + f_{M1}(E_\gamma)] + E_\gamma^2 f_{E2}(E_\gamma) + f_{pygmy}(E_\gamma)$$

$$f_{E1}(E_\gamma) = \frac{1}{3\pi^2\hbar^2c^2} \frac{0.7\sigma_{E1}\Gamma_{E1}^2(E_\gamma^2 + 4\pi^2T^2)}{E_{E1}(E_\gamma^2 - E_{E1}^2)^2}, \quad \Gamma_{E1}(E_\gamma, T) = \frac{\Gamma_{E1}}{E_{E1}^2}(E_\gamma^2 + 4\pi^2T^2)$$

$$f_{E2}(E_\gamma) = \frac{1}{5\pi^2\hbar^2c^2E_\gamma^2} \frac{\sigma_{E2}E_\gamma\Gamma_{E2}^2}{(E_\gamma^2 - E_{E2}^2)^2 + E_\gamma^2\Gamma_{E2}^2}$$

$$f_{M1}(E_\gamma) = \frac{1}{3\pi^2\hbar^2c^2} \frac{\sigma_{M1}E_\gamma\Gamma_{M1}^2}{(E_\gamma^2 - E_{M1}^2)^2 + E_\gamma^2\Gamma_{M1}^2}$$

$$f_{py}(E_\gamma) = \frac{1}{3\pi^2\hbar^2c^2} \frac{\sigma_{py}E_\gamma\Gamma_{py}^2}{(E_\gamma^2 - E_{py}^2)^2 + E_\gamma^2\Gamma_{py}^2}$$

S. G. Kadmenskij, V. P. Markushev, and V. I. Furman, *Yad. Fiz.* **37**, 277 (1983)

J. Kopecky and R. E. Chrien, *Nucl. Phys. A* **468**, 285 (1987).

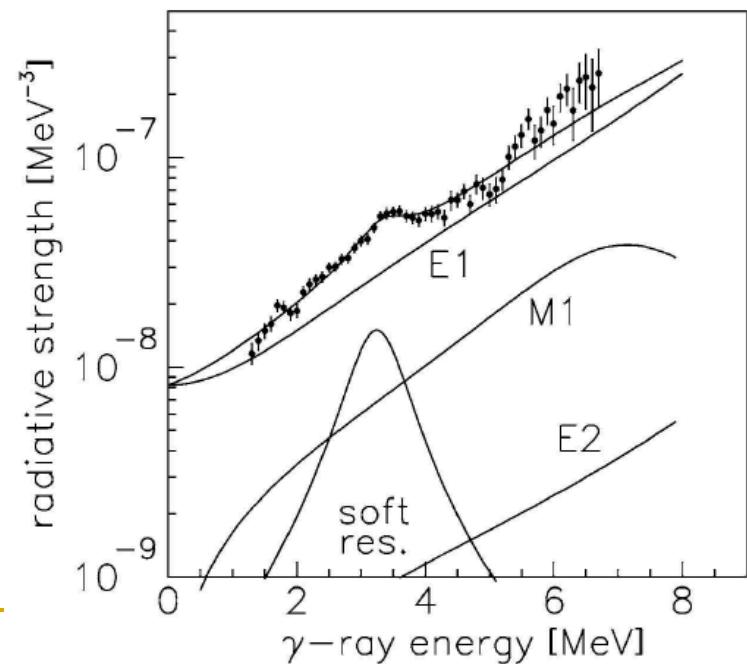
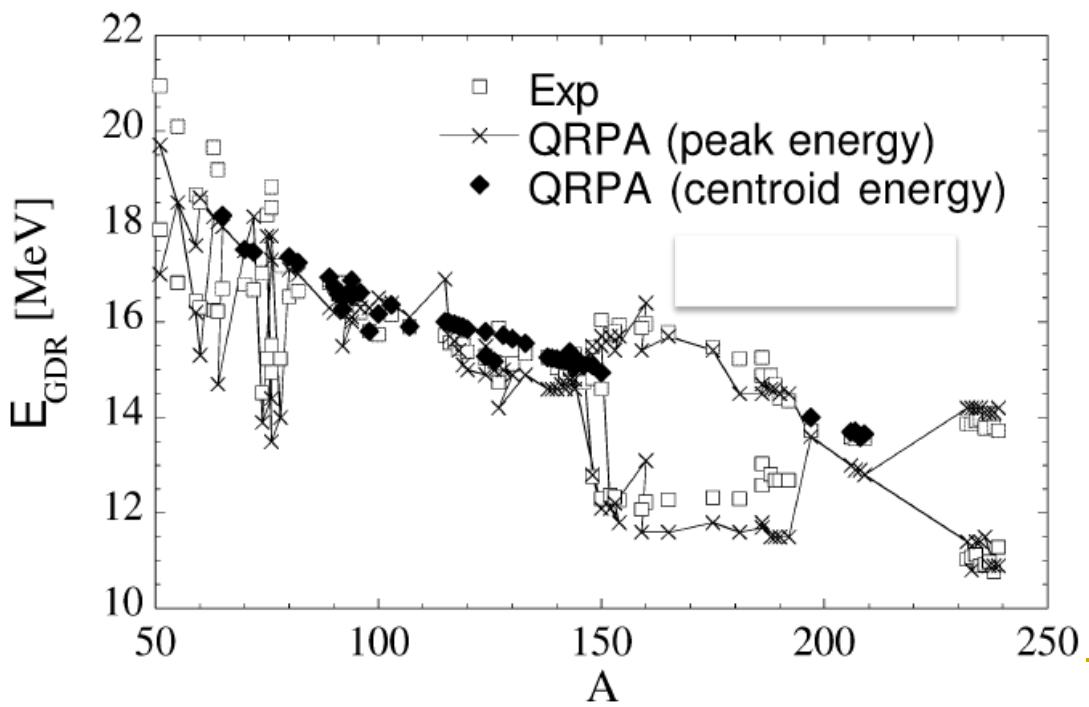
HFBCS + QRPA

<https://www-nds.iaea.org/RIPL-3/>

S. Goriely and E. Khan, Nucl. Phys. A 706, 217 (2002)

$$f_L(E, E_i, \gamma_i) = \frac{2}{\pi} \frac{\gamma_i E^2}{(E^2 - E_i^2)^2 + \gamma_i^2 E^2}.$$

$$\gamma_i = \Gamma_{\text{GDR}}/2$$



Microscopic Approach to NDL and RSF

[N. Quang Hung, N. Dinh Dang, and L.T. Quynh Huong, Phys. Rev. Lett. 118, 022502 \(2017\)](#)

□ For NLD

- *Exact pairing (EP): solve the pairing problem exactly by diagonalizing directly $\mathbf{H} = \mathbf{H}_0 + \mathbf{H}_{pair}$ within the truncated space → exactly conserve the particle number*

[A.Volya et al., Phys. Lett. B 509, 37 \(2001\)](#)

- *Independent Particle Model (IPM) (particles move independently when nucleus is excited): used to treat particles outside the truncated spaces.*

[Y.Allassid et al., Phys. Rec. C 68, 044322 \(2003\)](#)

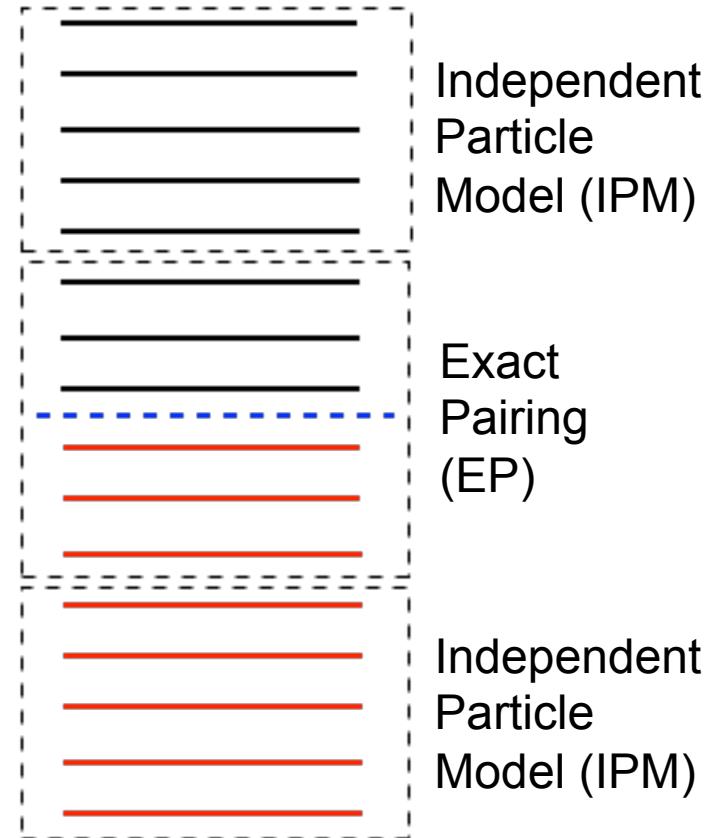
$$\ln Z_{tol} = \ln Z_{EP} + \ln Z_{IPM}$$

Total state density:

$$\omega(E) = \left(\frac{1}{2\pi i} \right)^2 \int_{-i\infty}^{+i\infty} e^{\beta E + \ln Z} d\beta$$

Total NLD:

$$\rho(E^*) = k_{rot} k_{vib} \frac{\omega(E^*)}{\sigma \sqrt{2\pi}}$$



Microscopic Approach to NDL and RSF

[N. Quang Hung, N. Dinh Dang, and L.T. Quynh Huong., Phys. Rev. Lett. 118, 022502 \(2017\)](#)

□ For RSF

[N. Dinh Dang, A. Arima, Phys. Rev. Lett. 80, 4145 \(1998\)](#)
[N. Dinh Dang, A. Arima, Phys. Rev. C 68, 044303 \(2003\)](#)

➤ Phonon Damping Model (PDM):

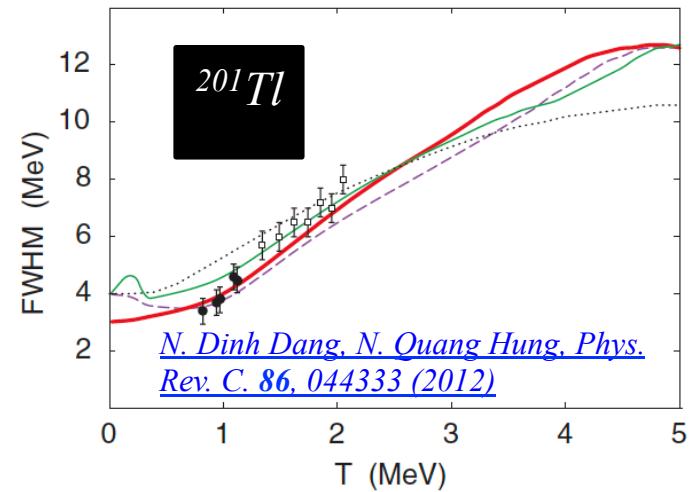
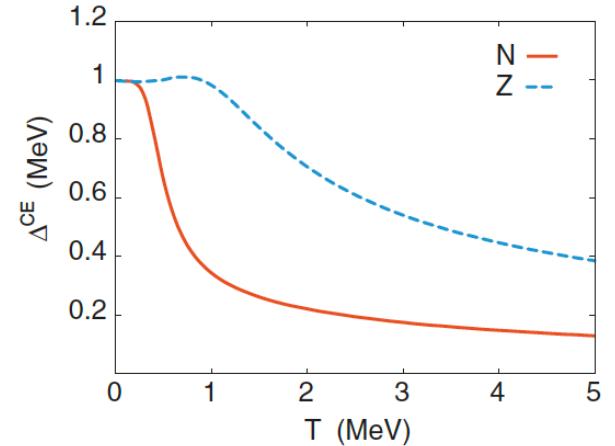
$$f_{XL}(E_\gamma) = \frac{1}{(2\lambda+1)\pi\hbar^2c^2} \frac{\Gamma(E_\gamma)\sigma(X\lambda)S_{X\lambda}(E_\gamma)}{E_\gamma}$$

X: E (electric), M (magnetic); λ: multipolarity

$$S_{X\lambda}(E_\gamma) = \frac{1}{\pi} \frac{\gamma(E_\gamma)}{(E_\gamma - E_{X\lambda})^2 + \gamma(E_\gamma)^2}$$

$$\Gamma_{X\lambda}(T) = 2\gamma[E_{X\lambda}(T)]$$

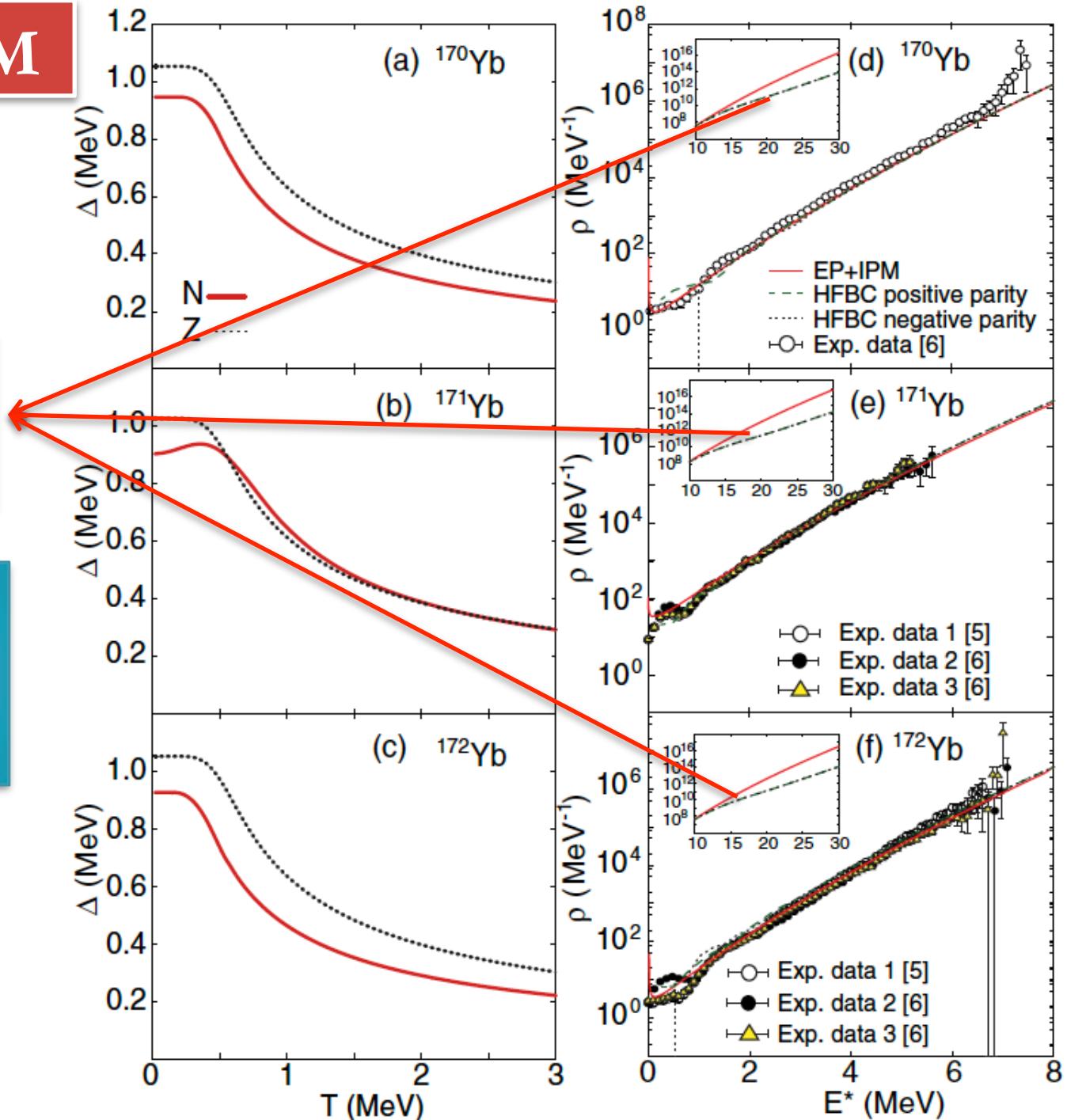
$$\begin{aligned} \gamma(E) = \pi & \left\{ F_1^2 \sum_{ph} u_{ph}^2 (1 - n_p - n_h) \delta(E - E_p - E_h) \right. \\ & \left. + F_2^2 \sum_{ss'} v_{ss'}^2 (n_{s'} - n_s) \delta(E - E_s - E_{s'}) \right\} \end{aligned}$$



NLD: EP+IPM

The HFBC NLDs are always lower than our NLDs at $E^* > B_n$

The HFBC NLDs are not reliable at high E^* due to their fitting to NLD data at B_n



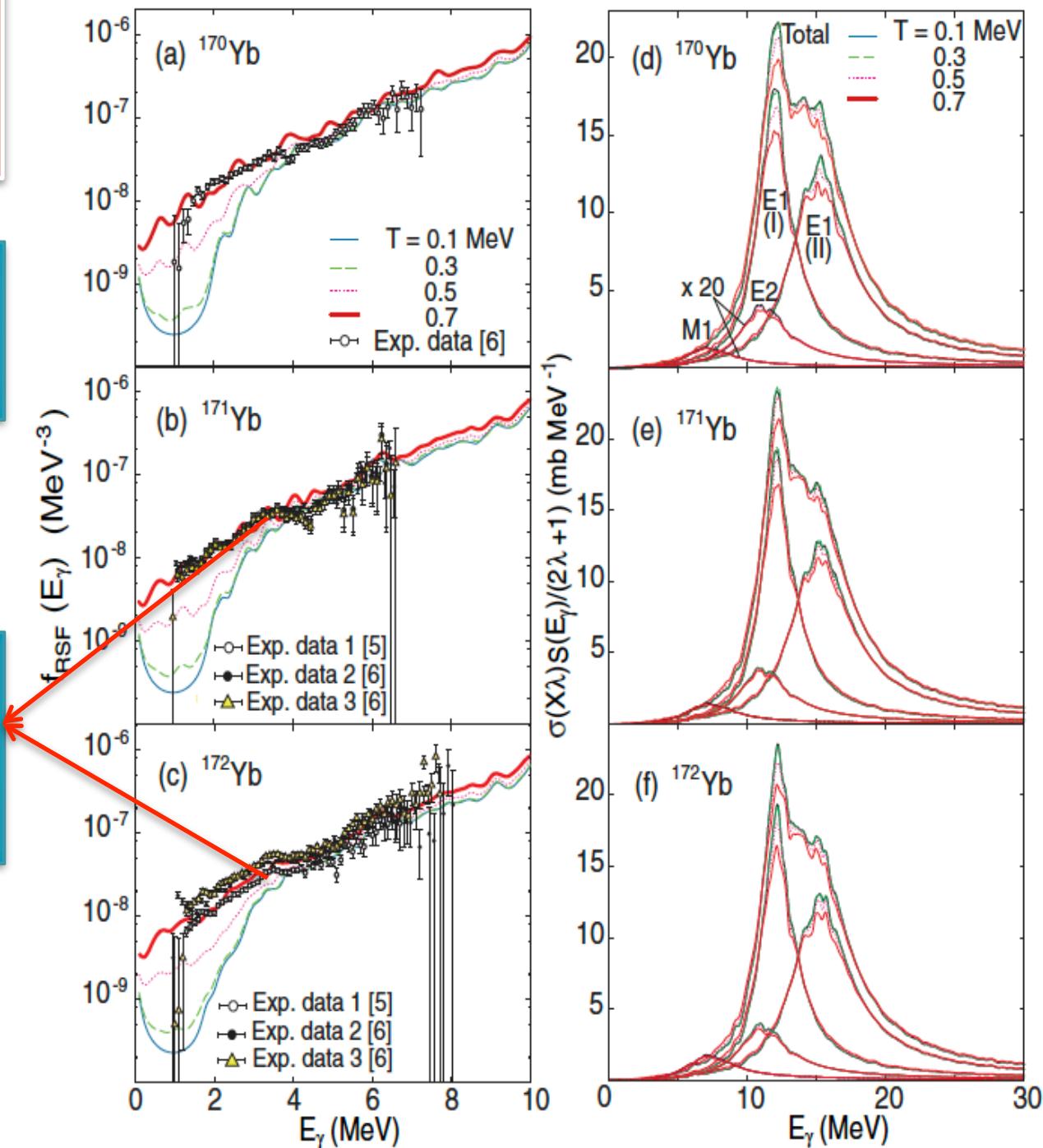
N. Quang Hung, N. Dinh Dang,
and L.T. Quynh Huong., Phys.
Rev. Lett. **118**, 022502 (2017)

RSF

EP+IPM+PDM

Temperature dependent RSF → invalidate the Brink Axel hypothesis

Enhancement of RSFs at low E is well reproduced without introducing PDR
→ effect of EP



N. Quang Hung, N. Dinh Dang,
and L.T. Quynh Huong., Phys.
Rev. Lett. 118, 022502 (2017)

Research Topics

□ Present Research Topics (**Extended**)

- ✧ *Pairing Reentrance Phenomenon*
- ✧ *Nuclear Level Density and Radiative Strength Function*
- ✧ *Nuclear Level Scheme from (n_{th}, γ) reactions*



Da Lat nuclear reactor began operating on 3.3.1963 with a capacity of 250KW, using US technology, and stopped working in 1968.



On 20/3/1984 it resumed operations, doubling its capacity.

Updated level scheme of ^{172}Yb from $^{171}\text{Yb}(\text{n}_{th}, \gamma)$ reaction studied via gamma-gamma coincidence spectrometer

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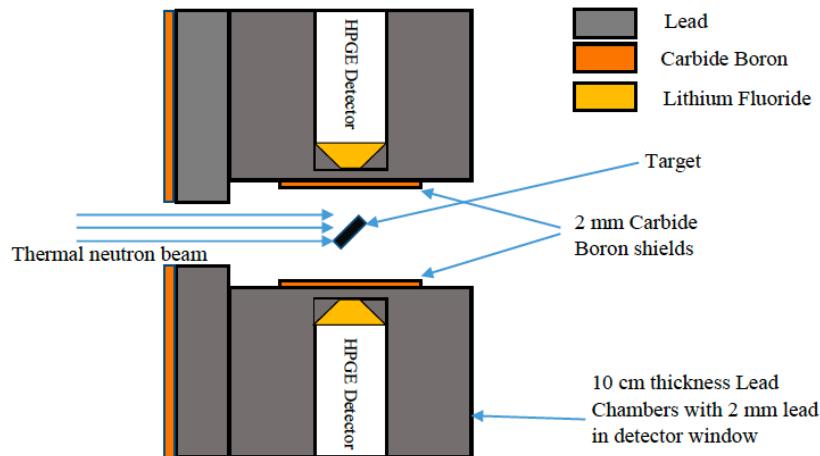
^bHanoi University of Science and Technology, 1 Dai Co Viet, Hanoi city, Vietnam

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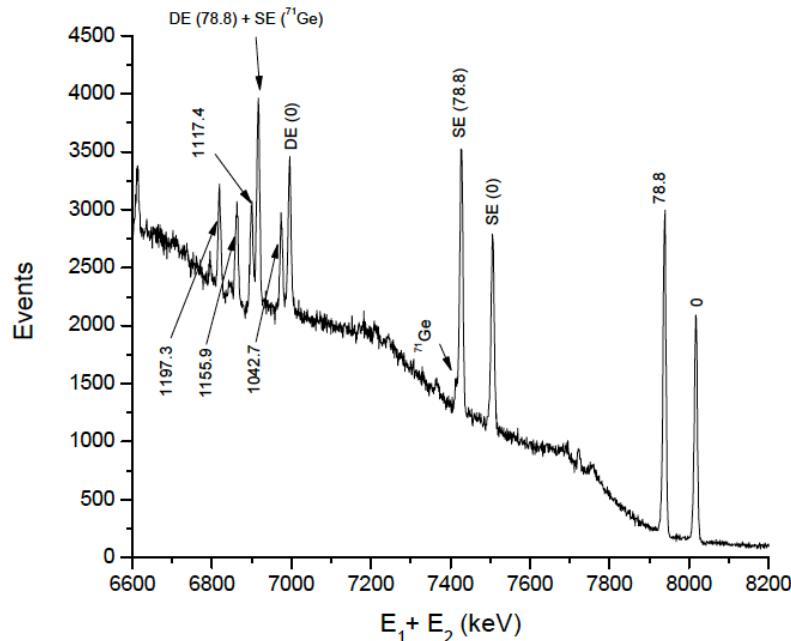
Submitted to Nucl. Phys. A
(Feb. 2017)

Abstract

This paper provides the updated information on the level scheme of ^{172}Yb nucleus studied via $^{171}\text{Yb}(\text{n}_{th}, \gamma)$ reaction using the gamma-gamma coincidence spectrometer at Dalat Nuclear Research Institute (Vietnam). The latter is used because of its advantages in achieving the low Compton background as well as in identifying the correlated gamma transitions. We have detected in total the energies and intensities of 128 two-step gamma cascades corresponding to 79 primary transitions. By comparing the measured data with those extracted from the ENSDF library, 61 primary gamma transitions and corresponding energy levels together with 19 secondary gamma transitions are found to be the same as the ENSDF data. Beside that, 18 additional primary gamma transitions and corresponding energy levels plus 109 secondary ones are not found to currently exist in this library and they are therefore considered as the new data.



Experimental setup for measuring the gamma-gamma coincidences.



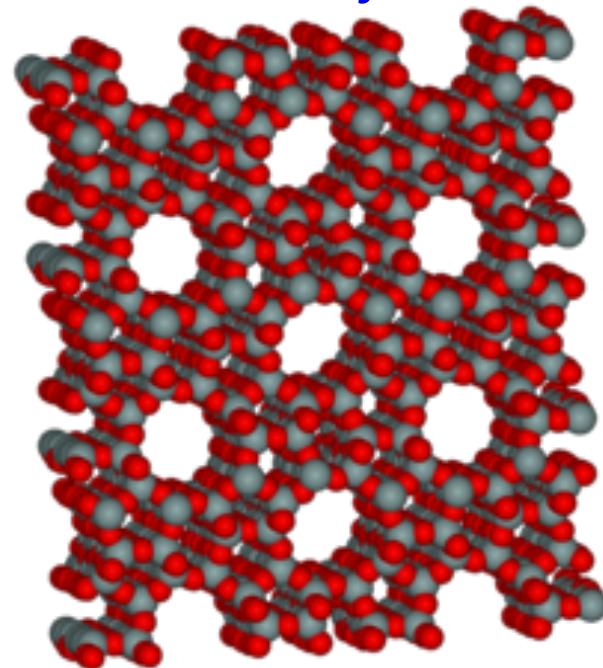
Keywords: Level scheme, $^{171}\text{Yb}(\text{n},\gamma)$ reaction, $\gamma - \gamma$ coincidence spectrometer.

Research Topics

□ Present Research Topics (**Extended**)

- ✧ *Pairing Reentrance Phenomenon*
- ✧ *Nuclear Level Density and Radiative Strength Function*
- ✧ *Nuclear Level Scheme from (n_{th}, γ) reactions*
- ✧ *Positron Annihilation Lifetime (PALS) and X-ray Diffraction Spectroscopies (XRD) Studies of Synthetic Nanosized Zeolite Materials*

ZSM-5



Simultaneous existence of defects and mesopores in nanosized ZSM-5 zeolite studied by positron annihilation and X-ray diffraction spectroscopies

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¹Center for Nuclear Techniques, Vietnam Atomic Energy Institute, 217 Nguyen Trai, District 1, Ho Chi Minh City, Vietnam

²Ho Chi Minh University of Science, 227 Nguyen Van Cu, District 5, Ho Chi Minh City, Vietnam

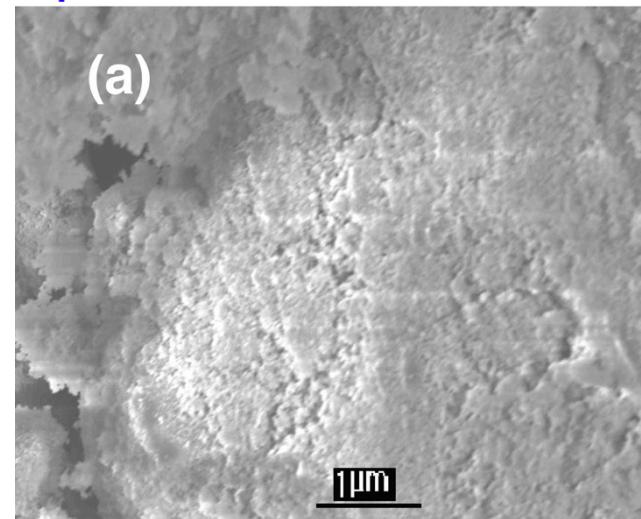
³Institute of Research and Development, Duy Tan University, K7/25 Quang Trung, Danang, Vietnam

⁴University of Technical Education, 1 Vo Van Ngan, Thu Duc District, Ho Chi Minh City, Vietnam

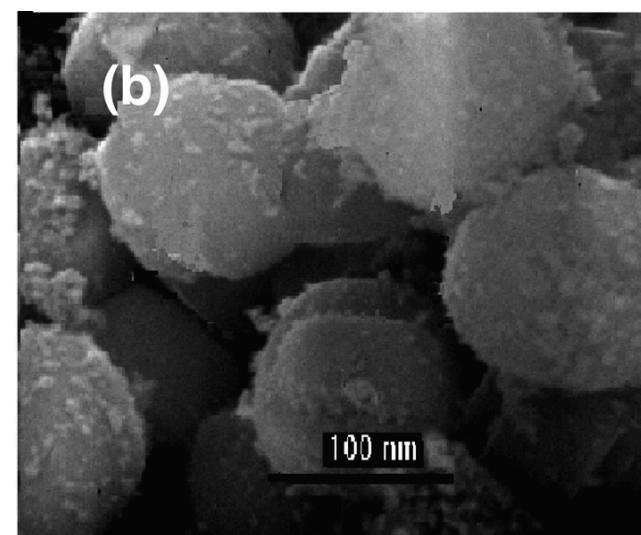
⁵Dong Nai University, 4 Le Quy Don, Bien Hoa, Vietnam

(Received 1 December 2016; accepted 8 February 2017; published online 24 February 2017)

Crystallization, formation, and accumulation of defects and mesopores in the ZSM-5 zeolite samples, which are synthesized from the gel composition of $1.2\text{Na}_2\text{O}$ $0.1\text{Al}_2\text{O}_3$ 0.8 tetrapropylammonium hydroxide (TPAOH) 6SiO_2 $400\text{H}_2\text{O}$ at a temperature of 140 degree Celsius ($^{\circ}\text{C}$) in 10, 15, and 18 h, are studied by using the Positron annihilation lifetime (PALS) and X-ray diffraction (XRD) spectroscopies. The XRD is used for investigating the crystalline concentration and nano-crystal size of ZSM-5 during the crystallizing process, whereas the PALS is performed in order to determine the presence of templates, defects, and mesopores in the zeolite samples. The latter are calcined in air during 1, 2, and 3 h at a temperature of $600\text{ }^{\circ}\text{C}$ before being measured. The results obtained indicate that there exist clusters of small crystals in the early crystalline stages of the samples. The size of these crystals increases with time and reaches approximately 100 nm after 18 h of reaction. In addition, the template (TPAOH) is found to exist not only in the channels inside the framework but also in the mesopores outside it. Finally, by analyzing the Positron lifetime spectra, we have found for the first time the simultaneous existence of defects and mesopores, which are formatted and accumulated during the crystallization of ZSM-5. Those important results contribute significantly to our understanding of the internal structure of the synthetic zeolite ZSM-5 as well as the synthetic processes for producing zeolites with special features. Published by AIP Publishing. [<http://dx.doi.org/10.1063/1.4977013>]



(a)



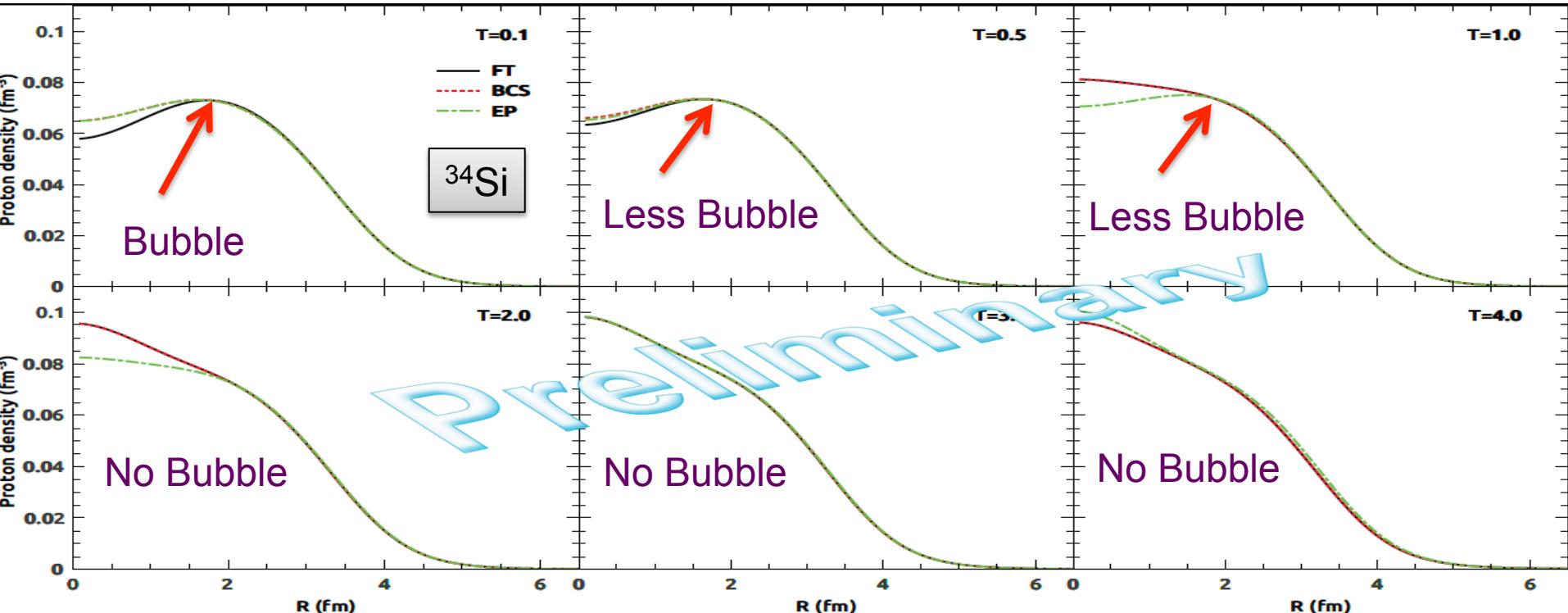
(b)

SEM images of the Z-10 (a) and Z-18 (b) zeolite samples.

Research Topics

□ Future perspectives

- ✧ *Pairing Reentrance Phenomenon*
More experimental data are needed
- ✧ *PDR and GDR within the RRPA at $T=0$ and $T \neq 0$*
 - *Exact pairing (EP) should be included into the HF calculations*
 - *RRPA (+ EP) with fully selfconsistent treatment of pp and hh excitations*

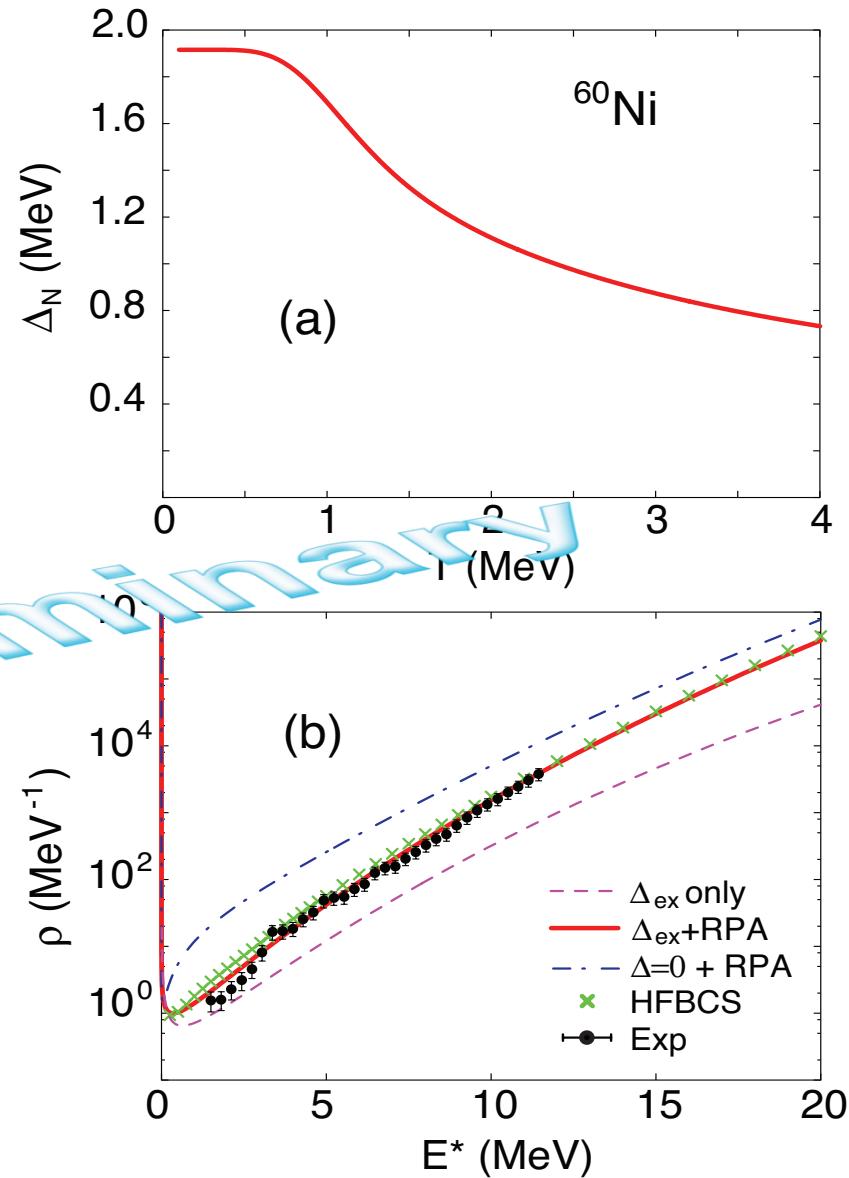
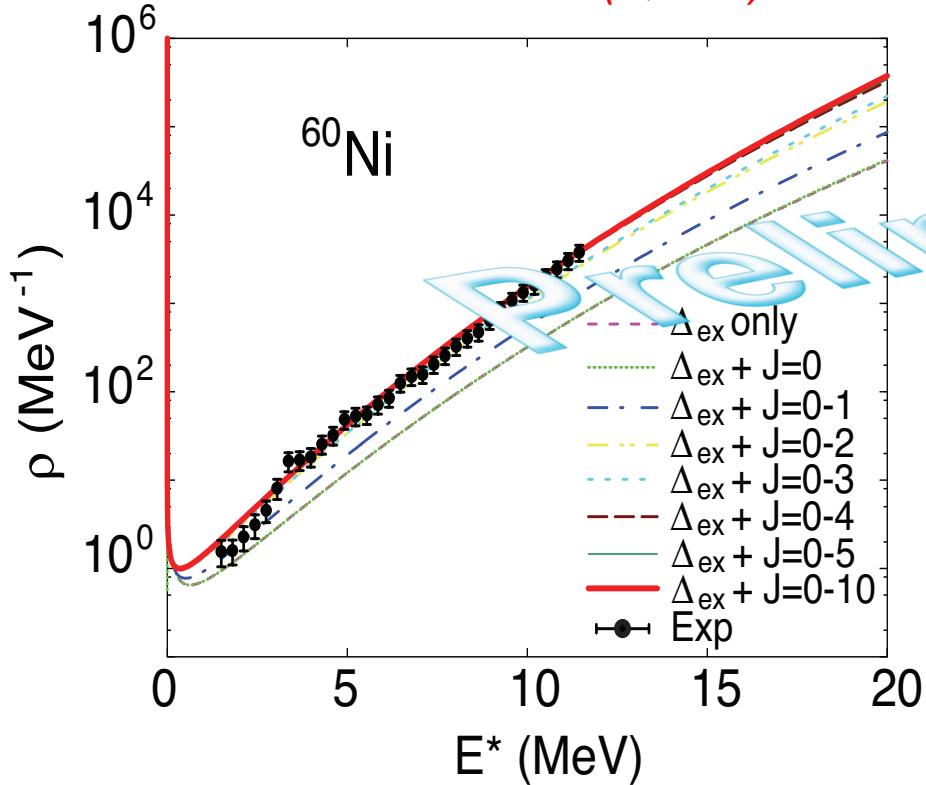


Research Topics

Future perspectives

✧ *NLD and RSF*

➤ *Theory: EP+IPM with collective and rotational enhancement factors calculated from RPA (QRPA)*



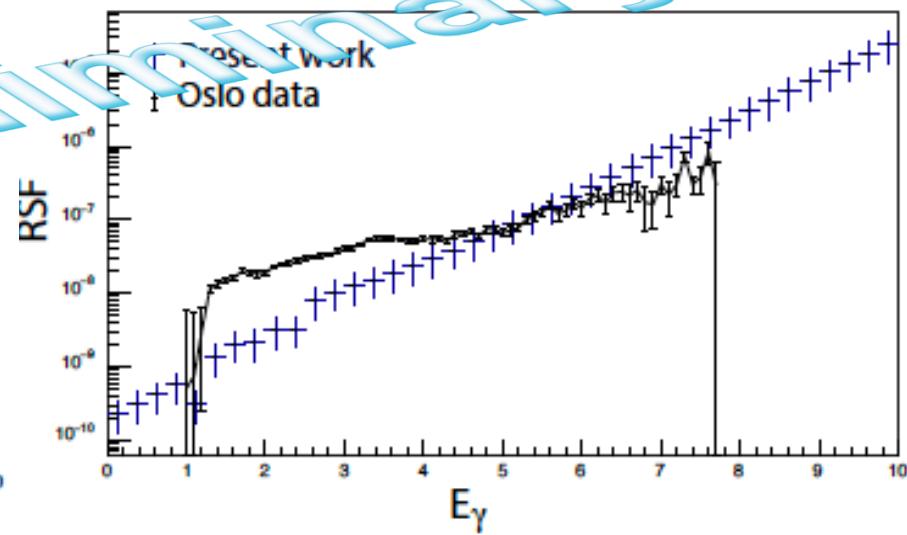
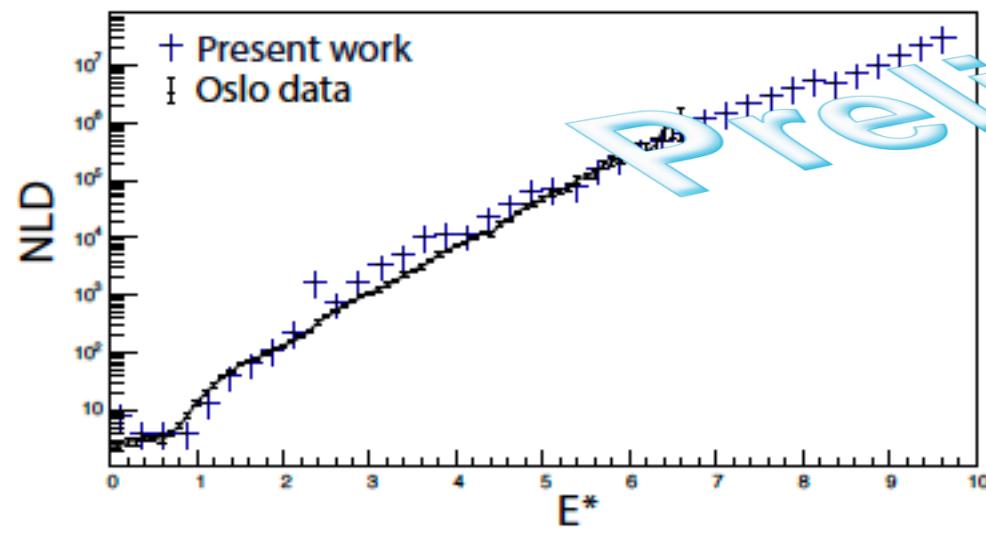
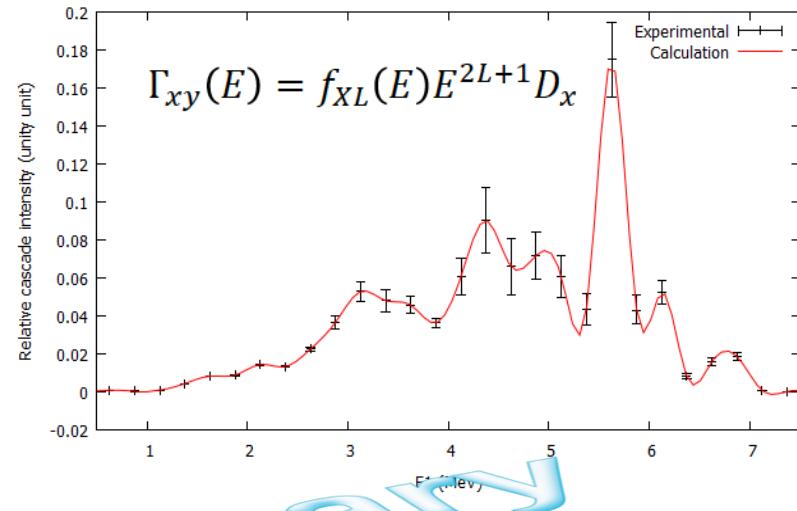
Research Topics

Future perspectives

✧ NLD and RSF

- Theory: extend EP+IPM with collective and rotational enhancement factors calculated from RPA (QRPA)
- Experiment: extract NLD and RSF from gamma spectra of (n_{th} , γ) reactions

$$I_{gg}(E1, E2) = \sum_{XL, J, \Pi} \frac{\Gamma_{im}(E1)}{\Gamma_i} \rho_m(B_n - E1, J, \Pi) \frac{\Gamma_{mf}(E2)}{\Gamma_m}$$



Research Topics

□ Future perspectives

❖ *NLD and RSF*

➤ *Experiment: extract NLD and RSF from gamma spectra of compound reactions or evaporation spectra*

Reactions to be used

- Cyclotron: ($^3He, \alpha$); ($^3He, ^3He'$); beam energy 10 – 30 MeV
- Pelletron: (d, n); (p, α); (p, n); ($^{12}C, p$); beam energy 5 – 40 MeV

30MeV Cyclotron



Tandem Pelletron 5SDH-2



Conclusion

Nuclear Theory Group at DTU

- ❖ Group members: 3
- ❖ Collaborators: from Japan, Indian, USA,...
- ❖ Research Topics
 - Past: pairing in hot rotating nuclei; nuclear giant (GDR) and pygmy (PDR) dipole resonances; viscosity in hot rotating nuclei.
 - Present: pairing reentrance; NLD and RSF; nuclear level scheme from (n_{th}, γ) reactions; ZSM-5 materials using PALS and XRD.
 - Future: pairing reentrance; fully microscopic approach to NLD and RSF; NLD and RSF from (n_{th}, γ) reactions; zeolite materials synthesized from Kaolin source in Vietnam and studied using the PALS and XRD.

Thank you !